# Effects of Foundation Characteristics and Building Separation Gap on Seismic Performance of Mid-rise Structures Incorporating Soil-Foundation-Structure-Interaction

### By

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A thesis submitted in fulfilment of the requirement for the degree of Doctor of Philosophy

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I hereby certify that the work embodied in this Thesis is the result of original research and has not previously been submitted for a degree nor has it been submitted as part of requirements for a degree except as fully acknowledged within the text.

I also certify that the thesis has been written by me. Any help that I have received in my research work and the preparation of the thesis itself has been acknowledged. In addition, I certify that all information sources and literature used are indicated in the thesis.

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(Quoc Van Nguyen)

Sydney, July 2017

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# LIST OF PEER-REVIEWED PUBLICATIONS BASED ON THIS RESEARCH

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- Nguyen, Quoc Van, Fatahi, Behzad and Khabbaz, Hadi. 'Three dimensional numerical simulation to predict performance of laterally loaded piles on clay-sand layered slope'. *International Conference GeoMontreal 2013*, Sep-Oct 2013, Montreal, Canada.
- Nguyen, Quoc Van, Fatahi, Behzad and Hokmabadi, S Aslan, 'Influence of Shallow Foundation Characteristics on Seismic Response of Mid-rise Buildings Subjected to Strong Earthquakes', *International Conference GeoChina 2016*, July 25-27, 2016, Shandong, China, Page 117-124.

#### ABSTRACT

Seismic waves travel many kilometres and pass through soil layers close to the ground surface before hitting the structures. The seismic induced dynamic behaviour of structures built on soft soil is highly dependent on the soil properties and the foundation type due to their interactions during an earthquake event. The design of building structures needs to consider seismic soil-foundation-structure interaction, where the building responses vary significantly depending upon the fixity of the base condition due to the interaction between the ground and the foundation as well as the building structures. This interaction is called "Seismic Soil-foundation-structure-interaction" (SSFSI). For a typical soil and foundation, SSFSI analysis shows lower natural frequency of the structural system and higher effective damping ratio compared to the traditional analysis with fixed base condition. This can considerably alter the response of the building frames under the seismic excitations by influencing the structural demand of the building as well as amplifying the lateral deflections and inter storey drifts of the superstructure. This phenomenon is highly influenced by the foundation type (i.e. shallow and deep foundation) and may change the performance level of buildings in the performance based design approach. Therefore the interaction should be considered in design of buildings subject to seismic activities so as to provide a safe and cost effective structural system.

In this study, a rigorous numerical modelling approach was developed and used to build numerical tests for different foundation types and sizes as well as the pounding effects between buildings. The results consisted of lateral deformation, inter-storey drifts, levelling shear forces of the structures, foundation rocking, impact force and pile responses. These perimeters cover a wide range of earthquake inputs and foundation characteristics.

The first step was that the soil-pile-interaction numerical behaviour was investigated in a case study of lateral loaded pile considering the shear plastic deformation of the layered sloping ground including sand and clay layers. Appropriate subroutines were adopted to simulate the soil-pile-interaction which included the incorporation of gapping and sliding (in normal and tangential directions) at the interface. A wide range of parameters for this numerical modelling was validated through comparison with an array of a full-scale lateral loaded pile experiments. Secondly, dynamic characteristics of soil-foundation-structure system were investigated for seismic response of a mid-rise moment resisting building on shallow foundation under four well-known earthquakes. By adopting a direct calculation method, the numerical model can perform a fully nonlinear time history dynamic analysis for three-dimensional numerical model with different foundation sizes where the infinite boundary, sliding and separation in soil-foundation was taken into account. In addition, the influence of foundation sizes on natural frequency and structure response spectrum was also studied. The results confirmed that when the size of shallow foundation is reduced, the natural period would lengthen, the base shear would reduce significantly while the lateral deformation, inter-storey drift and foundation rocking would increase.

Thirdly, the comprehensive pile foundation investigation concludes that the type and size of a pile foundation that supports mid-rise buildings in high-risk seismic zones can alter the dynamic characteristics of the soil-pile-foundation system during an earthquake due to soil-structure-interaction. It is not true to believe that longer piles can provide safer condition under earthquake loading. In fact, by increasing the length of floating piles the structure undergoes more maximum lateral deflection, more inter-story drift and more total maximum levelling shear force but less foundation rocking. This can be explained due to the fact that longer pile foundation has higher contact surface with surrounding soil which enable them to absorb extra seismic energy. This finding can be the recommendation for design engineers that the pile should not lengthen too much to reduce the seismic effects.

Finally, the separation gap between moment resisting and two shear wall braced buildings on pile foundation under seismic loading was studied. The result from this numerical modelling showed that pounding impact influences the distribution of shear force which disturbs the natural vibration and in extreme case, causes collapse. The outcome of this study provides essential insight to geotechnical and structural engineers when designing neighbouring structures in earthquake prone areas.

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# LIST OF ABBREVIATIONS

Full text	Abbreviation
American Society of Civil Engineers design code	ASCE
Boundary element method	BEM
Building Seismic Safety Council	BSSC
Complete quadratic combination	CQC
Earthquake design category	EDC
Earthquake Wave Equation Analysis for Piles	EQWEAP
Federal Emergency Management Agency	FEMA
Global Positioning System	GPS
International Building Code	IBC
Linear dynamic procedure	LDP
Linear static procedure	LSP
National Earthquake Hazards Reduction Program	NEHRP
National Computational Infrastructure	NCI
Nolinear dynamic procedure	NDP
Nonlinear static procedure	NSP
Seismic Soil-foundation-structure-interaction	SSFSI
Seismic soil-pile-structure interaction	SSPSI
Single degree of freedom	SDOF
Soil-foundation-structure interaction	SFSI
Soil-pile-structure interaction	SPSI
Soil-structure-interaction	SSI
Structure-soil-structure-interaction	SSSI
Thin layer method	TLM

# LIST OF NOTATIONS

a(t)	raw data record
$a_c(t)$	corrected acceleration record
$a_0(t)$	acceleration correction
2 <i>a</i>	width of the foundation
Α	Area, foundation width, cohesion
$A_{loop}$	area of the hysteresis
[A]	Damping matrix
В	width of the pile
$B_b$	width of building
$B_f$	width of foundation
$B_s$	width of soil model
С	damping coefficient, soil cohesion
$c_h$	damping coefficient in horizontal direction
$c_{ heta}$	damping coefficient in rotation direction
$\widetilde{C}$	equivalent damping coefficient
$C_1, C_2, C_3, C_k$	modification factor for pseudo lateral load, constant
<i>c'</i>	cohesion, effective cohesion
$c_p, c_s$	velocities of the normal wave and shear wave
CL	clayey soil
[ <i>C</i> ]	damping matrix
D	diameter of pile
Drift	maximum inter-storey drifts of the building
$d_p$ , $d_s$	distributed damping in the normal and shear directions
$d_c$	decay coefficient
$d_{i+1}$ , $d_i$	Deflection at level $(i + 1)$ and $(i)$
$d_i(t)$	deflection history at level (i)
Ε	Young's modulus, modulus of elasticity of concrete
$E_a, E_b, E_c, E_d, E_e$	Soil classification according to AS1170.4 (2007)
Es	soil subgrade reaction
$E_p$	Young's modulus of pile

t each level Rayleigh damping
Rayleigh damping
Rayleigh damping
il thickness, soil height
axis
stiffness
ase
a

$L_b$	length of building
$L_f$	length of foundation
$L_{FE}$	length of finite element section
L <sub>INF</sub>	length of infinite element section
т	mass
М	bending moment
[ <i>M</i> ]	mass matrix
$M_w$	moment magnitude of earthquake in Richter scale
Р	lateral load
p	load, contact pressure
$p_i$	load in segment (i)
$P_0$	amplitude of harmonic force
P <sub>x</sub>	axle force from structure applied to pile head
PI	plasticity index
PGA	peak ground acceleration
$q_{s}$	lateral distributed load from soil to the pile
$q_{\mathrm{y}}$	lateral distributed load along the beam
Q	Impose Action, shear force along the pile
R <sub>int</sub>	reduction factor
r <sub>in</sub>	inner radius of the pile
r <sub>out</sub>	outer radius of the pile
SDOF	single degree of freedom
S	slope (or rotational deflection) of the pile, distance
S <sub>a</sub>	response spectrum acceleration, spectral acceleration
$S_{DS}$	design earthquake motion
<i>s</i> <sub>i</sub>	minimum distance between adjacent structure at level (i)
$S_u$	undrained shear strength
$(S_u)_{soil}$	undrained shear strength of soil
$[(S_u)_{int}]$	reduce shear strength at the interface
SD	separation gap
Δ	lateral deflections in $P - \Delta$ effect
$\Delta_{i1}, \Delta_{i2}$	lateral deflections of neighbouring structures

Т	fundamental period
$\widetilde{T}$	effective fundamental period
$T_0$	characteristic period of the response spectrum
$T_1$ and $T_2$	limits of a time interval
t	time
$u_0$	structural distortion
$u_t^0$	total initial lateral displacement
$u_t$	total lateral displacement
$\widetilde{u_g}$	equivalent input motion
$u_i, u_j$	material particle displacement
$u_i(t)$	horizontal displacement history at level (i)
$u_0(t)$	horizontal displacement history at level (0)
$\ddot{u_l}$	material particle acceleration
V	pseudo lateral load, shear force
$V_S$	shear wave velocity
$V_{S0}$	average shear wave velocity
$v_c(t)$	corrected velocity record
W	total dead load and anticipated live load
W	total dead load and anticipated live load of structure fix at base
$W_D$	dissipated energy
$W_S$	the maximum strain energy
$x_i$	position of pile at segment ( <i>i</i> )
Y	deflection, pile deflection
${\mathcal Y}_{\mathbf i}$	deflection in segment (i)
$z_{ m i}$	depth of soil at segment ( <i>i</i> )
α, β	mass damping coefficient and stiffness damping coefficient
γ	shear strain, unit weight
$\dot{\gamma}_1$ and $\dot{\gamma}_2$	two local slip velocity components
$\gamma_c$	cyclic shear strain, shear strain
$\gamma_{max}$	maximum shear strain
Ϋ́eq	equivalent slip rate
ε	strain of concrete material

€ <sub>yield</sub>	strain at yield point
Z	damping ratio
Θ	angle
μ	coefficient of friction
$\mu_r$ , $\mu_p$	residual coefficient of friction, peak coefficient of friction
ν	Poisson's ratio
$\xi_0$	hysteretic damping
Ξ	damping ratio
Ĩ	equivalent damping ratio
ρ	density, mass density
$\sigma,\sigma'$	normal stress, effective normal stress
$\sigma_{ m y}$ , $\sigma_{ m yield}$	yield stress of concrete material
τ	shear strength
$ au_1$ and $ au_2$	two orthogonal components of shear stress
$ au_{cr},  au_{crit}$	critical shear stress
$ au_{eq}$	equivalent shear stress
$ au_c$	shear stress
arphi,arphi'	internal frictional angle, effective internal frictional angle
$\psi$	dilation angle
$\omega, \omega_0$	natural frequency
$\omega_i, \omega_j$	natural angular frequency for mode $(i)$ and $(j)$
$\widetilde{\omega}$	equivalent natural frequency
$\phi$ , Ø and Ø'	friction angle and effective friction angle