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State-of-Power Estimation of Li-ion Battery Considering Battery Surface Temperature

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Abstract: The State-of-Power (SOP) of Li-ion battery (LIB) is an important evaluation index for security control and energy recovery of electric vehicles. Major state estimation methods are only applicable to fixed room temperature at 20°C. Actually, the battery capacity and resistance vary dramatically with the change of battery surface temperature in the working process of the battery, which causes significant errors in state estimation if only room temperature is assumed. The inaccurate state may cause further excessive current at high or low temperatures to affect security and life cycle of the battery. Therefore, a novel state estimation method applicable to various battery surface temperatures is developed in this paper. This method establishes Capacity-Temperature relations and Resistance-Temperature relations from experimental data to predict more accurately battery capacity and resistance in the full temperature range, then applies the Extend Kalman Filter technique to estimate the State of Charge, and an algorithm with multi-parameters constrained to estimate the SOP of LIB. Simulation and experimental results show that the
proposed method can obtain accurate SOP results at different temperatures.

**Keywords:** Li-ion battery; State-of-Power; Temperature model; Temperature rising characteristic; algorithm with multi-parameters constrained

1 Introduction

In recent years, electric vehicle (EV) technology has been developed quickly because of increasingly serious energy supply shortage and environmental concerns. As the main power source of EVs, Li-ion battery (LIB) has attracted intensive research. State-of-Power (SOP) is an important evaluation index to characterize the charging or discharging peak power of LIB. SOP is used to evaluate whether the battery pack has sufficient power to meet the starting or acceleration demand of EVs. At the braking state, SOP can help to determine the maximum energy recovered by the battery and thus avoid overcharging. Moreover, accurate SOP estimation result can benefit vehicle performance control by optimizing battery capacity and size [1,2,3]. Therefore, it is important to estimate SOP accurately, and this paper aims to develop a new SOP estimation method which will have a satisfactory accuracy under various temperatures.

SOP of LIB is related to battery capacity, resistance, State-of-Charge (SOC) and ambient temperature amongst others [4], and the estimation of SOP needs to consider all these factors. In Ref. [5], Hybrid Pulse Power Characterization (HPPC) method is applied to estimate SOP. This method uses internal resistance, open-circuit voltage (OCV) and cut-off voltage to obtain the peak power of the battery. Another SOP estimation method based on SOC limits (MSL) is introduced in Ref. [6], where discharging peak current is obtained by the current SOC and minimum SOC limit over a given time period. In Ref. [1], a SOP estimation method based on voltage limit is proposed, in which
complex but more accurate battery models, such as an Equivalent Circuit Model (ECM) or Combined Model (CM), are applied to build the state-space equations of LIB. The peak current at the voltage limit is obtained to calculate the SOP of the battery.

In the above methods, the HPPC method and the MSL are unable to describe the characteristics of lithium batteries accurately due to the inaccurate models used, while the method based on voltage limit ignores the SOC limits and the maximum current provided by the manufacturer. Therefore, these three methods often cause the estimated SOP greater than the actual peak power, and the battery controlled by such an over-estimated SOP will suffer from over-charging, over-discharging or over-current and thus a shortened battery life period.

To improve the accuracy of the SOP estimation, some researchers propose the neural network method [7] and Algorithm with Multi-Parameters Constrained (AMPC) [2,3,8,9]. Neural network method is suitable for state estimation of LIB with a high accuracy degree. However, this method relies on a lot of training data and a proper training technique, otherwise its accuracy will be compromised. The AMPC compares the maximum current provided by the manufacturer with the peak currents obtained from two methods: the one based on SOC limit and the one based on voltage limit. Then it chooses the minimum one in order not to exceed the allowed current and power limit. Thevenin equivalent circuit model is used in AMPC to estimate the SOP in Ref. [8]. The electro-chemical polarization battery model is used in [2,3,9] to estimate the peak current at voltage limits, and then the SOP is estimated by AMPC.

Major battery state estimation methods are always applied at fixed room temperature (FRT) at 20°C, and the parameters of battery capacity and resistance are set as constants. Some methods are
applied at fix ambient temperature (FAT) which is equal to the initial battery surface temperature, and the parameters of battery capacity and resistance are set as functions varying with the ambient temperature but not the battery surface temperature. However, significant surface temperature change is inevitable in EV batteries because of the heat generated by the battery itself. Actually, these parameters of LIB change against SOC and battery surface temperatures. And particularly the change of battery temperature will cause sharp fluctuations in those parameters. When the battery surface temperature decreases, the slow kinetics of reactions and the reduced ionic conductivity of electrolyte result in lower capacity and higher resistance of battery [10,11]. Battery impedance online estimation and adaptive power prediction are studied considering such a battery surface temperature problem in [12], however, it studies only the temperature at 10°C.

Targeting at these problems, a state estimation method considering battery dynamic surface temperature is proposed in this paper. The effect of battery temperature on the parameters of LIB is studied. The capacity and resistance of the LIB are tested at different temperature to build the temperature models which can help to identify how the parameters of LIB vary against battery temperature. The battery performance model is optimized with the aid of temperature models to describe the dynamic characteristics of the LIB at different temperatures. The Extend Kalman Filter (EKF) technique at DBT is applied to estimate the battery SOC, and then an AMPC at DBT with the constraints from SOC and other parameters is applied for the estimation of battery SOP which will ensure the safe operation and energy recovery efficiency of the battery. Finally Dynamic Stress Test (DST) [13] is carried out under different temperatures to verify the accuracy of the temperature models and SOP estimation algorithm. Compared with existing methods, this new method achieves
the complete SOP estimation in the full temperature range with high accuracy. Moreover, this method is simple and suitable for practical application.

This paper is organized as follows. Temperature rising characteristic of LIB and temperature models of capacity and resistance are shown in Section 2. An SOP estimation model considering battery temperature is presented in Section 3. The experiments and simulation results are reported in Section 4. The conclusions are presented in Section 5.

2 Building the dynamic model of LIB

Since this paper targets to develop a new SOP estimation method applicable to all temperatures, it is necessary to study first how the relevant battery parameters change against temperature. Based on experimental data, this section establishes the relation between temperature, battery resistance and capacity, and then a dynamic model of LIB is built.

2.1 Temperature characteristics of LIB

The cylindrical LIB of type IFP3213100EA manufactured by Guoxuan High-Tech Power is chose to study its temperature characteristics, and the rated capacity is 9AH. The LIB is placed in an incubator, and ambient temperature in the incubator is set as -10°C, 0°C and 25°C respectively. Then the constant current discharge test of 2C and Dynamic Stress Test (DST) [13] are conducted to observe the temperature rising of the battery, where 2C represents two times of rated battery current. The DST curve and temperature rising results are shown in Fig.1, Fig.2 and Fig.3:
Fig. 1 Working condition of a single DST

Fig. 2 Surface temperature rising in constant current discharge test of 2C
Fig. 1 illustrates the test conditions of a single DST, where the current (in Amperes) at different time instant is given. Fig. 2 and Fig. 3 show the surface temperature rising of LIB at different ambient temperature in constant current discharge test and DST. And the temperature increases significantly at the discharging process as shown in Table 1:

<table>
<thead>
<tr>
<th>Working Condition</th>
<th>Ambient Temperature</th>
<th>Surface Temperature</th>
<th>Temperature increased</th>
<th>Working Time</th>
</tr>
</thead>
<tbody>
<tr>
<td>Constant Current Test</td>
<td>-10°C</td>
<td>10.55°C</td>
<td>20.55°C</td>
<td>17.5 min</td>
</tr>
<tr>
<td></td>
<td>0°C</td>
<td>18.42°C</td>
<td>18.42°C</td>
<td>20.5 min</td>
</tr>
<tr>
<td></td>
<td>25°C</td>
<td>39.81°C</td>
<td>14.81°C</td>
<td>25.5 min</td>
</tr>
<tr>
<td>DST</td>
<td>-10°C</td>
<td>0.81°C</td>
<td>10.81°C</td>
<td>80 min</td>
</tr>
<tr>
<td></td>
<td>0°C</td>
<td>8.73°C</td>
<td>8.73°C</td>
<td>91.5 min</td>
</tr>
<tr>
<td></td>
<td>25°C</td>
<td>30.06°C</td>
<td>5.06°C</td>
<td>121 min</td>
</tr>
</tbody>
</table>

The ambient temperature, the battery surface temperature and the temperature increased after the whole discharging process from 100% SOC to the protection voltage, the continuous working
time are shown in Table 1. Fig.2, Fig.3 and Table 1 show that the temperature rises quickly at low ambient temperatures. If we compare the results at the same time interval, the conclusion is more obvious. The heat at the battery discharge process consists of the heat from resistance and the heat from chemistry reactions, where the heat from resistance occupies the majority of the heat [14]. So the underlying reason of the quick temperature rise is that the resistance is higher at low temperatures, and thus low ambient temperature has a more significant impact on state estimation of LIB.

### 2.2 Temperature model of battery capacity

In order to find out how the battery usable capacity changes at different temperatures, a fully charged battery is discharged with constant current at different temperatures in an incubator. To avoid the impact of temperature rising on capacity test, the discharging current is set as 0.1C, and the surface temperature is detected in real time to ensure that the battery temperature rises within a permitted range. The ambient temperature is set as -20°C, -10°C, 0°C, 10°C, 20°C, 30°C and 40°C in turn. The measured LIB usable capacities under different temperatures are shown in Fig. 4.
In Fig. 4, the vertical axis is the ratio of capacity under the current temperature and usable capacity under room temperature (20°C), the horizontal axis is the ambient temperature. The figure shows that the LIB usable capacity decreases fast at lower ambient temperatures. At -20 °C, the capacity is only about 30% of the rated capacity which is measured at room temperature (20°C). As the temperature rises, the change rate of the usable capacity gradually reduces. At 40°C, the capacity is about 105% of the rated capacity.

Capacity temperature compensation coefficient $\lambda_c = C_T / C_0$ is defined to characterize the effect of temperature on LIB capacity, where $C_T$ is the capacity at temperature $T$, $C_0$ is the capacity at 20°C. The curve is fitted by the Arrhenius equation [15], and $\lambda_c$ can be expressed as:

$$\lambda_c = C_T / C_0 = B_C e^{-E_a / R T} + A_C$$

(1)

where $B_C$ is the pre-exponential factor, $E_a$ is the activation energy, $R$ is the gas constant, $T$ is the absolute ambient temperature, $A_C$ is Arrhenius correction factor. The fitted curve is shown as the
dashed line in Fig. 4, which is close to the measured capacity points.

2.3 Temperature model of battery resistance

In order to find out how the battery resistance changes at different temperatures and SOC, the Hybrid Pulse Power Characteristic (HPPC) [16] test is conducted, where the resistance refers to the total battery resistance. Firstly, a fully charged battery is put in the incubator of 40°C and discharged with constant current of 1/3C to the SOC of 90%, 70%, 50%, 30% and 10% successively, and the HPPC tests are conducted at each SOC to obtain the resistance of the LIB. Then, change the incubator temperature to 30°C, 20°C, 10°C, 0°C, -10°C and -20°C, repeat the above steps, and measure the battery resistance.

Fig. 5 Resistance of LIB under different temperatures and SOC

Fig. 5 shows how the resistance varies at different temperatures and SOC. The vertical axis is the ratio of resistance at the current temperature to the resistance at 20°C, and the horizontal axis is
the ambient temperature. The dashed line is the fitted curve. The figure shows that the resistance changes fast at low ambient temperatures. Furthermore, the resistances at different SOCs (higher than 10%) remain almost the same when temperature is fixed. Therefore, the impact of SOC on resistance can be ignored when the battery SOC is higher than 10%. As shown in Ref. [11], the resistance of the battery changes fast when SOC is lower than 10%, so the effect of SOC on resistance cannot be ignored when SOC is lower than 10%.

Resistance temperature compensation coefficient $\lambda_R = R_T / R_0$ is defined to characterize the effect of temperature on the LIB resistance, where $R_T$ is the resistance at temperature $T$, $R_0$ is the resistance at 20°C. The curve is fitted by Arrhenius equation, and $\lambda_R$ can be expressed as:

$$\lambda_R = R_T / R_0 = B_R e^{-E_a^R / R T} + A_R$$

(2)

where $B_R$ is the pre-exponential factor, $E_a^R$ is the activation energy, $R$ is the gas constant, $T$ is the absolute ambient temperature, $A_R$ is Arrhenius correction factor. The fitted curve is shown as the dashed line in Fig.5, which is close to the measured resistance points.

2.4 Dynamic model of LIB

In order to estimate the SOP of LIB accurately, the battery model should be built first. Widely used battery models are electrochemical model [17], equivalent circuit model [18, 19] and neural network model [20]. The electrochemical reaction mechanism of LIB is very complex. Therefore, the simplified electrochemical model such as the Shepherd, Unnewehr, Nernst model is used to describe the battery characteristics. Equivalent circuit model in [18, 19] describes the LIB from external electrical characteristics and PNGV, Thevenin and Rint model are typical equivalent circuit models. The calculation of neural network model in [20] is too complicated, and the estimation error
will be affected by the training data and training methods. Thus the combined electrochemical model (CM) from [1, 21, 22] is used in this paper. This CM consists of the Shepherd, Unnewehr and Nernst model, which solves the problem that the three models only match partially the LIB voltage characteristic: For example, the Shepherd model only considers the end of battery charge and discharge, and the Unnewehr model cannot express the voltage platform. Thus the CM model can provide better fitting in the whole charge and discharge interval. However, the effect of temperature on battery parameters is ignored which will lead to the poor accuracy at low temperatures. Therefore, the above temperature models are merged to this combined electrochemical model to describe the dynamic behavior of LIB at various temperatures. Details are given below:

\[
SOC(t)=SOC(0)+\int_0^t \eta i(t) dt / (\lambda_C C_0)
\]

(3)

\[
E(t)=E_0-\lambda_R R_0 i(t)-K_0 SOC(t) - K_1 SOC(t) - K_2 \ln(SOC(t))+K_3 \ln(1-SOC(t))
\]

(4)

where \(SOC(t)\) is the instantaneous SOC at time \(t\), \(SOC(0)\) is the initial SOC, \(\eta\) is the charging/discharging efficiency, \(i(t)\) is the current at time \(t\), \(C_0\) is the capacity at room temperature, \(E(t)\) is the terminal voltage at time \(t\), \(E_0\) is the OCV of the fully charged battery, \(R_0\) is the resistance at room temperature, \(K_0, K_1, K_2\) and \(K_3\) are constants. \(\lambda_C\) and \(\lambda_R\) are capacity and resistance temperature compensation coefficient respectively.

3 SOP estimation considering battery temperature

3.1 SOC estimation method

Extended Kalman Filter (EKF) is a popular algorithm to solve the nonlinear system state estimation problem [22]. Now Eq. (3) and Eq. (4) are discretized to obtain the state-space model of LIB. Let \(x_k=SOC_k\), \(y_k=E_k\), \(u_k=i_k\), then:
\[ x_k = f(x_{k-1}, u_{k-1}) + w_k = x_{k-1} - \eta u_{k-1} \Delta t (\lambda_C C_0) + w_k \]  
(5)

\[ y_k = g(x_k, u_k) + v_k = E_0 - \lambda_R R_0 u_k - K_0 / x_k - K_1 x_k + K_2 \ln(x_k) + K_3 \ln(1-x_k) + v_k \]  
(6)

Linearizing Eq. (6) and Eq. (7), and we will obtain:

\[
\begin{aligned}
  x_k &= A x_{k-1} + B u_{k-1} + w_k \\
  y_k &= C x_k + D u_k + E + v_k
\end{aligned}
\]  
(7)

where

\[
A = \frac{\partial f(x_{k-1}, u_{k-1})}{\partial x_{k-1}} \bigg|_{x_{k-1} = \hat{x}_{k-1}} = I,
\]

\[B = -\eta \Delta t (\lambda_C C_0),\]

\[C = \frac{\partial g(x_k, u_k)}{\partial x_k} \bigg|_{x_k = \hat{x}_k} = \frac{K_0}{(\hat{x}_k)^2} - K_1 + \frac{K_2}{\hat{x}_k} + \frac{K_3}{1-\hat{x}_k},\]

\[D = -\lambda_R R_0,\]

\[E = V_0 - \frac{2K_0}{\hat{x}_k} + K_2 (\ln \hat{x}_k - 1) + K_3 (\ln(1-\hat{x}_k) + \frac{\hat{x}_k}{1-\hat{x}_k}).\]

In EKF estimation method, SOC is calculated with AH integral method, and put into the observation equation to calculate the Kalman gain of each step. It reflects the residuals on the state variable weights of SOC, and then the optimal SOC estimation is obtained from the updated state estimation equation.

3.2 SOP estimation with AMPC

In order to ensure the accuracy of the SOP estimation, the AMPC is combined with EKF to estimate the SOP of LIB. Within a short time duration \( \Delta t \), the battery can be assumed to be discharged at a constant current, and after the short time \( \Delta t \) about 10 seconds \([13,24]\),

\[\text{SOC}(t+\Delta t) = \text{SOC}_{\text{min}} \quad \text{or} \quad V(t+\Delta t) = V_{\text{min}}.\]

Then the discharge peak power is

\[\text{SOP}(t) = I_{\text{max}}(t) E(t, I_{\text{max}}(t))\]  
(8)
where \( \text{SOP}(t) \) is the instantaneous state of charge at time \( t \), \( i_{\text{max}}(t) \) is the estimated peak current at time \( t \), \( E(t,i_{\text{max}}(t)) \) is the terminal voltage at time \( t \) when the current is \( i_{\text{max}}(t) \).

Based on the above models, the peak current can be calculated from SOC limit, which is denoted by \( u_{\text{max}}^{\text{SOC}} \) and equals:

\[
    u_{\text{max}}^{\text{SOC}} = B^{-1}(x_k - x_{\text{min}}) \tag{9}
\]

This peak current can also be calculated from voltage limit, which is represented by \( u_{\text{max}}^{\text{volt}} \) and equals:

\[
    u_{\text{max}}^{\text{volt}} = D^{-1}(y_{\text{min}} - Cx_k - E) \tag{10}
\]

Note also that manufacturers also provide the rated battery maximum current, which is denoted by \( u_{\text{max}} \), therefore, these notations can be combined together and the following maximum allowed peak discharge current \( u_{\text{max}}^{\text{dis}} \) is defined as

\[
    u_{\text{max}}^{\text{dis}} = \min(u_{\text{max}}^{\text{SOC}}, u_{\text{max}}^{\text{volt}}) \tag{11}
\]

Therefore, the maximum allowed discharge peak power is

\[
    \text{SOP}_{\text{max}}^{\text{dis}} = u_{\text{max}}^{\text{dis}} y(k,u_{\text{max}}^{\text{dis}}) \tag{12}
\]

The detail SOC and SOP estimation process is shown as follows:
Fig. 6 SOP estimation flow chart

Form the above flow chart, we can see that the algorithm is very simple and straightforward, and it is suitable for practical engineering applications such as Battery Management System (BMS).

In order to validate the accuracy of the estimation algorithm, the simulations and experiments are conducted in Section 4.

4 Simulations and Experiments

4.1 Parameters identification

In order to identify the model parameters, we choose the 9Ah Lithium iron phosphate battery
and conduct the constant current discharge test and HPPC test. The measured data are fitted by Arrhenius equation to obtain the temperature models of capacity and resistance as shown in Fig.4 and Fig.5. The model parameters are identified by the least squares method, and the results of parameters for the temperature models of battery capacity and residence are shown in Table 2 and Table 3:

<table>
<thead>
<tr>
<th>Parameter</th>
<th>( B_C )</th>
<th>( E_C^* )</th>
<th>( A_C )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Value</td>
<td>-1.683*10^{-6}</td>
<td>-2.77*10^4</td>
<td>1.117</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Parameter</th>
<th>( B_R )</th>
<th>( E_R^* )</th>
<th>( A_R )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Value</td>
<td>1.861*10^{-4}</td>
<td>-2.08*10^4</td>
<td>5.23*10^{-2}</td>
</tr>
</tbody>
</table>

4.2 The Dynamic Battery Model Validation

In order to validate the dynamic model in Eq. (4), a single LiFePO\(_4\) cell with a nominal capacity of 9Ah is chosen to be tested in an incubator with the temperature of -10°C, 0°C and 25°C successively. The battery is fully charged and the DST curve is chosen as the discharge curve which is provided in “USABC Electric vehicle battery test procedures manual” [13]. And the comparison between the voltage response curve of the dynamic model, the voltage response of the initial model and the test voltage is shown as follows.
In Fig. 7 the voltage response curve of the dynamic model (Dy-model), the voltage response of the initial model (In-model) and the test voltage (Test) are shown respectively. The proposed dynamic battery model is obviously better than the initial model.

4.3 SOC Estimation Validation

The single LiFePO₄ cell with a nominal capacity of 9Ah is chosen to be tested in an incubator with the temperature of -10°C, 0°C and 25°C successively. The battery is fully charged and the DST curve is chosen as the discharge curve which is provided in “USABC Electric vehicle battery test procedures manual” [13]. The SOC at fixed room temperature (SOC at FRT), the SOC at fixed ambient temperature (SOC at FAT), the SOC at dynamic battery temperature (SOC at DBT) and the real SOC are shown as follows:
Fig. 8 SOC estimation result at -10°C

Fig. 9 SOC estimation result at 0°C
In Fig. 8, Fig. 9 and Fig. 10, the SOC estimation curves after DST at temperature of -10°C, 0°C and 25°C are shown respectively. And the maximum errors are shown in Table 4:

<table>
<thead>
<tr>
<th>Ambient Temperature</th>
<th>Max-error of FRT</th>
<th>Max-error of FAT</th>
<th>Max-error of DBT</th>
</tr>
</thead>
<tbody>
<tr>
<td>-10°C</td>
<td>11.89%</td>
<td>22.40%</td>
<td>3.66%</td>
</tr>
<tr>
<td>0°C</td>
<td>5.92%</td>
<td>9.61%</td>
<td>2.07%</td>
</tr>
<tr>
<td>25°C</td>
<td>4.91%</td>
<td>3.93%</td>
<td>2.94%</td>
</tr>
</tbody>
</table>

From Table 4, we can see that the error of SOC at DBT is smaller than SOC at FRT and SOC at FAT, especially at low temperature. The reason is that the resistance of LIB is higher at low temperatures, so the battery temperature rises higher at DST. Besides, same temperature variation has a bigger impact on the parameters at low temperature as shown in Fig. 4 and Fig. 5. These reasons cause a poor performance of SOC estimation methods which do not consider temperature impact.
4.4 SOP Estimation Validation

In order to verify the SOP estimation algorithm, the real SOP of the battery at different temperature needs to be tested. The test method recommended in [24] is adopted in this paper. The battery is discharged and charged alternatively with the current of 1C, 2C, 5C and 10C at certain SOC and temperature shown in Fig.2 and Fig. 3. In this process, the voltage of the battery is recorded and fitted to obtain the maximum current at the cut-off voltage. Then the peak power of the battery at any SOC and temperature point is the multiplication of the cut-off voltage and maximum current. The SOP at fixed room temperature (SOP at FRT), the SOP at fixed ambient temperature (SOP at FAT), the SOP at dynamic battery temperature (SOP at DBT) and the real SOP are shown as follows:

![SOP estimation result at -10°C](image)

Fig.11 SOP estimation result at -10℃
In Fig. 11, Fig. 12 and Fig. 13, the SOP estimation curves after DST and the real SOP at temperatures of -10°C, 0°C and 25°C are shown respectively. In these figures, SOP at DBT which is nearer to the real SOP curve performs better than SOP at FRT and SOP at FAT. Comparing the three
SOP curves, we will see that the result of SOP at FRT is higher than the results of SOP at FAT and DBT at low temperatures; but it is lower at high temperatures. The reason is that the battery resistance is higher at low temperatures and lower at high temperatures. When comparing SOP at FAT and DBT, the result of DBT is nearly the same with the result of FAT at the initial discharging process. The results of SOP at DBT increase quicker than SOP at FAT because the battery capacity increases and resistance decreases due to the rising temperature. Thus, the SOP at FRT will lead to higher peak power which exceeds the one withstood by the battery at lower temperatures, and the SOP at FAT will lead to lower peak power which cannot ensure effectively battery performance.

When compared to the HPPC method and the method based on SOC limits (MSL) at dynamic battery temperatures, the following Fig. 14 is obtained.

![Fig. 14 SOP estimation result at 0°C](image)

In Fig. 14, the SOP estimation curves with different methods after DST and the real SOP at temperature 0°C are shown respectively. As analyzed in Section 1, the SOP with HPPC and MSL method are high than the proposed methods (SOP at DBT). Especially, the results of MSL methods...
is much high than the Real SOP.

Analyzing the SOP estimation results at different temperature further in Fig. 15, it is found that the peak discharge currents are around 3.62C, 5.42C and 10.13C at temperature of -10°C, 0°C and 25°C respectively, which means that the LIB is unable to achieve a high discharging rate and cannot meet the demands of starting or acceleration of the electric vehicle at low temperature. Thus, heating equipment and thermal insulations must be added to the LIB pack to meet the driving demand at low temperatures.

![Fig.15 SOP estimation results at different ambient temperature](image)

The battery SOP, SOC and terminal voltage are compared at the discharge platform of the LIB and the end of discharge at 25°C in Fig. 14 and Fig. 15. The SOC intervals are 77.23%~85.41% and 5.12%~12.03% respectively.
Fig. 16 Comparison of SOC, terminal voltage and SOP of LIB at voltage platform

Fig. 17 Comparison of SOC, terminal voltage and SOP of LIB at the end of discharge

As shown in Fig. 16 and Fig. 17, the SOP changing trend is nearly the same with the terminal voltage at the discharge platform, and the impact of SOC to SOP is minor. Therefore, battery terminal voltage can reflect the peak power to certain extent. However, at the end of the discharge, the SOP decreases faster than the battery terminal voltage due to a rapid increase in battery resistance where the SOC is lower than 10%. So the battery will have to withstand a greater impulse current if only the terminal voltage is used as the control parameter, and this might damage the system security and battery life.
5 Conclusions

At low temperatures, key LIB characteristic parameters, such as battery capacity and resistance, change significantly when the ambient temperature is low. In this paper, a new SOP estimation method is developed, which includes the establishment of battery temperature, capacity and resistance based on experimental data, and also a combination of the AMPC method and the EKF technique to study the impact of temperature to SOP. The following conclusions can be obtained after analyzing the SOP estimation results:

1) The newly proposed SOP estimation algorithm performs better than the algorithm at fixed room temperature and the algorithm at fixed ambient temperature. And also the proposed method shows high accuracy when compared to the existing method at dynamic battery temperatures.

2) The SOP curve shows the same trend with the terminal voltage of the discharge platform, and decreases faster at the end of discharge. Thus, system security and battery life will be damaged if the terminal voltage at the end of discharge is used as the only control parameter.

3) The peak power of LIB decreases with the decreasing temperature. The peak current of the voltage platform is only 3.62C at the temperature of -10°C and cannot meet the demands of vehicle starting and acceleration. Thus, heating equipment and thermal insulations must be added to the LIB pack at low temperature.

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Reference


