

1 Monte Carlo investigation of the characteristics of 2 radioactive beams for heavy ion therapy

3 Andrew Chacon^{1,2,+}, Mitra Safavi-Naeini^{1,2,3,4,*,+}, David Bolst¹, Susanna Guatelli^{1,4}, Daniel
4 R. Franklin⁵, Yuma Iwao⁶, Hideaki Tashima⁶, Eiji Yoshida⁶, Fumihiko Nishikido⁶, Atsushi
5 Kitagawa⁶, Akram Mohammadi⁶, Taiga Yamaya⁶, Marie-Claude Gregoire^{1,2,3}, and Anatoly
6 B. Rosenfeld^{1,4}

7 ¹Centre for Medical Radiation Physics, University of Wollongong, Wollongong NSW 2522 Australia

8 ²Australian Nuclear Science and Technology Organisation (ANSTO), NSW, Australia

9 ³Brain and Mind Centre, University of Sydney, Sydney, NSW, Australia

10 ⁴Illawarra Health and Medical Research Institute, University of Wollongong, Wollongong NSW 2522 Australia

11 ⁵Faculty of Engineering and IT, University of Technology Sydney, Ultimo NSW 2007 Australia

12 ⁶National Institute of Radiological Sciences (NIRS), National Institutes for Quantum and Radiological Science and
13 Technology, 4-9-1 Anagawa, Inage-ku, Chiba 263-8555, Japan

14 *mitras@ansto.gov.au

15 +These authors contributed equally to this work

16 ABSTRACT

This work presents a simulation study evaluating relative biological effectiveness at 10% survival fraction (RBE_{10}) of several different positron-emitting radionuclides in heavy ion treatment systems, and comparing these to the RBE_{10} s of their non-radioactive counterparts. RBE_{10} is evaluated as a function of depth for three positron-emitting radioactive ion beams (^{10}C , ^{11}C and ^{15}O) and two stable ion beams (^{12}C and ^{16}O) using the modified microdosimetric kinetic model (MKM) in a heterogeneous skull phantom subject to a rectangular 50 mm×50 mm×60 mm spread out Bragg peak. We demonstrate that the RBE_{10} of the positron-emitting radioactive beams is almost identical to the corresponding stable isotopes. The potential improvement in PET quality assurance image quality which is obtained when using radioactive beams is evaluated by comparing the signal to background ratios of positron annihilations at different intra- and post-irradiation time points. Finally, the incidental dose to the patient resulting from the use of radioactive beams is also quantified and shown to be negligible.

18 1 Introduction

19 Heavy ion therapy (HIT) is a relatively new cancer treatment modality, with several facilities operating or
20 under construction around the world¹⁻³. A monoenergetic heavy ion beam deposits most of its energy
21 within a narrow depth range - known as the Bragg Peak - with the peak dose depth determined by the
22 beam energy, ion species and target composition^{4,5}. Irradiation of the entire target volume is achieved
23 using a range of particle energies, either via a passive scatterer or a raster-scanned spot beam with varying
24 energy. Due to the narrow depth range of the Bragg peak, together with minimal lateral scattering and the
25 high relative biological effectiveness (RBE) of heavy ions, HIT delivers a highly conformal therapeutic
26 dose to the target volume with a much lower entrance dose than is possible with photon therapy. HIT
27 achieves a lower entrance dose compared to proton therapy, although unlike proton therapy, some dose is
28 delivered beyond the distal edge of the target volume due to the fragmentation tail.

29 The precision of HIT makes it particularly useful for treating deeply-situated tumours while minimising
30 damage to adjacent healthy tissue^{4,6-8}. However, due to the large dose gradients, deviations between

31 the treatment plan and the delivered dose distribution can result in significant adverse effects on healthy
32 tissue, particularly if the treatment region is in the proximity of an organ at risk (OAR). Accurate real-time
33 measurement of spatial dose distribution during irradiation will provide a mechanism for closed-loop
34 control over the treatment process, minimising errors between the treatment plan and the actual delivered
35 dose.

36 During HIT, a fraction of the ions in the beam will undergo nuclear inelastic collisions. Fragmentation
37 of nuclei either from the primary beam or in the target and entrance path result in the production of a
38 range of stable and radioactive nuclei⁶. Some of these fragments are positron-emitting radionuclides,
39 which continue to travel a short distance in the target before coming to a stop, where they eventually decay.
40 Measuring of the distribution of these secondary positron-emitting fragments offers a unique opportunity
41 for noninvasive, real-time and/or offline quality assurance (QA) in heavy ion therapy via positron emission
42 tomography (PET)⁹⁻¹⁶.

43 A large number of annihilation photons must be detected in order to obtain a PET image of sufficient
44 quality for useful treatment QA. The cross-sections for inelastic ion collisions depend on several parameters,
45 including incident ion species and energy, and the density and composition of the target¹⁷. These factors
46 determine the mix of fragments produced, which, in turn, determines the number and distribution of
47 positron-emitting radionuclides resulting from each beam spill. To improve image quality, several authors
48 have proposed the use of positron-emitting radioactive nuclei (such as ¹¹C, ¹⁵O or ¹⁰C) as the primary
49 particle in the heavy ion beam. Most primary particles will survive intact to decay via positron emission at
50 their stopping point, corresponding to the location of the Bragg peak. Therefore, for radioactive beams,
51 the spatial distribution of the stopping points of primary particles is the dominant component of the PET
52 image, while positron-emitting target and beam fragments making up a secondary component.

53 Beamlines capable of producing beams of radioactive ion species such as ¹¹C, ¹⁰C and ¹⁵O with
54 sufficient dose rates and beam purity for therapeutic use are currently under development at the National
55 Institutes for Quantum and Radiological Science and Technology (NIRS, QST) in Japan and other facilities
56 around the world¹⁸⁻²³.

57 In order to perform proper treatment planning with positron-emitting radioactive beams, and to
58 understand how their use will impact image-based QA, it is necessary to address three key research
59 questions:

- 60 1. How does the relative biological effectiveness (RBE) of polyenergetic radioactive beams vary as a
61 function of depth within a spread out Bragg peak, and how does this compare to the corresponding
62 stable ion species?
- 63 2. What quantitative differences are expected between the maps of positron annihilation resulting from
64 treatment with stable and positron-emitting radioactive ion beams, and how will these impact the
65 use of PET images as an intra-treatment or post-treatment QA mechanism? and finally,
- 66 3. What additional dose will be received by the patient if a positron-emitting radioactive beam is used
67 instead of a stable beam?

68 In this work, simulations of a simple treatment plan (consisting of a flat biological dose in a rectangular-
69 prismatic primary treatment volume inside a human skull phantom) are performed for five primary nuclei
70 (three positron-emitting and two stable) using the Geant4 Monte Carlo toolkit. The values of RBE₁₀ (RBE
71 at 10% survival fraction) are estimated across a range of depths along the beam path (in the entrance,
72 SOBP and tail regions) using Kase's modified microdosimetric kinetic model (MKM)²⁴⁻²⁶. The validity of
73 using Monte Carlo simulations to evaluate RBE using the MKM has previously been established by Bolst

74 et al.^{27,28}; however, to our knowledge, this is the first time that this approach has been applied to estimate
75 the RBE₁₀ of a polyenergetic radioactive beam. The method can easily be extended to other homogeneous
76 or heterogeneous targets and heavy ion species, and is a convenient and cost-effective alternative to in
77 vitro experiments.

78 Monte Carlo simulation-based 2D maps of positron yield obtained in a skull phantom using a spread out
79 Bragg peak (with the same flat biological dose (in Gy(RBE)) delivered throughout the planned treatment
80 volume) are compared across all beam types. The distribution of positron production in the target volumes,
81 as measured during the beam-off periods during irradiation of the phantom with the radioactive and
82 corresponding stable heavy ion beams were measured, and the resulting signal to background ratios
83 (SBRs) estimated. The chosen physics models in the simulation are validated via experimental work
84 conducted at NIRS's HIMAC facility.

85 Finally, the additional dose to the patient resulting from the use of radioactive beams is estimated to
86 determine whether it poses any significant risk to the patient compared to the use of a stable ion beam.

87 The remainder of this paper is organised as follows. A summary of key related work, including a
88 description of the modified MKM which is adopted in this paper, is presented in Section 2. Details
89 of the Monte Carlo simulations, including the phantom, physical and biophysical models used and the
90 experimental validation of the selected physics models, the implementation of a pseudo-clinical beamline
91 and treatment plan for stable and their corresponding radioactive ion beams are discussed in Section 3.
92 Simulation results and analysis of the RBE₁₀ values of stable and radioactive beams, the resulting positron
93 yield maps and the incidental dose resulting from the use of the radioactive beams are presented and
94 discussed in Section 4. Conclusions and proposed future work are presented in Section 5.

95 **2 Related Work**

96 The use of positron-emitting radioisotopes for heavy ion therapy has been investigated by a number of
97 authors. In 2001, Urakabe et al. demonstrated that a positron-emitting ¹¹C scanned spot beam could be
98 directly used as the therapeutic agent²⁹. However, the estimate of RBE₁₀ used to obtain a flat biological
99 dose was based on an extrapolation of previously-reported results for ¹²C in water, which was assumed
100 to extend to human tissue³⁰. Iseki et al. at NIRS used low-intensity monoenergetic ¹⁰C probe beams
101 with between 10⁴ and 10⁵ particles per spill to estimate the depth of the therapeutic ¹²C beam's Bragg
102 peak, while keeping the dose received during the range measurement under 100 mGyE (a few percent of
103 therapeutic dose)³¹. RBE of the radioactive beam was estimated via simulation using the one-dimensional
104 HIBRAC beam transportation code from Sihver et al. combined with Kanai's RBE model^{30,32,33}. However,
105 this work only considered monoenergetic ¹¹C ion beams, and ignored the effects of low-LET fragmentation
106 products, which resulted in an overestimation of the RBE for ¹¹C. Augusto et al. used the FLUKA Monte
107 Carlo toolkit to investigate the use of ¹¹C beams either alone or in conjunction with ¹²C³⁴. It was found
108 that for beams with equivalent energy per nucleon incident on the same water phantom, ¹¹C and ¹²C
109 beams produce very similar fragmentation products, with the main differences being the relative yield of
110 helium ions and several boron isotopes. While this study demonstrated the potential of using ¹¹C in heavy
111 ion therapy, it only considered monoenergetic beams of ¹¹C at a fixed depth (100 mm) in a homogeneous
112 water phantom. The composition of the phantom, the isotope and the specific beam energy are important
113 factors affecting the fragmentation process and the spatial distribution of positron-emitting nuclei which
114 results^{35,36}.

115 These works demonstrate the potential for using positron-emitting beams both for radiotherapy and
116 for range verification. However, in order to conclusively establish their clinical utility, it is necessary to
117 quantify their RBE and evaluate the quality of the resulting PET image in a clinically relevant configuration,

118 through the use of heterogenous tissue-equivalent phantoms and polyenergetic ion beams.

119 Relative biological effectiveness (RBE) is an empirically-derived ratio which can be used to predict
 120 the physical dose of a specific type of radiation which will result in the same cellular survival fraction as a
 121 reference dose (typically a 200 keV X-ray beam)^{37,38}. The complex dependencies of RBE on the energy
 122 and type of radiation, as well the location of the target and the specific tissue types present, require the
 123 use of biophysical methods for accurate theoretical estimation of RBE³⁹⁻⁴¹. The Microdosimetric Kinetic
 124 Model (MKM), proposed by Hawkins et al., is a widely-used method for estimating RBE in which the
 125 microdosimetric spectrum ($f(y)$) is measured through the use of a tissue-equivalent proportional counter
 126 (TEPC)²⁴. It was subsequently extended by Kase et al. to relate the saturation-corrected dose-mean lineal
 127 energy (\bar{y}^*) to the radiation sensitivity coefficient α of the linear quadratic model (LQM, measured in units
 128 of Gy^{-1} and Gy^{-2}), such that the method can be applied to therapeutic heavy ion beams^{25,26,42}. This
 129 *modified MKM* has been extensively validated for carbon ion therapy, and also extended to proton and
 130 helium ion therapy^{25,26,42-44}.

131 The RBE_{10} for an ion beam, defined as the ratio of the physical dose from a 200 kVp X-ray beam
 132 required to achieve a cellular survival fraction of 10% ($D_{(10,R)}$) to the ion beam dose resulting in the same
 133 cell survival fraction, can be derived using the microdosimetric spectra $f(y)$, using (1), (2) and (3):

$$y^* = y_0^2 \frac{\int \left(1 - e^{-\left(\frac{y}{y_0}\right)^2}\right) f(y) dy}{\int y f(y) dy} \quad (1)$$

$$\alpha = \alpha_0 + \frac{\beta_0}{\rho \pi r_d^2} y^* \quad (2)$$

$$\text{RBE}_{10} = \frac{2\beta D_{10,X-ray}}{\sqrt{\alpha^2 - 4\beta \log(0.1)} - \alpha} \quad (3)$$

134 For human salivary gland (HSG) tumour cells, the dose resulting in a survival fraction of 10%, $D_{(10,R)}$
 135 is 5 Gy for 200 kVp X-rays; the LQM radiation sensitivity coefficient values are $\alpha_0 = 0.13 \text{ Gy}^{-1}$ and
 136 $\beta_0 = 0.05 \text{ Gy}^{-2}$. ρ and r_d are the density and the radius of the sub-cellular domain, and assumed to be
 137 $0.42 \mu\text{m}$ and 1 g/cm^3 , respectively²⁵.

138 In this work, RBE_{10} is estimated using an extension to the modified MKM proposed by Bolst et
 139 al., whereby the mean path length $\langle l_{path} \rangle$ of the charged particles that cross the sensitive volume
 140 is introduced to account for the directionality of the radiation field when deriving the microdosimetric
 141 spectra $f(y)$ in a non-spherical sensitive volume, as opposed to the average chord length used in isotropic
 142 fields^{27,28}.

143 Although estimates of the RBE_{10} for radioactive beams have been reported previously, these have
 144 been calculated using simplified analytic models with parameters interpolated/extrapolated from limited
 145 experimental data from beams of stable isotopes in homogeneous targets^{45,46}. The assumption that
 146 the RBE of radioactive ion species can be estimated from its stable analog has not been previously
 147 demonstrated in the literature.

Interaction	Energy Range	Geant4 Model/Package
Radioactive Decay	All energies	G4RadioactiveDecayPhysics
Particle Decay	All energies	G4Decay
Hadron Elastic	All energies	G4HadronElasticPhysicsHP
Ion Inelastic	0–110 MeV > 100 MeV	Binary Light Ion Cascade QMDModel
Neutron Capture	0–20 MeV	NeutronHPCapture
Neutron Inelastic	0–20 MeV >20 MeV	NeutronHPInelastic Binary Cascade
Proton Inelastic	0–9.9 GeV	Binary Cascade
EM Interactions	All energies	G4EmStandardPhysics_option3

Table 1. Hadron physics models used in all simulations

3 Method

All Monte Carlo simulations were performed using the Geant4 toolkit (version 10.2.p03)^{47,48}. The hadronic physics models used in the simulations are listed in Table 1, while electromagnetic interactions were modelled using the standard Geant4 option 3 physics constructor (G4EmStandardPhysics_option3). The hadronic physics processes and models are listed in Table 1.

Section 3.1 details the methods used to experimentally validate the Geant4 simulation. The phantoms used in the simulations are described in detail in Section 3.2. In Sections 3.3, 3.4 and 3.5, the implementation of the modified MKM for the evaluation of the RBE₁₀ of pseudo-clinical, polyenergetic carbon and oxygen beams and their corresponding radioactive beams is described. Lastly, Section 3.6 describes a simulation study which examines the yield of different positron-emitting radionuclides during and after the irradiation of a skull phantom with radioactive and corresponding stable beams and introduces the metric used for the evaluation of the quality of the resulting annihilation maps.

3.1 Experimental Validation of the Physics Models

To validate the Monte Carlo physics models, several simulations evaluating depth-dose profiles and positron-emitting radionuclide yield were performed and compared with measurements obtained from equivalent physical experiments.

All experiments were performed at the Heavy Ion Medical Accelerator in Chiba (HIMAC), Japan, with the stable ion beams produced at the primary beam course, and the radioactive ion beams at the secondary beam course^{19,23}. The peak energies of the non-radioactive ¹²C and ¹⁶O ion beams, as measured at the beamline nozzle, were 290 MeV/u and 400 MeV/u, respectively with an energy spread of $\sigma = 0.2\%$. The peak energies of the radioactive ¹¹C and ¹⁵O ion beams were 330 MeV/u and 290 MeV/u, respectively, each with an energy spread of $\sigma = 5\%$. The nominal transverse diameter of all beams was 2 mm full width at half maximum (FWHM).

3.1.1 Depth-Dose Relationship

The experimental configuration shown in Figure 1 was used to compare the experimental and simulation-based depth-dose curves. The deposited energy was measured using a pre-calibrated cross ionisation

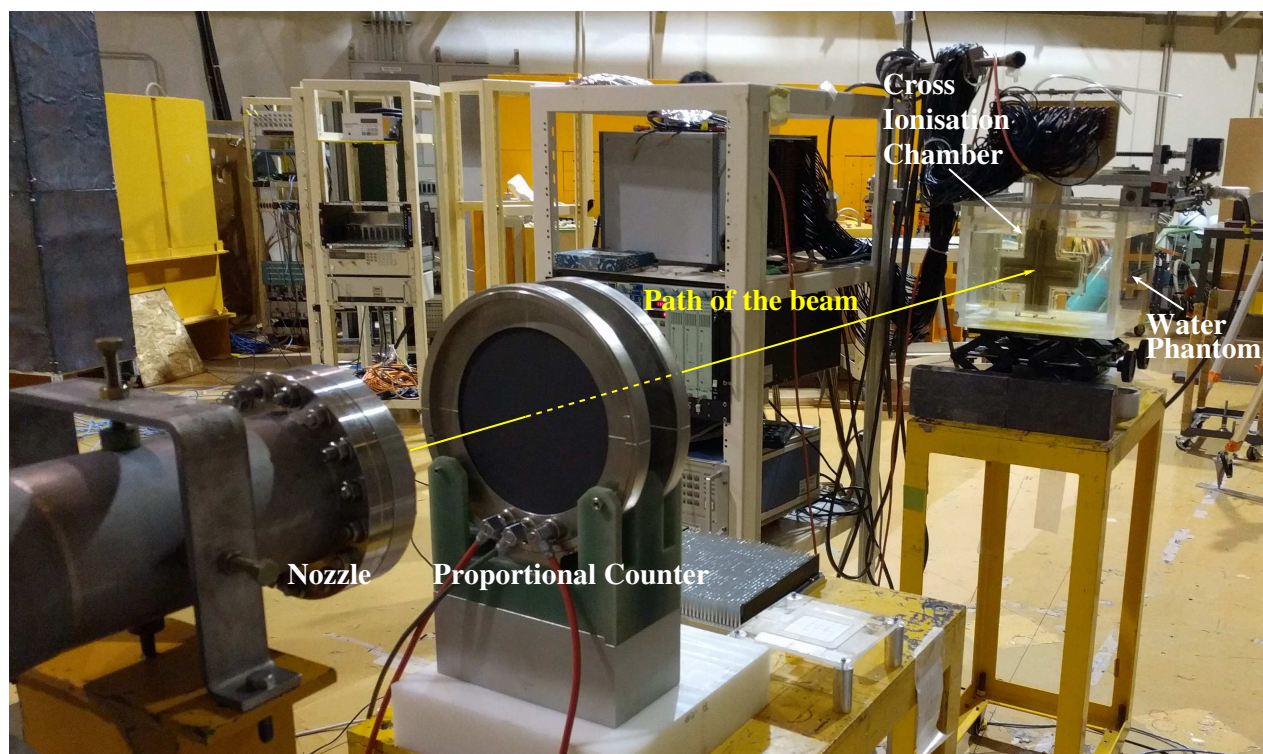


Figure 1. The experimental configuration used to estimate the depth-dose profile of the stable ion beams in water, at the primary beam course (HIMAC, Japan); the radioactive beams were produced at the secondary beam course (not shown in this image).

174 chamber (IC) with a sensitive volume of 36 mm^3 , inside a $300 \times 300 \times 300 \text{ mm}^3$ water phantom²³. The IC
 175 was encased within a 0.5 mm PMMA casing and moved along the path of the beam using a motorised
 176 stage, with an accuracy of $10 \mu\text{m}$. The energy deposited within the ionisation chamber at each point along
 177 the beam was normalised to the energy deposited at the entrance (i.e. at the front of the phantom). All
 178 depth measurements were converted to water equivalent depth.

179 For the simulation study, each beam was modelled using a monoenergetic incident beam with a
 180 Gaussian energy distribution, with the same peak energies and spreads as for the HIMAC beamlines. The
 181 simulated beams entered the water phantom perpendicular to its front surface (see Table 2), with an air
 182 gap of 2.5 m between the beamline nozzle and the phantom surface as per the corresponding experimental
 183 configuration. The energy deposited was scored in the water phantom using 1 mm^3 voxels and summed
 184 over a 36 mm^3 volume equivalent to the sensitive volume of the ionisation chamber used throughout
 185 the experimental measurements. Energy deposited in the sensitive volume (as a function of depth) was
 186 normalised to value observed at the entrance plateau.

187 **3.1.2 Positron-Emitting Fragmentation Product Yield**

188 The hadronic physics models of Geant4, including the Quantum Molecular Dynamics (QMD) ion hadronic
 189 inelastic scattering and Radioactive Decay physics models, were validated by comparing the simulated and
 190 experimentally estimated yields of ^{11}C , ^{10}C and ^{15}O , the three dominant positron-emitting radionuclides
 191 generated during irradiation of a $100 \times 100 \times 300 \text{ mm}^3$ PMMA phantom by monoenergetic ^{12}C and ^{16}O
 192 beams with energies of 290 MeV/u and 400 MeV/u, respectively.

193 The experimental configuration is shown in Figure 2. The phantom was positioned such that the
 194 expected location of the Bragg peak was aligned with the centre of the field of view in the OpenPET

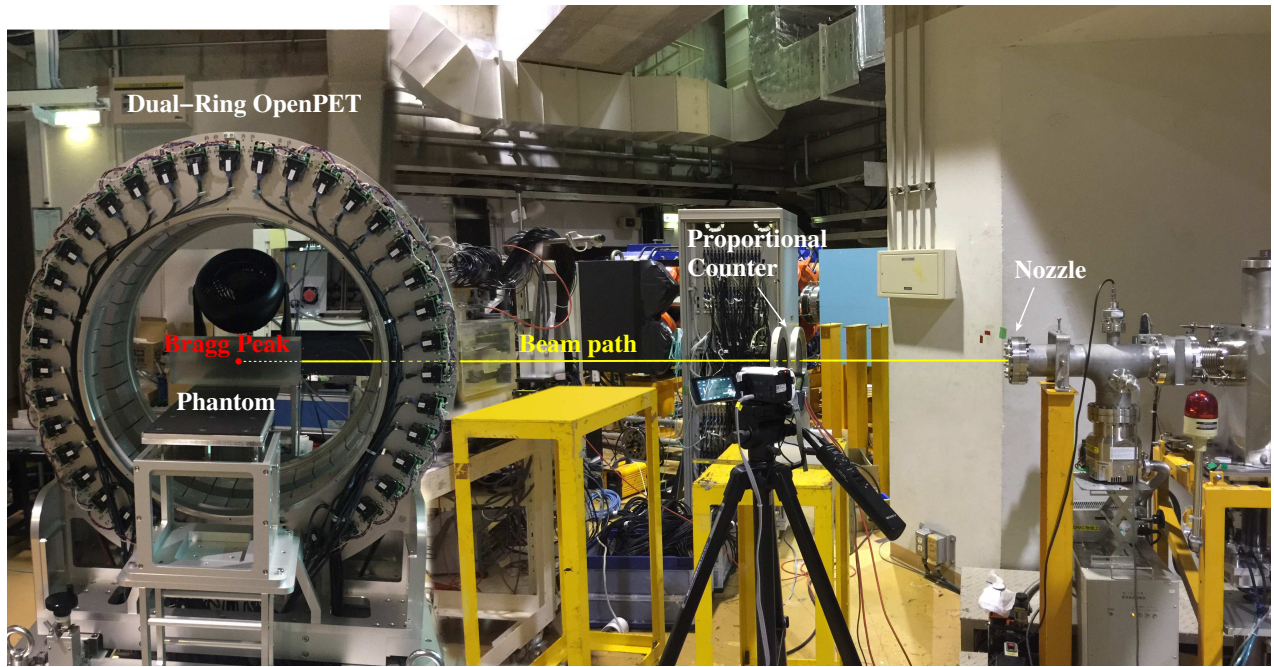


Figure 2. The experimental configuration used in HIMAC, Japan, to validate the QMD ion hadronic inelastic scattering model used in the simulations. The phantom is positioned within the field of view (FOV) such that the calculated location of the Bragg peak (indicated by a red dot) is placed at the centre of the field of view (CFOV).

scanner¹⁴. 20 spills were used, with a beam intensity of 1.0×10^9 particles per second (pps). In each spill, the beam was on for 1.9 seconds and off for 1.4 seconds. List-mode PET data were collected intra-spill, and for 36 minutes after the final spill. Dynamic (4D) images were reconstructed using the 3D ordinary Poisson ordered-subset-expectation-maximisation algorithm (3D-OP-OSEM) with $1.5 \times 1.5 \times 1.5$ mm³ voxels. Temporal frame lengths were chosen so as to be able to observe decay over several half-lives of ¹¹C, ¹⁰C and ¹⁵O. Yields of each positron-emitting radionuclide were estimated by fitting the parameters of a simple analytical model to the observed time-activity curves (TACs). Total activity as a function of time t in a volume with initial activities of ¹¹C, ¹⁰C and ¹⁵O of $A_{0,C11}$, $A_{0,C10}$ and $A_{0,O15}$, respectively, is given by

$$A_{total}(t) = A_{0,C11}e^{-\ln(2)t/T_{C11}} + A_{0,C10}e^{-\ln(2)t/T_{C10}} + A_{0,O15}e^{-\ln(2)t/T_{O15}} \quad (4)$$

where T_{C11} , T_{C10} and T_{O15} are the respective half-lives of ¹¹C, ¹⁰C and ¹⁵O. Total activity is measured as a function of time across the build-up and Bragg peak region, defined as the region from the point at which the dose profile has risen 5% above the entrance plateau to the point after which the profile is below 5% of the peak value.

The individual initial activities for each radionuclide are then estimated for both the simulation results and the experimental data by fitting the model to the observed curve.

For the simulation studies, monoenergetic ¹²C and ¹⁶O beams were directed perpendicularly to the surface of a simulated $10 \times 10 \times 30$ cm³ PMMA with an air gap of 1.75 m between the beamline nozzle and the phantom surface, matching the experimental configuration. Density, mean excitation, ionisation potential and dimensions of simulated phantoms were chosen to match those used in the experiment.

Phantom Name	Phantom material	Dimensions
PMMA phantom	PMMA	100×100×300 mm ³
Water phantom	Water	250×250×250 mm ³
Skull phantom	Bone	250×250×10 mm ³
	Brain Tissue (modelled as muscle)	250×250×240 mm ³

Table 2. Phantom compositions

214 The spatio-temporal distributions of positron-emitting nuclei, positron production and annihilation were
 215 recorded with a scoring volume resolution of 1.5 mm, corresponding to the voxel dimensions in the
 216 experimental PET images. Simulated yield profiles were convolved with a Gaussian filter, with its FWHM
 217 equal to the estimated OpenPET spatial resolution (3.5 mm)¹⁴.

218 3.2 Phantom Geometry

219 The phantoms used in the simulation were rectangular prisms with compositions as listed in Table 2. All
 220 material compositions were based on data from the National Institute of Standards and Technology (NIST)
 221 database⁴⁹.

222 3.3 Estimation of RBE₁₀ for a pseudo-clinical SOBP

223 To evaluate and compare the RBE₁₀ of polyenergetic stable and positron-emitting radioactive beams,
 224 sensitive 1 mm×1 mm×10 μm volumes were defined every 100 μm along the path of the beam. The lineal
 225 energy deposition spectrum in each volume for all interactions ($f(y)$) was stored and used to calculate the
 226 RBE₁₀ at that point, using (3) (equivalent results for monoenergetic carbon and oxygen ion beams with the
 227 energies listed in Supplementary Table S1 are presented in Supplementary Table S2). A correction factor
 228 1.05 were used to account for the difference in stopping power and density of water relative to brain tissue.

229 A simple variance analysis method was used to estimate a sufficient number of primary particles to use
 230 in the simulations. M test simulations were conducted, each with N primary particles, with RBE estimated
 231 for each simulation and the mean and standard deviation (SD) calculated across the M simulations. The
 232 standard deviation should approach zero as N tends to infinity; therefore, in this experiment, N was
 233 progressively doubled with a fixed value of $M = 50$ until the ratio of standard deviation to mean was less
 234 than an arbitrary threshold of 1%. This analysis suggested that $N = 10^7$ would be sufficient to get a good
 235 estimate of RBE (95% probability of the estimated RBE being within ±2% of the true RBE).

236 3.4 Carbon

237 The spectrum for the simulated carbon beams was generated using an experimentally-validated model
 238 of the passively-scattered ¹²C beamline at HIMAC, which is known to produce a flat biological dose
 239 across a 60 mm depth range⁵⁰. The spectra of the positron-emitting radioactive beams (¹⁰C and ¹¹C) were
 240 based on the ¹²C spectrum from this beamline, by determining the energies for which the Bragg peaks of
 241 monoenergetic radioactive ion beams were located at the proximal and distal edges of the desired SOBP,
 242 and linearly mapping the weights of the energies of the ¹²C SOBP spectrum to this range of energies.
 243 Finally, the SOBPs were compared and confirmed to both correspond to the planned depths.

244 3.5 Oxygen

245 Currently a validated model of the ¹⁶O beamline does not exist. Therefore, generation of the 60 mm flat
 246 biological dose SOBP in the target depth range was achieved by performing monoenergetic Monte Carlo

247 simulations of an ^{16}O beam at a range of energies (177, 237, 297, 345 and 418 MeV/u), and evaluating the
248 RBE_{10} as a function of depth for each energy using the modified MKM (see Section 3.3 and Supplementary
249 Table S2). This RBE was used to convert the physical dose deposited in the simulations to an estimated
250 biological dose for the 5 evaluated energies. Profiles were then generated for other intermediate energies
251 by interpolating between the simulated values in increments of 1 MeV/u. Finally, the target flat biological
252 dose was achieved by adjusting the weights of each of these profiles such that a flat biological dose rate
253 of 5 Gy(RBE)/min was achieved within the target depth range. The spectra of the positron-emitting
254 radioactive beam (^{15}O) was based on the ^{16}O spectrum, with energies scaled such that the SOBP was
255 positioned in the desired depth range (as per carbon).

256 3.6 Positron-Emitting Radionuclide Yield Study

257 The impact of using positron-emitting primary beams on interspill and post-irradiation image quality
258 was evaluated by comparing the spatial distributions of positron decays observed in the simulation over
259 several different intervals during treatment of the skull phantom. A simple treatment plan was designed
260 for each primary particle type, aimed at producing a constant biological dose rate of ≈ 5 Gy(RBE)/min in
261 a depth range of 78-138 mm within a skull phantom. A total of 1×10^9 primary particles were used in
262 each simulation. As for the experimental validation study, twenty spills were simulated, with the beam on
263 for 1.9 seconds and off for 1.4 seconds.

264 The distributions of positron decays were acquired for each beam type between the first and second
265 spill, during the first five inter-spill intervals, and in the five minutes following the final spill.

266 The contrast-to-noise ratios (CNRs) between the inside and outside of the proximal, distal and upper
267 lateral edges of the SOBP are computed for each image. The CNR provides a metric for objectively
268 comparing the specificity with which the irradiated region is delineated, and is defined as:

$$\text{CNR} = \frac{|\mu_a - \mu_b|}{\sqrt{(\sigma_a^2 + \sigma_b^2)}} \quad (5)$$

269 where μ_a and μ_b are the mean signal amplitudes and σ_a and σ_b are the standard deviations of the
270 image intensity in two regions a and b of the image^{51,52}.

271 3.7 Data Availability

272 All data generated or analysed during this study are included in this published article (and its Supplementary
273 Information files) or are available from the corresponding author on reasonable request.

274 4 Results and Discussion

275 4.1 Physics Model Validation

276 Experimental and simulation-based depth-dose curves are shown in Figure 3; the difference between the
277 locations of the Bragg peaks obtained from the simulated and the experimental ^{12}C , ^{16}O , ^{11}C and ^{15}O
278 depth-dose profiles were 0.8 mm, 0.24 mm, 0.37 mm and 0.43 mm, respectively.

279 The experimental and simulation yields of ^{10}C , ^{11}C , and ^{15}O produced during the irradiation of a
280 PMMA phantom using a 290 MeV/u ^{12}C beam and a 400 MeV/u ^{16}O beam are expressed as a percentage
281 of the total positron-emitting radionuclide yield and are listed in Table 3.

282 The close agreement between the experimental and simulated normalised depth-dose profiles and the
283 relative yield estimations of the positron-emitting fragments demonstrate the validity of the simulation

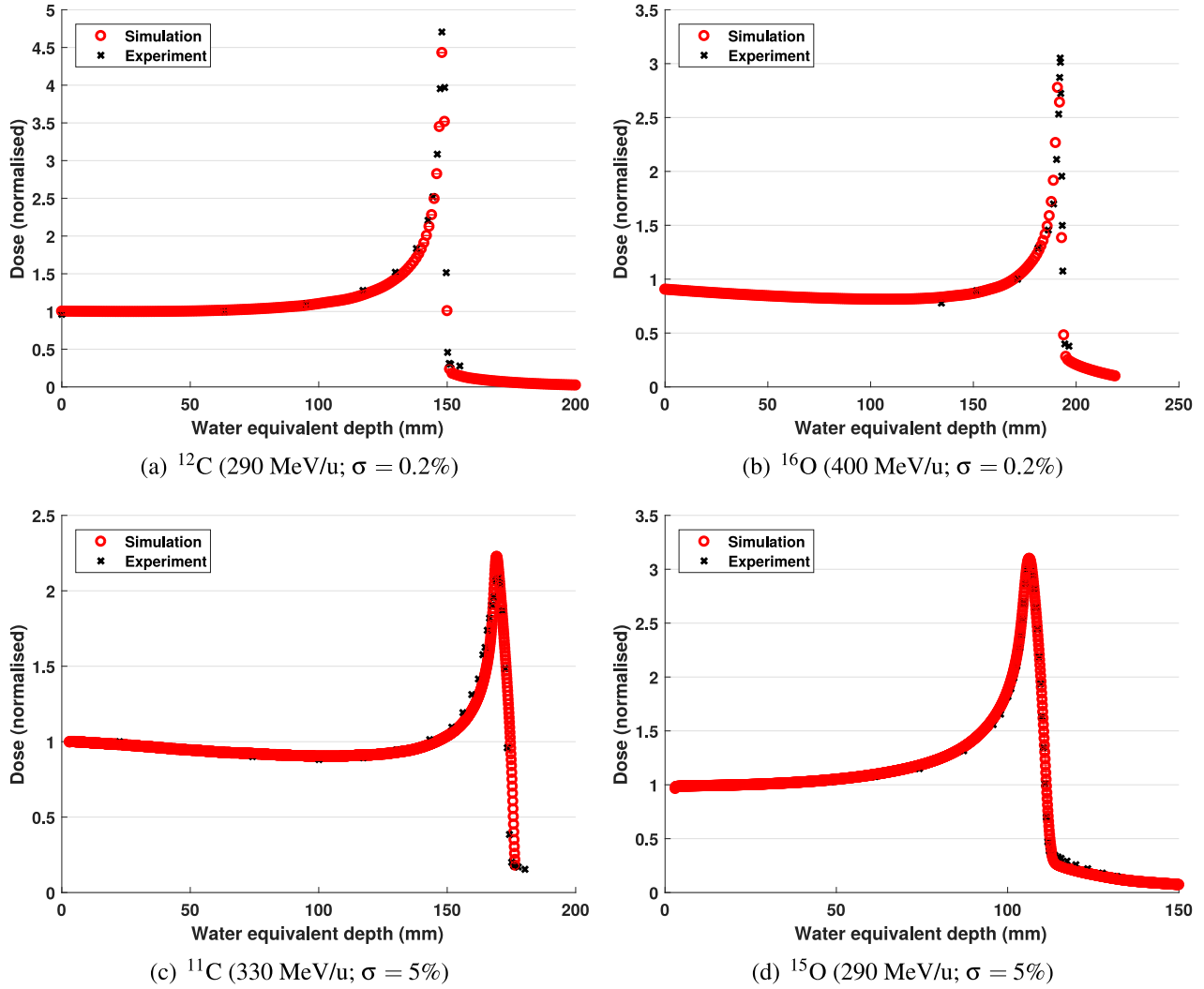


Figure 3. Experimental and simulated energy deposited in the sensitive volume plotted as a function of depth for the ^{12}C , ^{16}O , ^{11}C and ^{15}O ion beams. The deposited energy is normalised to value observed at the entrance plateau.

Table 3. Relative yields of positron-emitting nuclei in experiment and simulation

Primary beam	Energy (MeV/u)	Isotope	Relative Yield (%)	
			Simulation	Experimental
^{12}C	290	^{11}C	80 ± 8	82 ± 9
		^{10}C	5 ± 3	4 ± 2
		^{15}O	15 ± 6	14 ± 8
^{16}O	400	^{11}C	44 ± 10	43 ± 10
		^{10}C	7 ± 7	7 ± 5
		^{15}O	49 ± 14	50 ± 10

Table 4. Means and standard deviations of the RBE₁₀ for each beam evaluated at five depths (entrance, start, middle and end of SOBP, and tail). At each depth, RBE₁₀ is evaluated in 11 adjacent sensitive volumes (every 100 μm along the path of the beam) and the mean and standard deviation calculated.

Region	Depth (mm)	¹² C RBE ₁₀		¹¹ C RBE ₁₀		¹⁰ C RBE ₁₀		¹⁶ O RBE ₁₀		¹⁵ O RBE ₁₀	
		μ	σ	μ	σ	μ	σ	μ	σ	μ	σ
Entrance	50	1.32	0.0577	1.31	0.0646	1.30	0.0511	1.51	0.0455	1.50	0.0469
Start of SOBP	81	1.61	0.184	1.61	0.182	1.56	0.148	1.84	0.137	1.84	0.173
Middle of SOBP	111	1.80	0.202	1.79	0.199	1.76	0.235	2.05	0.163	2.05	0.190
End of SOBP	131	2.21	0.251	2.23	0.258	2.20	0.256	2.59	0.215	2.46	0.187
Tail	171	1.15	0.396	1.12	0.317	1.12	0.365	1.28	0.501	1.27	0.407

284 model. The small differences between the experimental and simulated depth dose profiles for radioactive
 285 primary particles may be due to an underestimation of the initial energy spread, heterogeneity of the
 286 beryllium target leading to contamination with other fragments and systematic errors introduced by the
 287 ionisation chamber measurements.

288 4.2 RBE and Biological Dose in Gy(RBE)

289 Figure 4 presents a comparison of RBE₁₀ as a function of depth for the positron-emitting radioactive
 290 beams and for the corresponding stable isotope beams (for clarity, RBE₁₀ values are shown at depth
 291 increments of 3 mm; refer to Supplementary Spreadsheet 1 for a full list of RBE₁₀ values evaluated at
 292 100 μm intervals for all ion species). In each case, the mean RBE₁₀s of the stable and radioactive beams
 293 are well within each others' 95% confidence interval. Radioactive-to-stable RBE₁₀ ratios are also shown,
 294 with the mean values remaining very close to 1.0 in the entrance and SOBP. The larger confidence intervals
 295 in the tail region are due to very little energy being deposited beyond the end of the SOBP (as expected for
 296 heavy ion beams), resulting in significant statistical noise.

297 Table 4 lists numerical values of the RBE₁₀ obtained at the entrance, the beginning, middle and end of
 298 the SOBP, and tail region for each beam type. The mean and standard deviations presented are calculated
 299 over 11 consecutive 100 μm deep sample volumes along the beam path centred about the listed depth. In
 300 all cases, the mean RBE₁₀s for the radioactive and corresponding stable ion beams are within one standard
 301 deviation of each other.

302 The significance of this result is that it indicates that the evaluated radioactive ion beams are comparable
 303 to their non-radioactive counterparts in terms of relative biological effectiveness. Heavy ion therapy with
 304 any of the radioactive ion species examined in this study should be feasible, with only minimal changes to
 305 the current treatment planning algorithms required to account for the small differences in RBE₁₀.

306 4.3 Positron Yield

307 Figure 5 shows the 2D annihilation maps obtained during and after the simulated delivery of 5 Gy(RBE)
 308 for each beam type to the target volume within the skull phantom. Images in the first column correspond
 309 to data acquired during the first beam-off interval (i.e. after one spill), the centre column show images
 310 following 5 spills, and finally, the last column shows images acquired during the five minutes (300 seconds)
 311 immediately after the completion of the 20th (and final) spill.

312 The CNRs of the inside and outside of the proximal, distal and upper lateral boundaries of the SOBP
 313 images in Figure 5 are listed in Table 5.

314 Positron annihilation maps acquired at different stages of the treatment process clearly demonstrate
 315 the potential improvements in range-verification QA that can be obtained with radioactive ion beams.
 316 Following a single spill, the boundaries of the SOBP are very clearly visible in the cases of ¹⁰C and ¹⁵O

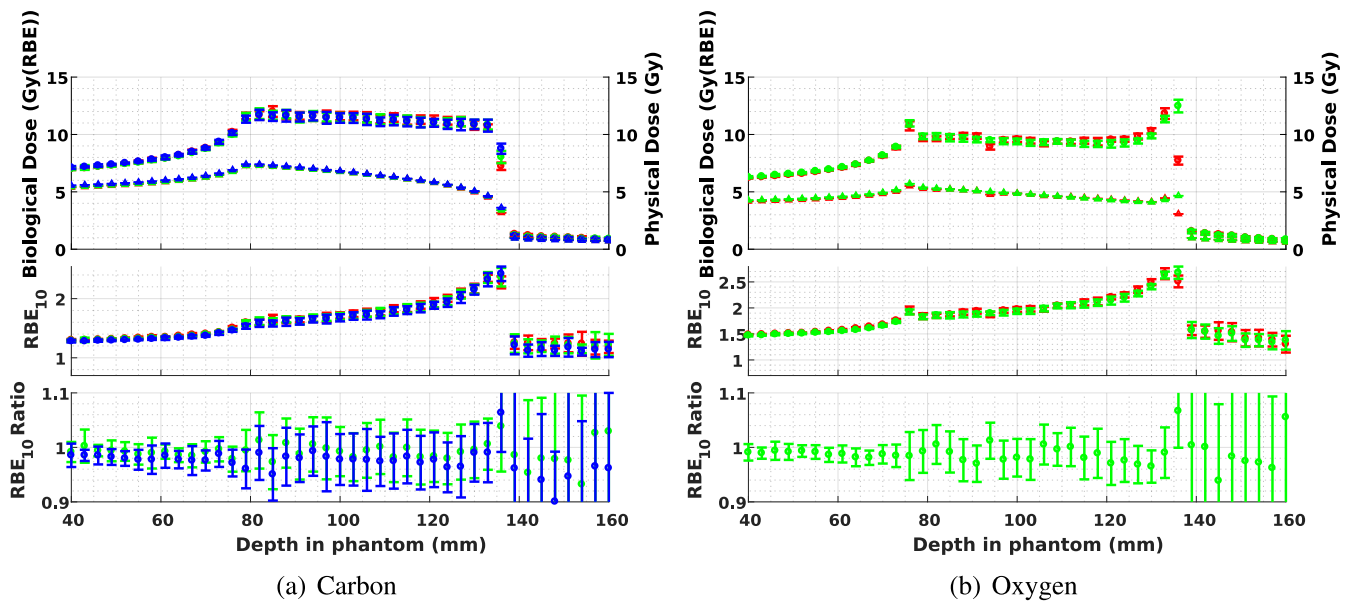


Figure 4. Biological dose, physical dose and RBE_{10} for positron-emitting radioactive beams, together with the ratio of radioactive-beam RBE_{10} to stable-beam RBE_{10} , each shown as a function of depth within the phantom. The objective is a uniform dose within a 60 mm SOBP, from 78 to 138 mm depth. For carbon, ^{12}C is shown in red, with ^{11}C and the ratio of $^{11}\text{C}:^{12}\text{C}$ shown in green, and ^{10}C and the ratio of $^{10}\text{C}:^{12}\text{C}$ shown in blue. ^{16}O is shown in red, while both ^{15}O and the ratio of $^{15}\text{O}:^{16}\text{O}$ is shown in green. All confidence intervals are 95% (two standard deviations).

317 (Figure 5 (a) and (j)), due to their short half-lives (19.29 seconds and 122.24 seconds, respectively). The
 318 images from the ^{10}C simulation also exhibit the the highest CNR values for all boundaries after both 1
 319 and 5 spills (i.e. the delivery of 5% and 25% of the total planned dose) and 5 minutes after the delivery
 320 of the full treatment for the distal boundary. ^{15}O also exhibits an excellent CNR following a 5 minute
 321 acquisition, demonstrating the best results for proximal and distal edge. The two stable beams produce
 322 images which are indistinct in comparison to any of the radioactive beam images. Due to its half life of
 323 20.334 minutes, only a small number of positron annihilations resulting from decays of ^{11}C are observed
 324 within the first beam-off period (Figure 5 (d)). The distal edge can be clearly seen, however the proximal
 325 edge is indistinct. Finally, in the long post-irradiation image acquisition (right column in Figure 5), most
 326 primaries from the ^{10}C and ^{15}O beams have decayed, resulting in very similar high-contrast images. A
 327 substantial number of primaries have now decayed in the case of ^{11}C , resulting in the emergence of a
 328 well-defined edges to the SOBP; it is expected that a ^{11}C beam with a post-irradiation image acquisition of
 329 20 minute or more will result in very high CNRs due to its longer half-life. By contrast, after a 5 minute
 330 acquisition, the distal and proximal edges of the SOBP remain indistinct in the case of ^{12}C . ^{16}O exhibits a
 331 more well-defined distal edge to its SOBP compared to ^{12}C , however, the proximal edge is again poorly
 332 defined.

333 The images also demonstrate one of the key differences between the radioactive and stable beams.
 334 For radioactive beams, positron annihilations principally occur in the vicinity of the stopping point of the
 335 primary particle. The intensity of the decay radiation observed in a PET image is therefore proportional to
 336 the number of primary particles which have arrived at that particular depth. The energy weightings required
 337 to achieve a flat biological dose have a bias towards higher energies (since more deeply-penetrating high-
 338 energy particles also deposit an entrance dose which is added to the dose deposited by lower energy

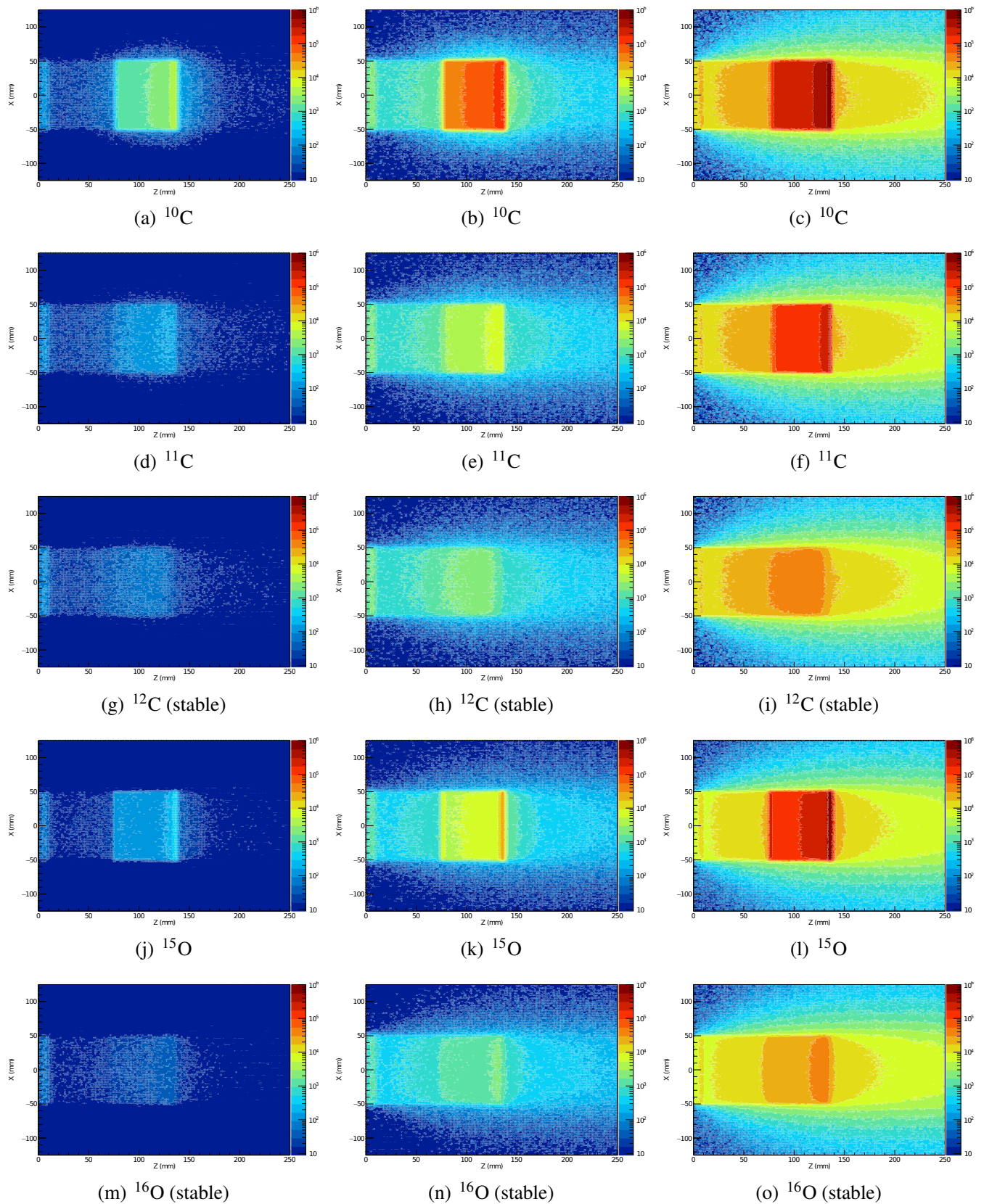


Figure 5. 2D positron annihilation maps resulting from 5 Gy(RBE) irradiation of the skull phantom, during and after irradiation: after 1 of 20 beam spills (5% of the planned dose - first column), 5 of 20 beam spills (25% of the planned dose - centre column) and 5 minutes post full-treatment (right column); Signal to background ratio (SBR) is quoted under each image.

Table 5. Contrast-to-noise ratios (CNRs) corresponding to Figure 5; the highest CNR value in each column is highlighted in bold.

	Proximal Edge			Lateral Edge			Distal Edge		
	1 spill	5 spills	5 min	1 spill	5 spills	5 min	1 spill	5 spills	5 min
¹⁰ C	156.47	332.99	122.36	120.26	286.72	190.95	125.38	338.18	335.90
¹¹ C	9.7344	19.567	57.338	17.731	39.356	108.26	15.415	39.075	202.55
¹² C	4.5779	8.2736	12.979	11.034	19.265	21.380	2.9674	4.6759	6.8661
¹⁵ O	28.398	79.051	201.99	72.384	133.94	216.50	53.606	85.169	233.24
¹⁶ O	3.7561	8.7385	15.572	14.183	23.685	26.484	5.6323	9.5223	14.268

beams). Therefore, the distal edge of the SOBP can be expected to be much brighter than the proximal edge, as is clearly evident in the images from the radioactive beams. By contrast, the contribution of primary or target fragmentation, which is relatively minor for the radioactive beams, is the *only* source of positrons in the case of the stable beams, and positron-emitting fragmentation products are produced to a varying extent along the entire length of the beam path (see Supplementary Tables S3 and S4). Therefore, the stable beams exhibit a flatter (although not completely flat) activity distribution in the SOBP, and weaker contrast between the SOBP and the entrance region.

4.4 Radiation dose to patients

Given the superiority of positron-emitting radioactive beams for intra- and post-treatment QA imaging, it is also important to consider whether or not the use of such beams would have any unintended side effects for the patient. From this perspective, the main difference for the patient is that an additional radiation dose will result from the use of a radioactive beam. The dose resulting from the decay of a positron-emitting radionuclide includes the kinetic energy of the positrons together with the 511 keV gamma photons resulting from their eventual annihilation; for a ¹¹C beam, a 70 Gy(RBE) dose delivered to a 100 mm cubic treatment volume would require approximately 2.3×10^{11} particles, distributed throughout the treatment volume. This corresponds to an initial activity concentration of 1.3 MBq/cc, which is comparable to tissue concentrations of radiotracer which would be used in diagnostic ¹¹C clinical PET imaging, and would deliver a biological dose⁴ within the treatment volume of the order of 3-10 mSv. The additional dose rapidly falls off outside the treatment volume, and would be insignificant compared to the dose due to lateral scattering of particles.

5 Conclusion

This work aimed to quantitatively evaluate the therapeutic potential of positron-emitting radioactive heavy ion beams; in particular, with regard to the relative biological effectiveness of the beams compared to their non-radioactive counterparts, the spatial distribution of the positron-emitting annihilations generated during and after irradiation of the target, and the incidental dose to the patient. Monte Carlo simulations of heavy ion therapy using a pseudo-clinical spread out Bragg peak constructed with positron-emitting radioactive beams of ¹¹C, ¹⁰C and ¹⁵O as well as stable ¹²C and ¹⁶O were undertaken with the Geant4 toolkit.

The simulation physics model was validated through a comparison of depth-dose curves for monoenergetic ¹¹C, ¹²C, ¹⁵O and ¹⁶O beams and relative yield estimations of the positron-emitting fragments produced within the build-up and the Bragg peak region with experimental data for ¹²C and ¹⁶O obtained

370 from the HIMAC facility in Japan. The maximum difference between the location of maximum dose in
371 the simulation and experimental data was 0.8 mm, while the maximum difference in mean relative yields
372 of the secondary positron-emitting fragments was 2%.

373 The radiobiological effectiveness (RBE_{10}) of each beam was calculated for an SOBP extending from
374 depths of 78 to 138 mm in a skull phantom using the modified microdosimetric kinetic model (MKM). The
375 RBE_{10} of the radioactive ion beams was found to be within one standard deviation of the corresponding
376 non-radioactive ion beams for all energies, indicating that the therapeutic efficacy of such beams should
377 be very similar to beams of the corresponding non-radioactive ion.

378 Finally, the additional dose to the patient resulting from the use of radioactive beams was estimated
379 to determine whether it poses any unreasonable risk to the patient compared to the use of a stable ion
380 beam. The additional dose was found to be comparable to that received during diagnostic clinical PET,
381 and therefore negligible compared to the dose delivered to the target volume or surrounding tissues during
382 the radiotherapy procedure.

383 In summary, positron-emitting radioactive heavy ions are approximately equivalent to the correspond-
384 ing stable isotope with respect to expected therapeutic properties in heavy ion radiotherapy, while being
385 greatly superior to non-radioactive beams in terms of the potential for accurately imaging the treatment
386 volume during and after treatment. The substantial increase in positron yield offered by positron-emitting
387 radioactive beams for the same biological effective dose will allow the boundaries of the spread out Bragg
388 peak in a PET image to be unambiguously identified, making the use of positron-emitting radioactive ions
389 a compelling choice for heavy ion therapy.

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511 **Author Contributions**

512 Dr M. Safavi-Naeini contributed to the concept of using radioactive beams therapeutically, proposed
513 and contributed to the implementation of methods used for validation of the hadronics physics model,
514 the method used for simulation of pseudo-clinical beams and evaluation of their RBE, variance analysis
515 method used to estimate a sufficient number of primary particles to use in the simulations, and the
516 quantification of positron fragmentation yield. She implemented and quantified the excess dose received
517 as a result of the use of radioactive primary beams, analysed the intra-spill and post treatment images and
518 quantified the CNR. Dr Safavi-Naeini organised the manuscript preparation, has written the majority of
519 the text in the original and revised manuscript and provided overall technical leadership of the project.

520 Mr A. Chacon contributed to the concept, designed and carried out the Monte Carlo simulations,
521 contributed to the data analysis and discussion of results and contributed to the writing of the manuscript.

522 Dr D. Bolst and Dr S. Guatelli contributed to the concept, the implementation of the modified MKM
523 and participated in the preparation of the manuscript.

524 Dr D.R. Franklin contributed to the data analysis, image quality assessment, discussion of results,
525 manuscript preparation and provided an overall editorial reviewing of the manuscript.

526 Dr A. Mohammadi provided Figure 1 and Figure 2, the experimental dosimetric and imaging data
527 used in the validation of the electromagnetic and hadronics physics model and assisted in the manuscript
528 preparation.

529 Dr H. Tashima, Dr E. Yoshida, Dr Y. Iwao, Dr F. Nishikido, Dr A Kitagawa and Prof T. Yamaya
530 contributed to the design of the dosimetric and imaging experiments, and preparation of the dynamic
531 images used in the validation of the hadronics physics model.

532 Prof Gregoire contributed to the manuscript preparation and provided technical feedback on the
533 analytic methodology.

534 Dist Prof A. Rozenfeld contributed to the concept and the method for the quantification of the relative
535 biological effectiveness of radioactive beams, assisted with the manuscript preparation and contributed his
536 extensive knowledge and experience of particle therapy and dosimetry.

537 **Additional Information**

538 The author(s) declare no competing interests. The datasets generated during and/or analysed during the
539 current study are available from the corresponding author on reasonable request.