

48 into a current of electrons in the two end electrodic compartments [7, 8]. At the
49 same time, electro-chemical equilibria at the solutions/membranes interface
50 generate a voltage increase along the same direction of electric current, thus
51 reproducing the operation of a power generator or a battery.

52

53 Pressure retarded osmosis operates in a different way. The high and low
54 concentration solutions are separated by an osmotic membrane that rejects ionic
55 species but allows water to pass through from the dilute solution to the concentrate
56 one, driven by the difference in water activity (i.e. in osmotic pressure) of the two
57 solutions [8]. In PRO, the high concentration solution (draw solution) is pressurized
58 and fed into the membrane module, so that the passage of water from the low
59 salinity (feed) solution is “retarded” by the hydraulic pressure applied. In this way,
60 the permeating water gains pressure and the chemical potential is converted
61 into pressure energy or hydraulic energy transferred to the draw solution. Fraction
62 of the diluted draw solution equals to the volume of permeate flow goes into a
63 hydro turbine for power generation while the other fraction is used to pressurize the
64 draw solution entering the membrane module via an ideal pressure exchanger
65 [figure 1].

66

67 Despite the high potential of salinity gradient power technologies, PRO technology
68 has not been commercialized yet. Several pilot plants have been tested worldwide in
69 addition to the large number of laboratory size experiments. First pilot plant was
70 tested by Statkraft using the salinity gradient between seawater and river water, and
71 was not successful to satisfy the required energy demands [3]. This is, most likely,
72 because of the low osmotic pressure driving force across the PRO membrane [3].
73 Subsequent pilot plant test in Mega-ton project, Japan, demonstrated better results
74 with 7.7 W/m^2 power density [9], that is greater than recommended threshold of 5.5 W/m^2
75 W/m^2 [3]. Toyobo hollow fiber membrane was used in the conjunction with the
76 salinity gradient of reverse osmosis (RO) brine and wastewater for power generation.
77 With Toyobo membrane, a maximum 30 bar feed pressure can be applied on the
78 draw solution side of the PRO membrane [10]. However, researchers have
79 developed laboratory scale membranes with high water flux and can tolerate a range
80 of hydraulic pressure that exceeds 30 bar. Madsen et al., carried out PRO experiment
81 at 70 bar using 5M NaCl draw solution to reach power density in excess of 5.5 W/m^2
82 [11]. Li et al., [12] reported 4.3 W/m^2 power density at 12 to 13 bar hydraulic
83 pressure using wastewater RO retentate and 1M NaCl feed and draw solution,
84 respectively. The research group used in-house developed hollow fiber PRO
85 membrane and experiments were performed at Forward Osmosis (FO) mode [AL-FS]
86 to decrease pretreatment requirements of feed solution. Wan and co-workers [13]
87 achieved 38 W/m^2 at 30 bar hydraulic pressure using thin-film composite hollow
88 fiber membrane. The salinity gradient resource was DI water feed solution and 1.2M
89 NaCl draw solution. In an experiment to evaluate the structural stability of PRO
90 membrane researchers conducted PRO experiment over 10 hours on a laboratory
91 fabricated membrane polyamide membrane [14]. A power density of 12.8 W/m^2 was
92 achieved at 17.2 bar hydraulic pressure. Chen et al., [15] performed a laboratory
93 experiment to test stability of polyamide PRO membrane. The research group
94 reported 19.2 W/m^2 power density at 15.0 bar hydraulic pressure using 1.0 M NaCl

95 and DI water as the draw and feed solution, respectively. Hickenbottom et al., [16]
96 evaluated commercially available membrane for PRO process. The study found that
97 thin-film composite (TFC) polyamide membrane from Hydration Technology
98 Innovations (HTI) is the most stable membrane with 22.6 W/m^2 power density at 41
99 bar hydraulic pressure using 3M NaCl draw solution. Unfortunately, membrane
100 deformation was detected at 35 bar hydraulic pressure.

101

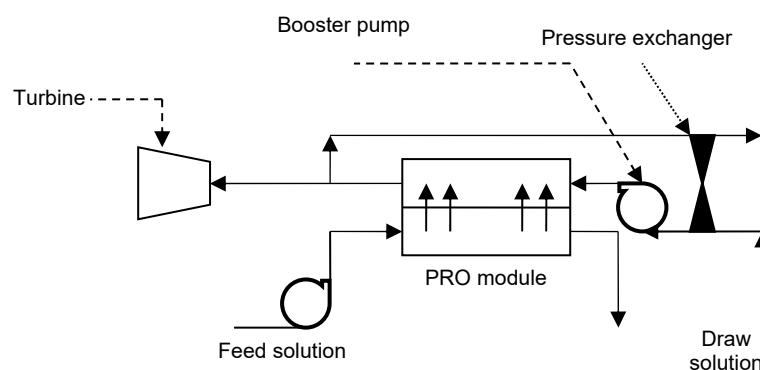
102 In the unoptimized (normal) PRO process, the recommended hydraulic pressure is
103 equal to $\Delta P = \Delta\pi/2$ and the flow rate of feed solution is equal to that of draw
104 solution [4]. Most researchers and scientists still recommend optimum values of
105 hydraulic pressure and feed to draw mixing ratio that are obtained from a laboratory
106 scale PRO process, ignoring the difference in the hydrodynamic conditions and
107 concentration variation along channels between laboratory and full-scale membrane
108 [5, 17]. However, dilution and concentration of draw and feed solution in a full-scale
109 PRO module affect the osmotic driving force and extractable energy along the PRO
110 membrane. Tamburini et al. [18] reported a very preliminary analysis of the effect of
111 up-scaling and non-ideal phenomena in PRO performance. The study highlighted the
112 evidence that optimal operating pressure and flow rate may differ depending on
113 module geometry and feed composition. However, in that study, no effort toward a
114 structured optimisation process was performed.

115

116 In the current study, a computer model was applied to find the optimum hydraulic
117 pressure and feed to draw ratio that is required to maximize the energy output from
118 salinity gradient in the PRO process. The performance of the PRO process was
119 optimized in a full-scale PRO module using a validated computer model. The study
120 investigated different types of salinity gradients to mimic a number of natural feed
121 and draw solutions that would have been suggested in the PRO process.

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Figure 1: A schematic diagram of PRO process

131

132 **2. Materials and methods**

133

134 *2.1 Pressure retarded osmosis model*

135

136 A physical model was used to calculate water flux in the PRO process taking into
 137 account the impact of concentration polarization and external resistance along the
 138 PRO module. Some details on the model formulation and implementation are
 139 reported in the Appendix A1, while only the main equations are presented below.
 140 The model was validated using experimental data from a pilot plant [20], though
 141 relevant information is also reported in the Appendix A2 [Table A1]. Water flux along
 142 the PRO module was calculated from the following equation [17]:
 143

$$144 \quad J_{w,x} = A_w \left\{ \frac{(nRT C_{Di,x} (1 + \frac{Q_{Di,x}}{Q_{Do,x}}) / 2) \exp\left(\frac{-J_{w,x}}{k_d}\right) - nRT C_{Fi,x} \left(1 - \frac{Q_{Fi,x}}{Q_{Fo,x}}\right) \exp\left(J_{w,x} K + \frac{J_{w,x}}{k_f}\right)}{1 + \frac{B}{J_{w,x}} \left(\exp\left(J_{w,x} \frac{J_{w,x}}{k_f}\right) - \exp\left(\frac{-J_{w,x}}{k_d}\right)\right)} - \Delta P \right\} [1]$$

145

146 where, $J_{w,x}$ is the water flux (L/m²h) along the PRO module with interval $x = 0.1$ m, n
 147 is number of ions in the solution, R is the gas constant, and T is the temperature in
 148 Kelvin. A_w and B were assumed to be 1.23 L/h.m².bar and 2.6 kg/h.m² respectively,
 149 $k_d = k_f = 0.18$ m/h, and $K = 31$ h/m, $C_{Di,x}$ represents the inlet concentration of the draw
 150 solution at the distance x along the membrane, $C_{Fi,x}$ represents the inlet
 151 concentration of the feed solution at the distance x along the membrane, $Q_{Di,x}$ and
 152 $Q_{Do,x}$ represent the inlet and outlet flow rate of the draw solution, respectively, and
 153 $Q_{Fi,x}$ and $Q_{Fo,x}$ represent the inlet and outlet flow rate of feed solution at distance x
 154 along the membrane, respectively [18]. In this study, the length of the PRO module is
 155 1 m [17] and has 24 m² active area. Equation 1 accounts for concentration
 156 polarization and external resistance in the PRO membrane [9]. Equation 1 is valid for
 157 PRO membrane operating on the PRO mode; i.e. draw solution faces the active layer.
 158 More details on the model derivation can be found in the Appendix A1 and literature
 159 [17]. The fractions of draw and feed volumes, λ_D and λ_F respectively, in the mixture
 160 solution were calculated from the following equations:

$$161 \quad \lambda_D = \frac{\gamma_D}{\gamma_D + \gamma_F} \quad [2]$$

162

$$163 \quad \lambda_F = \frac{\gamma_F}{\gamma_F + \gamma_D} \quad [3]$$

164

165 where, γ_D and γ_F are the volumetric flow rates of draw and feed solution. Specific
 166 energy generation, E_s (kWh/m³), was calculated at different operating conditions
 167 using the following expression:
 168

$$E_s = \frac{\Delta P^* Q_p}{Q_D + Q_F} \quad [4]$$

170

171 where, ΔP is the hydraulic pressure of the draw solution entering the hydro turbine
172 (bar) and Q_p , Q_d and Q_f are the permeate, draw and feed solution flow rates,
173 respectively. In this study, we performed PRO optimization to find the optimum
174 hydraulic pressure and mixing ratios in the PRO system leading to maximum values
175 of specific energy output (E_s). Optimized values of E_s were compared with those in
176 the unoptimized (normal) PRO case for each salinity gradient resource considered.
177 Matlab software was used to implement the model and the optimization algorithm
178 of the PRO process.

179

180 **3. Results**

181 *3.1 Applied hydraulic pressure optimization*

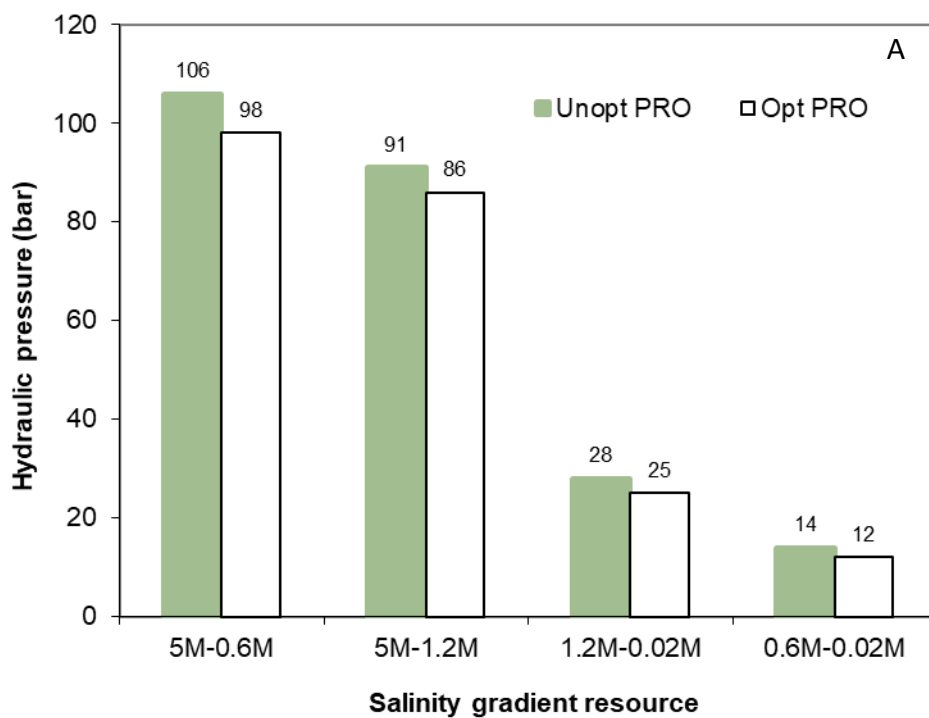
182 Previous studies recommended the optimum hydraulic pressure for the power
183 density to reach a maximum amount is $\Delta P = \Delta \pi / 2$ [4, 5]. This value has been
184 experimentally validated on a flat sheet PRO unit as well as in a full scale ideal PRO
185 process; i.e. ignoring the effect of concentration polarization [5]. We performed PRO
186 optimization for a full-scale spiral wound module taking into account the impact of
187 concentration polarization and results were compared with that from unoptimized
188 PRO process. We assumed pressure drop along the spiral wound is insignificant. Four
189 salinity gradient resources were evaluated using sodium chloride salt, these are 5M-
190 0.6M, 5M-1.2M, 1.2M-0.02M and 0.6M-0.02M to resemble field situation of Dead
191 Sea-seawater, Dead Sea-RO brine, RO brine-wastewater, and seawater-wastewater,
192 respectively. These salinity gradients have been widely investigated in literature due
193 to their potential for application in salinity gradient power plant [1, 5, 6].

194 Hydraulic pressure optimization was performed using equal feed and draw solution
195 flow rates, 2000 L/h. Results in Figure 2A show hydraulic pressure in optimized and
196 unoptimized PRO process consisting of one full-scale module. In general, hydraulic
197 pressure was 5% to 14% lower in the optimized PRO compared to the unoptimized
198 PRO process. The largest difference was 14% for 0.6M-0.02M salinity gradient
199 followed by 7.5%, 5.5% and 11% for 5M-0.6M, 5M-1.2M and 1.2M-0.02M salinity
200 gradients, respectively. Water flux in the PRO module is shown in Figure 2B.
201 Optimized PRO processes exhibited higher water flux than unoptimized PRO
202 processes because of the higher net driving force across the membrane. Water flux
203 decreased across the PRO membrane due to osmotic pressure decrease as a result of
204 dilution of the draw solution and concentration of the feed solution. Figure 2C shows
205 the net energy output in the optimized and unoptimized PRO processes. Hydraulic
206 pressure optimization resulted in none to subtle increase in the energy output in the
207 PRO process. 5M-0.6M and 5M-1.2M salinity gradients exhibited 0.7% and 0.6%
208 increase in energy generation due to the optimization of hydraulic pressure while
209 1.2M-0.02M and 0.6M-0.02M salinity gradients showed no improvement in the
210 energy generation due to optimization of the hydraulic pressure.

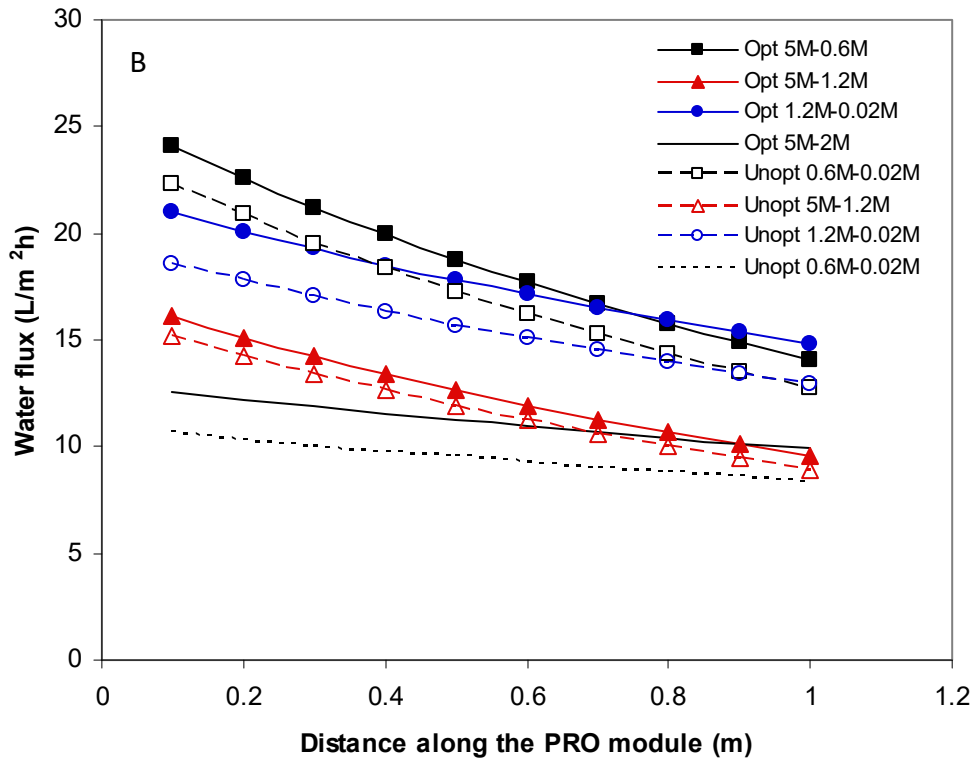
211 The average power density in the optimized PRO process was calculated as the
212 average membrane flux multiplied by the hydraulic pressure; i.e. $W_{ave} = J_{w-ave} * P$ [17].
213 Results show that the average power density of 5M-0.6M, 5M-1.2M and 1.2M-

214 0.02M salinity gradients was slightly higher in the optimized PRO compared to the
215 unoptimized PRO process while there is no improvement in 0.6M-0.02M salinity
216 gradient [Figure 2D]. Apart from 0.6M-0.02M salinity gradient, all salinity gradient
217 resources achieved average power density over 5 W/m² threshold value that is
218 recommended in the PRO process. The advantage of optimization was that
219 optimized PRO process requires less pressure for operation. This would be reflected
220 on the type and characteristics of PRO membrane and high pressure pump and,
221 eventually, on the capital cost of the PRO plant.

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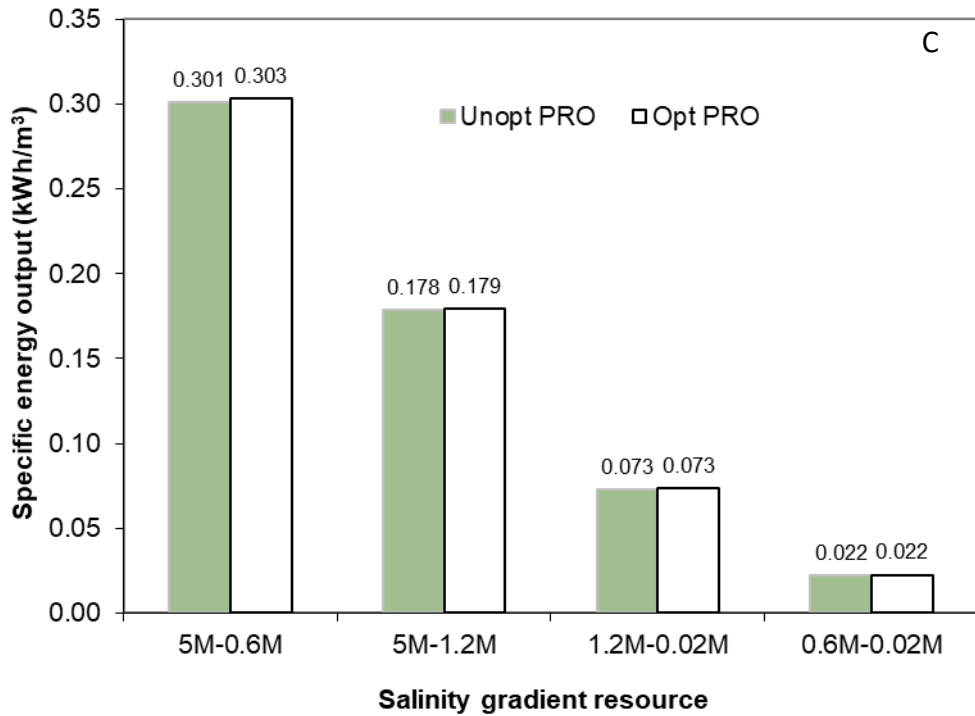


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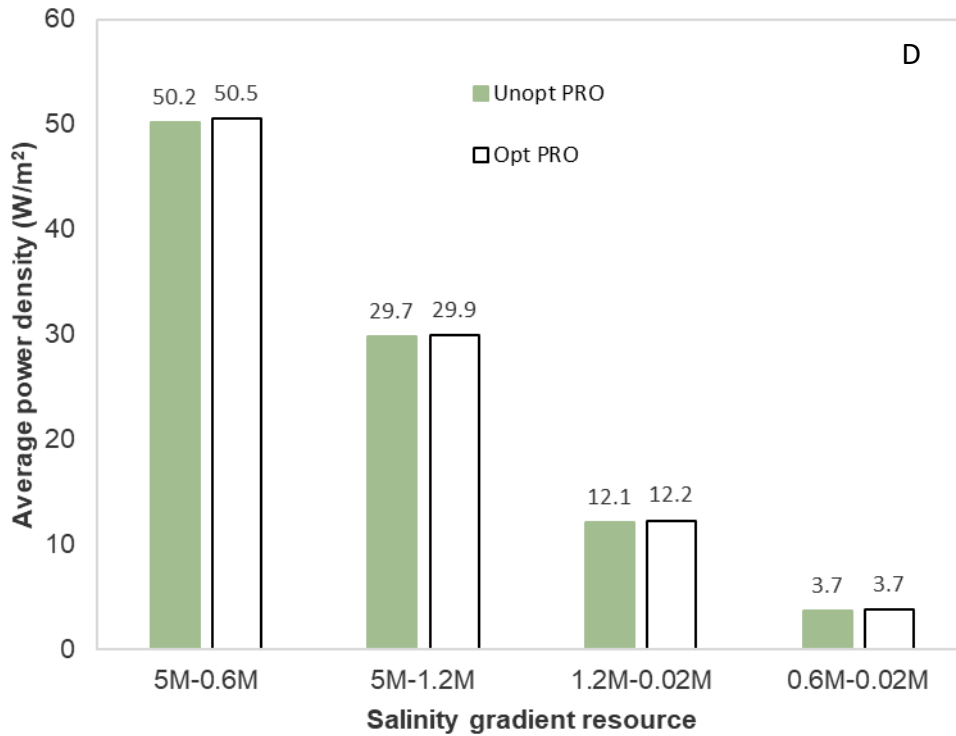
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229 Figure 2: Results of the optimization analysis of applied hydraulic pressure in terms
 230 of: A) optimal applied hydraulic pressure; B) water flux; C) specific energy output D)
 231 average power density

232

233 3.2. Optimization of draw solution to mixture ratio

234 In irreversible PRO processes, researchers proposed that the optimum ratio of draw
 235 to feed solution is 1:1 (i.e. draw to mixture ratio $\lambda_D=0.5$) at a hydraulic pressure
 236 equal to $\Delta P = \Delta\pi / 2$, which maximise the energy output achieved [4]. We
 237 performed an optimization analysis of draw solution flow rate at $\Delta P = \Delta\pi / 2$ for a
 238 number of salinity gradients [Figure 3]. Apparently, optimized PRO process requires
 239 γ_D values below 0.5, contrarily to what is recommended in earlier studies [Figure
 240 3A]. In fact, the optimum γ_D was 0.35, 0.33, 0.31, and 0.26 for 5M-0.6M, 5M-1.2M,
 241 1.2M-0.02M and 0.6M-0.02M salinity gradients, respectively. This suggests that γ_D
 242 decreased with decreasing the osmotic pressure gradient of the salinity gradient
 243 resource. In effect, decreasing the osmotic pressure gradient across the membrane
 244 results in a lower permeation flow and dilution of the draw solution. As such, the
 245 concentrative concentration polarization (ECP) on the feed side will be lower and the
 246 flow rate of the draw solution can be decreased. Finally, a direct effect of reducing
 247 γ_D on the energy generation is related to the definition of E_s , in which a reduction in
 248 the flow rate of feed and/or draw solutions leads to an increase in the specific
 249 energy generation, though a reduction in the total generated power is expected as
 250 commented below [Figure 3D].

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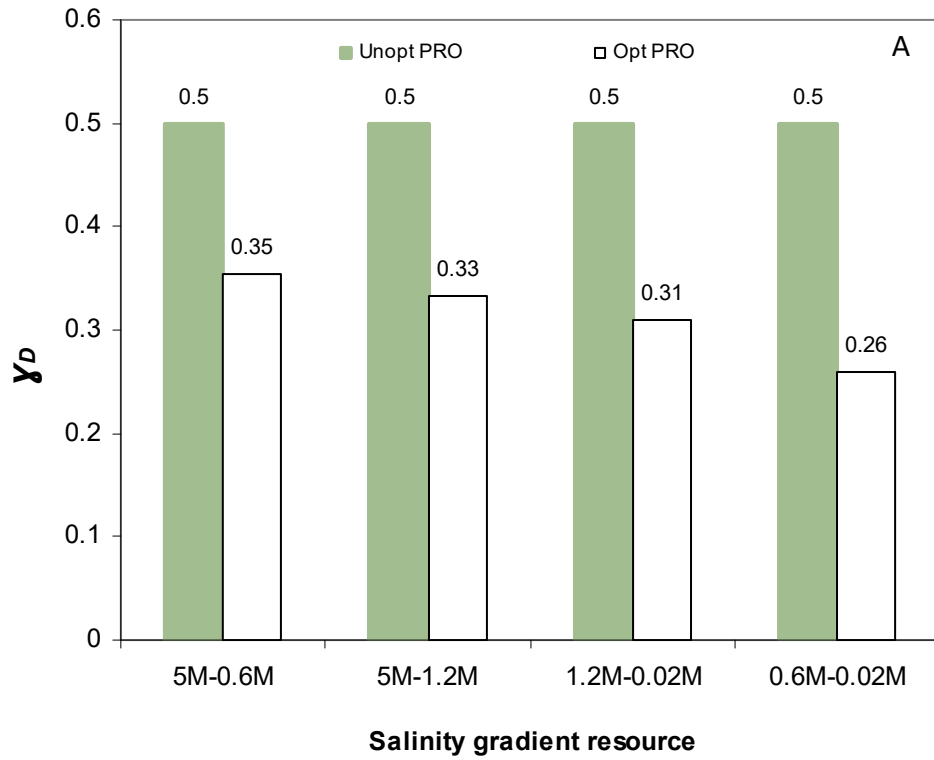
252 Water flux in optimized and unoptimized PRO process is shown in Figure 3B. Results
 253 show also in this case a decrease in water flux along the PRO module due to the

254 decrease in osmotic pressure driving force across the membrane [Figure 3B]. Water
255 flux in the optimized and unoptimized PRO process was not changed for 5M-0.6M
256 salinity gradient. For the other salinity gradients considered, optimized PRO process
257 presents lower water flux than unoptimized water flux. This was due to the intensive
258 concentration polarization at the draw solution side, because of the lower flow rate
259 compared to unoptimized PRO process, in addition to the larger concentration
260 variation due to a more intense dilution process in the smaller draw solution volume
261 flowing in the channel. On the other hand, specific energy output was higher in the
262 optimized PRO process than in the unoptimized process, this observation holds true
263 for all salinity gradients. Despite the lower water flux in unoptimized PRO process,
264 specific energy output was higher because of the lower draw solution flow rate
265 according to Equation 4. The highest increase in specific energy output was 23% for
266 0.6M-0.02M salinity gradient followed by 14%, 13% and 10% for 1.2M-0.02M, 5M-
267 1.2M and 5M-0.6M salinity gradient, respectively. Figure 3D reveals that the average
268 power density in the optimized PRO process is equal to that in the unoptimized
269 process in 5M-0.6M salinity gradient resource but it is lower than the average power
270 density in unoptimized PRO process in 5M-1.2M, 1.2M-0.02M and 0.6M-0.02M
271 salinity gradients. That is because reducing the flow rate in the optimized PRO
272 process [Figure 3A] resulted in a decrease in the water flux across the membrane
273 due to the effect of concentration polarization. Therefore, the average power
274 density was lower in the optimized PRO process.

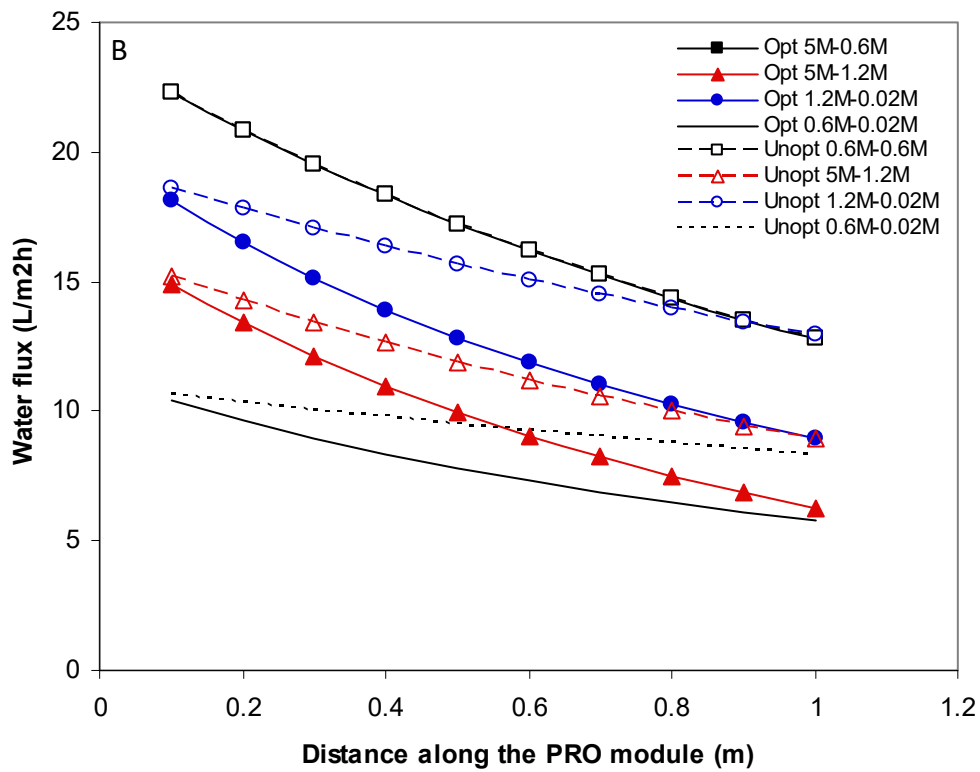
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276 Overall, results show that optimization of the draw solution flow rate has more
277 impact on improving the specific energy output in the PRO process. In fact,
278 optimization of feed pressure resulted in a subtle increase of the specific energy
279 output, <1%, while optimization of draw solution flow rate increased the specific
280 energy output up to 23%. Moreover, a lower draw solution flow rate in real PRO
281 plants would also decrease the effect of pumping losses on the overall process
282 efficiency.

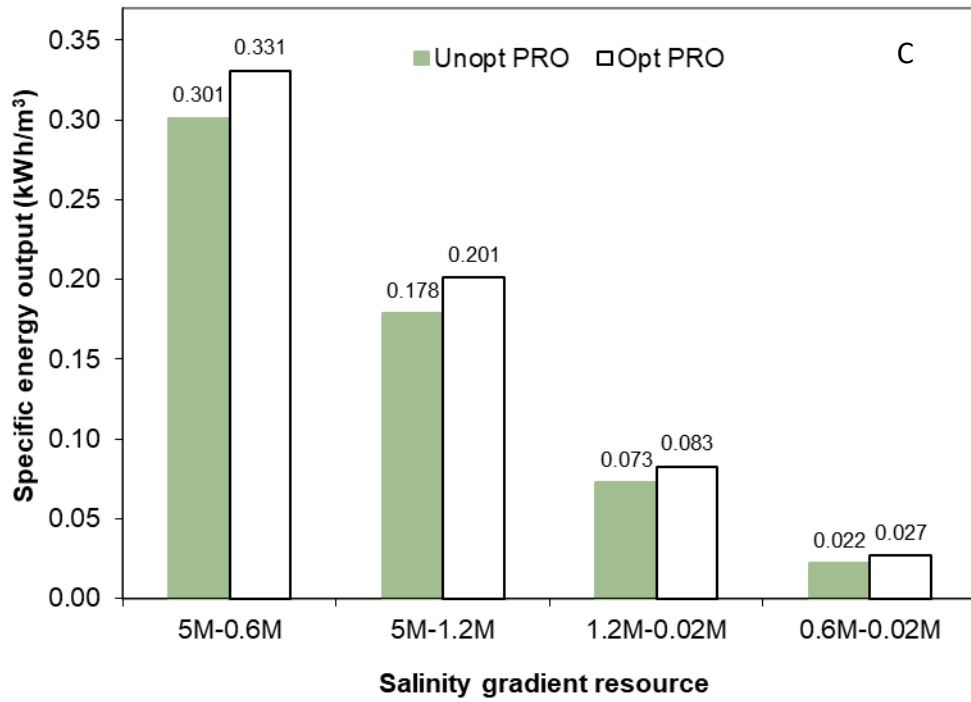
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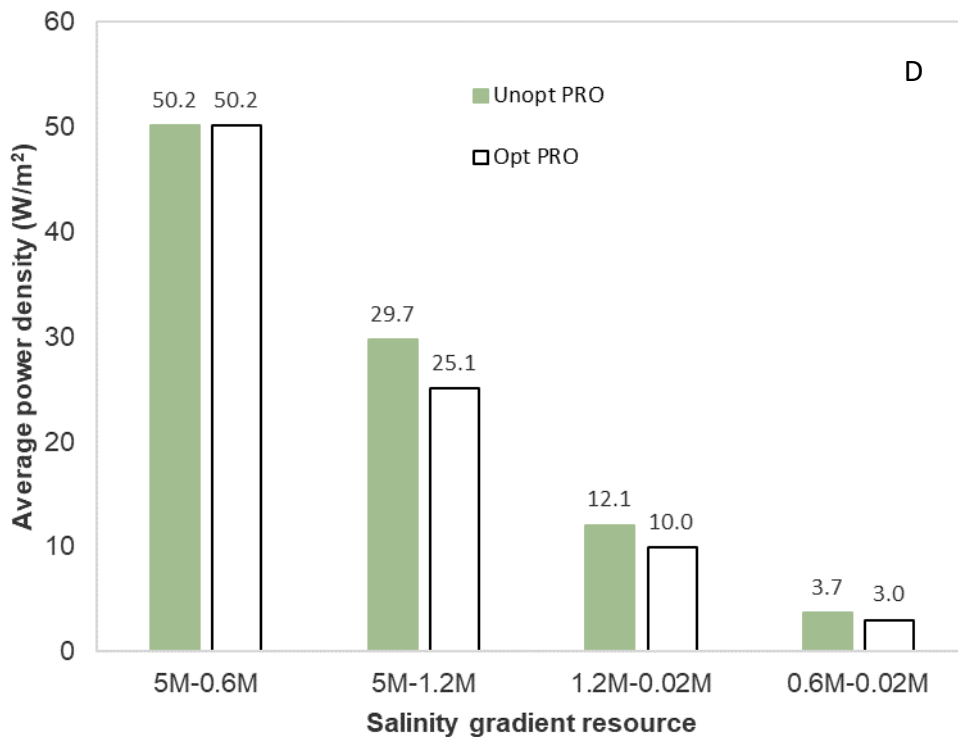
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Figure 3: Results of the optimisation analysis of draw solution flow rate in terms of: A) optimal draw solution mixing ratio; B) water flux; C) specific energy output; D) average power density. Hydraulic pressure on the draw solution is equal to $\Delta\pi/2$

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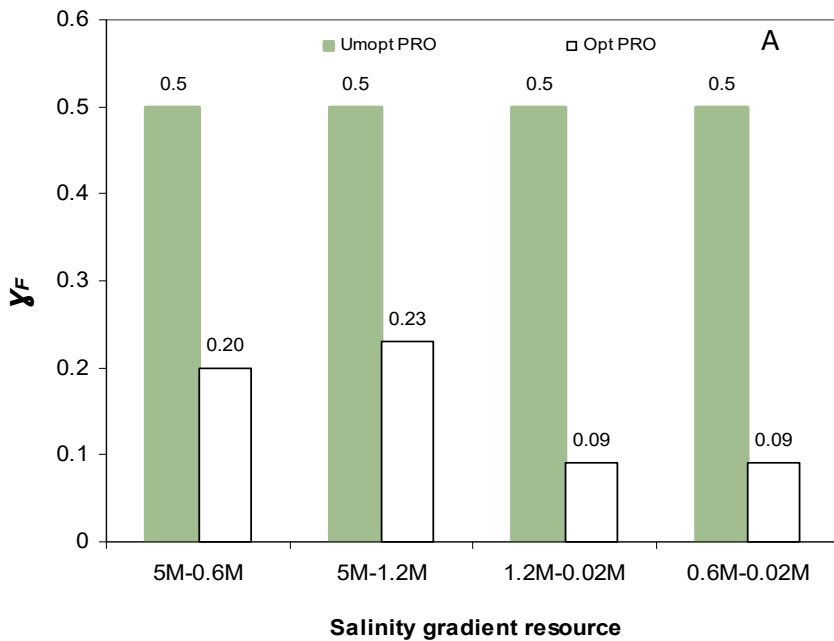
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298 **3.3. Optimization of feed solution to mixture ratio**

299 Optimization of the feed solution to mixture ratio was carried out for the same
300 salinity gradient resources previously considered and results were compared with
301 the unoptimized cases. All results were obtained at a hydraulic pressure gradient
302 equal to $\Delta P = \Delta \pi / 2$. In all cases the optimal ratio of feed flow rate in the mixing
303 solution, γ_F , was significantly lower than the optimum value recommended in
304 earlier studies (equal to 50% [5]), ranging from 0.2 to 0.23, 0.09, and 0.09 for 5M-
305 0.6M, 5M-1.2M, 1.2M-0.02M and 0.6M-0.02M salinity gradients, respectively [Figure
306 4A]. Water flux, however, decreased along the PRO module and was lower in the
307 optimized PRO process than in the unoptimized processes [Figure 4B]. Difference
308 between optimized and unoptimized water flux increased with the increase of the
309 osmotic pressure driving force across the PRO membrane because lower feed flow rate
310 rate brought about more intense internal concentration polarization and a more
311 pronounced reduction in the salinity gradient along the channel, as in the case of γ_D
312 optimisation. There was a 30% decrease in water flux for both 5M-0.6M and 5M-
313 1.2M salinity gradients, 13% for 1.2M-0.02M salinity gradient and 10% for 0.6M-
314 0.02M salinity gradient. Despite the lower water flux in the optimized PRO process,
315 specific power generation was higher in optimized PRO than reference conditions
316 [Figure 4C]. This was because of the higher energy generation per cubic meter of
317 mixed solution generated in the optimized PRO process. The highest specific energy
318 generation was 0.402 kWh/m³ for a 5M-0.6M salinity gradient, followed by 0.229,
319 0.123, and 0.037 for 5M-1.2M, 1.2M-0.02M and 0.6M-0.02M salinity gradient
320 resource, respectively.

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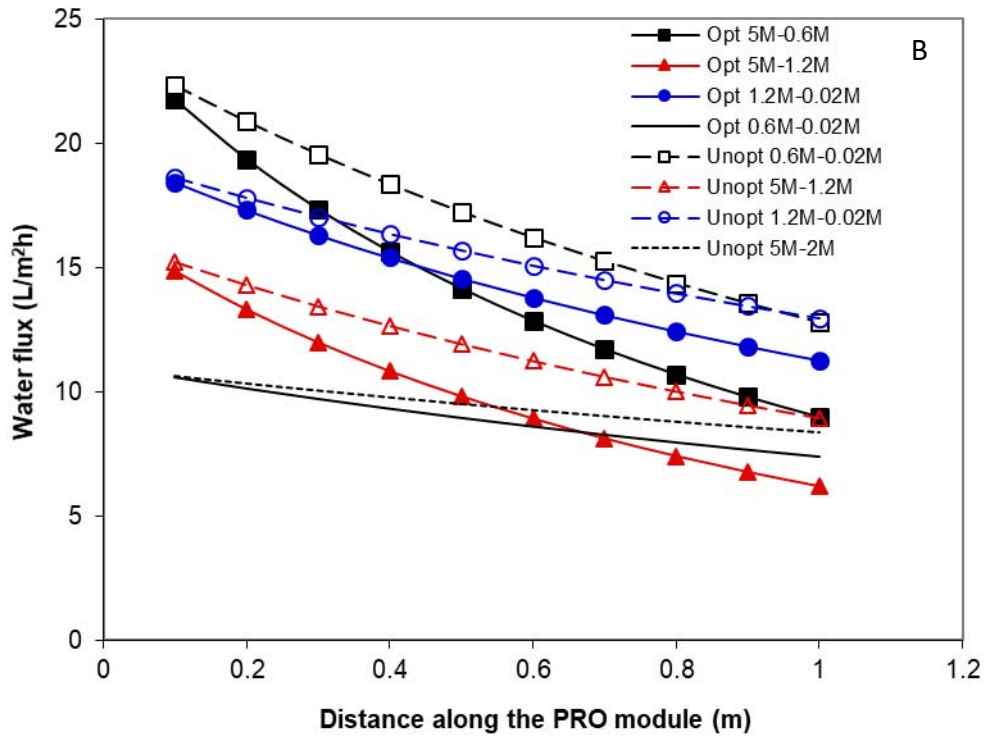


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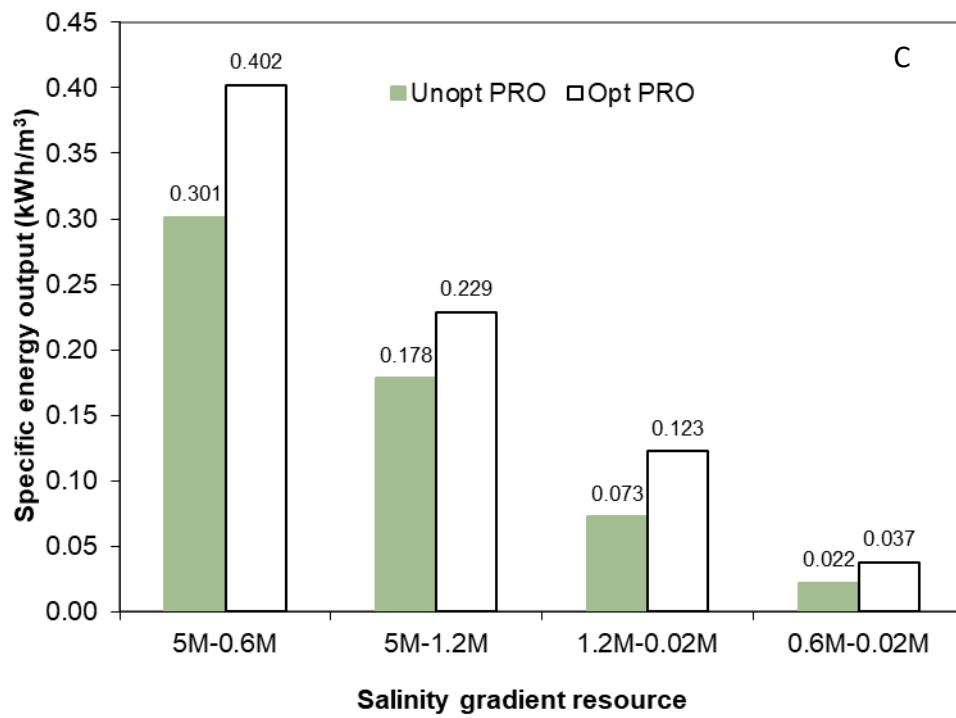
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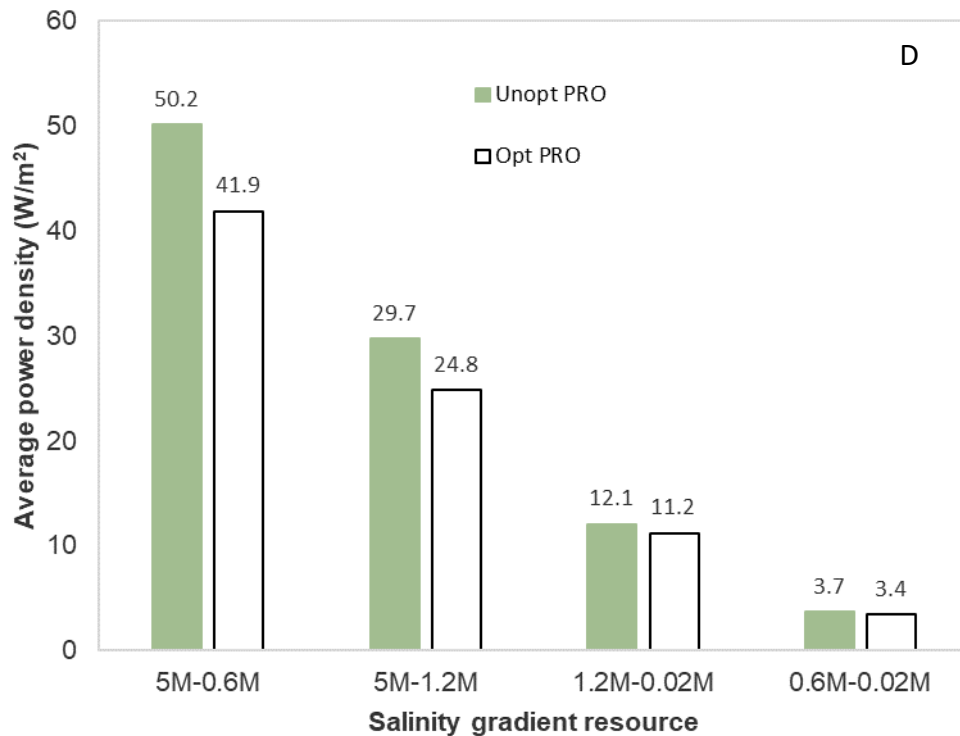
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334 Figure 4: Optimization of feed solution flow rate A) optimized and unoptimized draw
 335 solution mixing ratio B) membrane flux C) energy output; D) average power density.
 336 Hydraulic pressure on the draw solution is equal to $\Delta\pi/2$

337

338

339 Results in Figures 4C and 4D show an improvement in the specific energy output in
 340 the optimized PRO process although the average power density in the optimized
 341 processes is lower than that in the unoptimized processes. The reason for this is that
 342 reducing the flow rate of draw solution reduced water flux and hence the average
 343 power density per square meter of membrane area. However, unoptimized PRO
 344 process uses higher draw solution flow rate and that decreased the specific energy
 345 output per cubic meter of processed draw and feed solution mixture, Equation [4].
 346 This suggest that the average power density should not be always taken as an
 347 indicator for high performance PRO process as it does not consider the effect of feed
 348 and draw solution flow rates. Finally, feed flow optimization resulted in up to 68%
 349 increase in the specific energy generation for 0.6M-0.02M salinity gradient and
 350 about 65% increase in the specific energy generation for 1.2M-0.02M salinity
 351 gradient. Results also show that optimization of feed flow rate had the highest
 352 impact on the specific energy generation in the PRO process, followed by draw
 353 solution flow rate and finally the hydraulic pressure. It should be mentioned that
 354 although hydraulic pressure optimization resulted in subtle increase in the specific
 355 energy generation, it also allows PRO process to work at lower pressure, which may
 356 decrease the capital cost because of the less demanding high-pressure pump and
 357 PRO membrane specifications required.

358

359

360

361 *3.4 Optimization of hydraulic pressure and feed flow rate*

362 Simulation results revealed that optimization of feed flow rate results in a tangible
363 improvement in the specific power generation in the PRO process. PRO process with
364 optimized feed flow rate in section 3.3 was further optimized for the hydraulic
365 pressure to improve the process performance. The combined effects of hydraulic
366 pressure and feed flow rate on the performance of the PRO process is shown in
367 Figure 5. The ratio of feed flow in mixture, γ_F , reduced from 0.5 in the unoptimized
368 PRO process to 0.2 in the optimized PRO process using 5M-0.6M salinity gradient
369 resource [Figure 5A]. Reducing the flow rate of feed solution will increase the
370 specific energy generation according to Equation 4 while decreasing the operation
371 and capital cost. For 5M-1.2M, 1.2M-0.02M and 0.6M-0.02M salinity gradients, γ_F
372 was 0.23, 0.09 and 0.9 respectively. The ratio of feed flow rate to mixture in the
373 optimized PRO process was between 18% and 46% of that in the unoptimized PRO
374 process, $\gamma_F \sim 0.5$.

375

376 Water flux in the optimized and unoptimized PRO process is explained in Figure 5B.
377 The optimized PRO process with 5M-0.6M and 5M-1.2M salinity gradients exhibited
378 lower water flux than that in the unoptimized PRO process [Figure 5B]. This is caused
379 by the lower feed flow rate in the optimized PRO process, which intensified the
380 impact of concentrated concentrative concentration polarization. Water flux with
381 the optimised PRO configuration follows the observed trend for the previous
382 optimisation cases. In fact, while the reduction in the applied pressure leads to an
383 increase in flux, the reduction of feed flow rate reduces it. The obtained trend of
384 water flux along the channel indicates a significant reduction of water flux in the
385 case of highly concentrated draw solutions (5M), with a maximum deviation
386 between optimised and non-optimised case being around 30% in the last part of the
387 channel. For lower concentration draw solution (1.2M and 0.6M) roughly the same
388 average flux is observed for the optimised case. The difference in water flux between
389 optimized and unoptimized PRO was 6% and 4% for 1.2M-0.02M and 0.6M-0.02M
390 salinity gradients, respectively. The reason for insignificant difference in water flux
391 between the optimized and unoptimized PRO process was due to low feed
392 concentration, which caused only minor concentrative concentration polarization
393 effect. Despite the lower water flux in the optimized PRO process, the specific power
394 generation was higher in the optimized than in the unoptimized PRO process. This is
395 due to the lower feed flow rate in the optimized PRO process, which resulted in a
396 higher specific power output per mixed volume of salinity gradient resource. It
397 should be mentioned that lower water flux in the optimized PRO processes indicates
398 to the fact of larger membrane area is required to generate an equal flow comparing
399 to unoptimized PRO process. In light of the results here, optimized PRO process
400 requires between 4% to 29% higher membrane area. Although this will increase the
401 capital cost, it should be noted that membrane life is 5 years at least. Furthermore,
402 commercial PRO membranes price is now available as low as 17 USD/m² such as
403 Toyobo hollow fibre FO membrane [1]. For 1.2M-0.02M and 0.6M-0.02M salinity
404 gradients, only 4% to 6% increase in the membrane area is required upon process
405 optimization, which is insignificant difference over 5 years.

406

407 Specific power generation in the PRO process is illustrated in Figure 5C. The largest
 408 increase in the specific power generation was 72% in the optimized 0.6M-0.02M
 409 salinity gradient resource followed 1.2M-0.02M, 5M-0.6M, and 5M-1.2M salinity
 410 gradient, respectively [Figure 5C]. The lowest increase in the specific power
 411 generation was 29% for 5M-1.2M salinity gradient resource. This is probably due to
 412 the high feed concentration, which led to a significant concentrative concentration
 413 polarization. The average power density in the optimized PRO process was illustrated
 414 in Figure 5D. In general, the average power density in the optimized PRO process
 415 was lower than that in the unoptimized PRO process. The optimized resulted in a
 416 16.3%, 16.1%, 6.6% and 5.4% reduction in the average power density for 5M-0.6M,
 417 5M-1.2M, 1.2M-0.02M, and 0.6M-0.02M salinity gradient, respectively. All salinity
 418 gradient resources showed an average power density over 5W/m² except 0.6M-
 419 0.02M salinity gradient in which it was 3.5 W/m². The optimum hydraulic pressure in
 420 the optimized POR process is 100, 89, 26, and 13 bar for 5M-1.2M, 1.2M-0.02M, and
 421 0.6M-0.02M salinity gradient, respectively [Figure 5D]. The corresponding values in
 422 the unoptimized PRO process are 106, 91, 28, and 13 bar, respectively. The
 423 advantage of operating the PRO at lower hydraulic pressure will be reflected on the
 424 operation and capital cost of the PRO process that would need lower equipment
 425 specifications than the unoptimized PRO process.

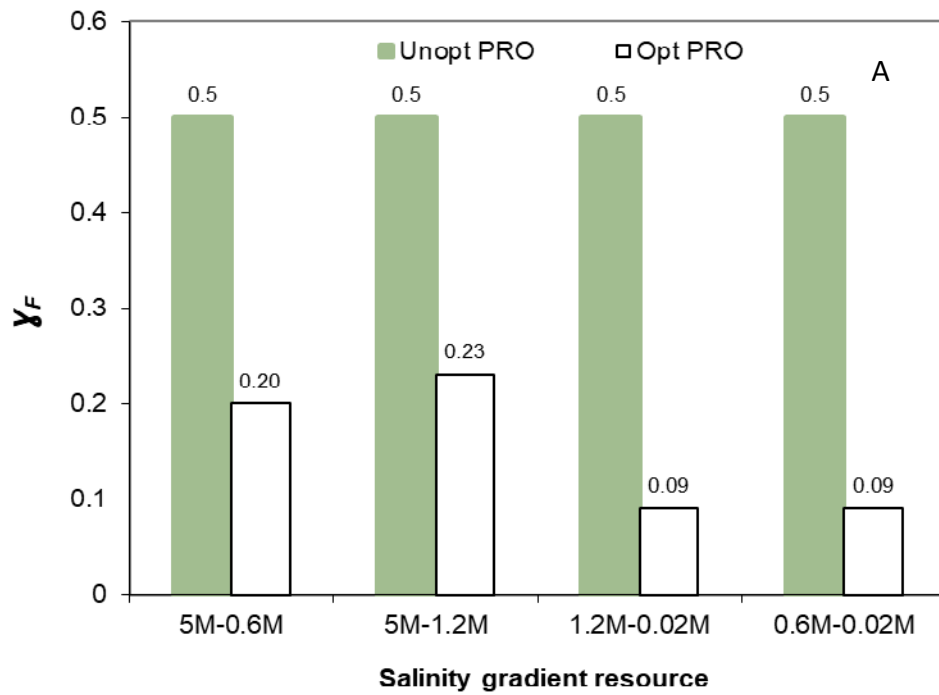
426
 427 The energy generation in the PRO module only is the difference between energy
 428 output and energy input [17]. The energy input, E_{in} (kWh/m³), around the PRO
 429 module is the pumping energy that is calculated from the following expression:

430
 431
$$E_{in} = \frac{Q_{Di} * P_F + Q_{Fi} * P_D}{n * Q_p} \quad [5]$$

432 Where, P_F and P_D are the pressure of feed and draw solution (bar), Q_p is the permeate flow
 433 rate and n is the pump efficiency. The energy required for pumping solution in the PRO
 434 module is 1 bar [17]. The net energy generation in the PRO process depends on the type of
 435 salinity gradient resource and are illustrated in table1 for the analysed scenarios. The results
 436 show that highest net energy output was 0.313 kWh/m³ for 5M-0.6M salinity gradient
 437 resource followed by 5M-1.2M salinity gradient resource (0.095 kWh/m³) and 1.2M-0.02M
 438 salinity gradient resource (0.036 kWh/m³). For 0.6M-0.02M salinity gradient resource, the
 439 energy output was lower than the energy input as illustrated in Table 1. In effect, the energy
 440 output in the PRO process is directly dependent on the chemical potential of salinity
 441 gradient resource. Unfortunately, 0.6M-0.02M salinity gradient has low chemical potential,
 442 which resulted in an insignificant driving force across the membrane to generate enough
 443 osmotic power. The results of this study is in agreement with previous findings, which
 444 highlighted significance of salinity gradient for power generation in the PRO process [5, 18].
 445 Apparently, salinity gradient with low osmotic energy such as 0.6M-0.02M salinity gradient is
 446 not suitable for power generation in the PRO process unless significant improvements in the
 447 process are achieved (e.g. increasing the water permeability of PRO membrane or
 448 dramatically reducing the pumping losses in the PRO module). On the other hand, the
 449 energy generated from 5M-0.6M, 5M-1,2M and 12M-0.02M salinity gradients was promising
 450 for power generation from osmotic energy. More research is underway to develop high
 451 permeability PRO membrane and better performing modules but one of the major issues to
 452 overcome is the membrane cost.

453

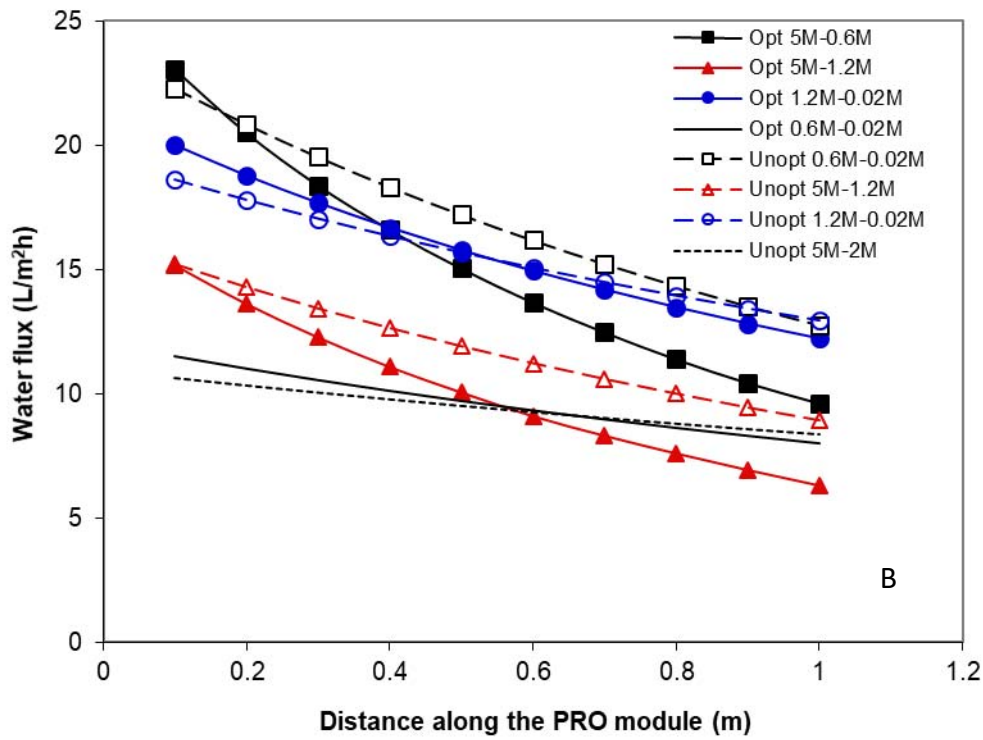
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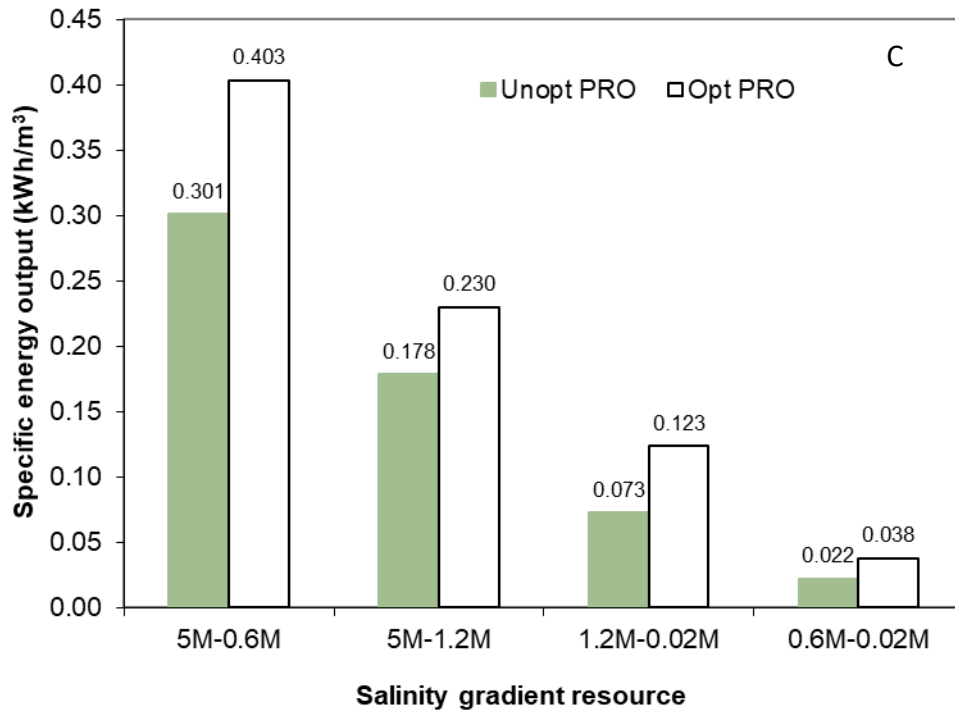
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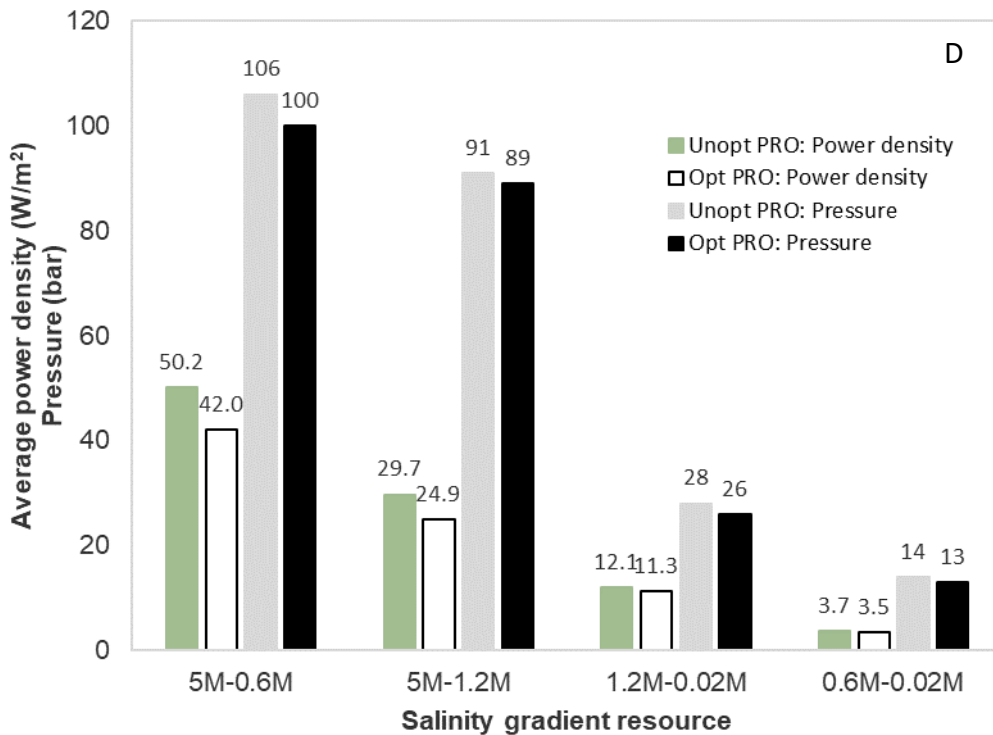
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Figure 5: Optimized hydraulic pressure and feed flow rate in PRO A) feed flow fraction in mixture B) water flux C) specific power consumption D) average average power density.

470 Table 1: Net energy generation in the PRO process for different salinity gradient
 471 resources as the difference between the energy generation and pumping energy in
 472 the PRO module

Process Description	Energy kWh/m ³			
	5M-0.6M	5M-1.2M	1.2M-0.02M	0.6M-0.02M
Pumping energy in module	0.090	0.135	0.087	0.141
Energy output	0.403	0.230	0.123	0.038
Net energy input	0.313	0.095	0.036	-
<i>Applied Pressure bar (opt)</i>	<i>100</i>	<i>89</i>	<i>26</i>	<i>13</i>

473
 474
 475

476 4. Conclusions

477 PRO process was evaluated for power generation from salinity gradient resources
 478 under different operating conditions. Key operating parameters such as the
 479 hydraulic pressure and feed and draw fractions in the mixing solution were
 480 optimized using a computer model. The results showed that the specific energy
 481 output of a full-scale PRO process could be increased by process optimization.
 482 Previous optimization processes performed in a laboratory size experimented
 483 ignored the impact of draw solution dilution along the PRO module. The results of
 484 this study showed that dilution of draw solution in a full-scale module has significant
 485 impact on the operating parameters. This is due to the change in the chemical
 486 potential and osmotic energy along the PRO module in the PRO process. The key
 487 operating parameters in laboratory size experiment, $Q_D=Q_F$ and $\Delta P=\Delta\pi/2$, was found
 488 invalid in a full-scale PRO module.

489

490 The impact of the optimized operating parameters on the energy output in the PRO
 491 process varied from a subtle to a tangible increase in the specific energy generation.
 492 Hydraulic pressure was found to have a subtle impact on the energy output in the
 493 PRO process, <5% increase in the energy output, while the optimization of draw
 494 solution flow rate brought out up to 23% increase in the energy yield. However,
 495 optimization of the feed flow rate demonstrated the highest impact on the energy
 496 yield in the PRO process with up to 68% increase. Finally, PRO process was optimized
 497 for the hydraulic pressure and feed flow rate to maximize the specific energy
 498 generation in the PRO process. The study showed the importance of computer-
 499 based algorithms in engineering and renewable energy field.

500

501 Appendix

502

503 A1 Model description

504

505 Equation 1 calculates water flux, J_w , in the PRO process [21]:

506

$$J_w = A_w \left(\frac{\pi_{Db} e^{\left(\frac{-J_w}{k}\right)} - \pi_{Fb} e^{\left(\frac{J_w K}{k}\right)}}{1 + \frac{B}{J_w} \left(e^{\left(\frac{J_w K}{k}\right)} - e^{\left(\frac{-J_w}{k}\right)} \right)} - \Delta P \right) \quad [1]$$

where, π_{Db} and π_{Fb} are the osmotic pressures of the bulk draw and feed solution, respectively, A_w is the water permeability coefficient, ΔP is the hydraulic pressure across the PRO membrane, k is the mass transfer coefficient, B is the solute permeability coefficient, and K is the solute resistivity for diffusion within the porous support layer. The bulk concentration of draw solution, C_{Db} , is the average of inlet and outlet concentration of draw solution. We assumed PRO module of L length and divided into x number of equal sections. Equation 2 calculated the bulk concentration of draw solution, C_{Db-x} , at distance x from the membrane inlet:

$$C_{Db,x} = \frac{C_{Di,x} + C_{Do,x}}{2} \quad [2]$$

where, $C_{Di,x}$ and $C_{Do,x}$ are the inlet and the outlet concentrations of the draw solution at distance x . We assumed a PRO membrane of a perfect rejection to solutes, the outlet concentration of draw solution can be determined from mass and flow balance equation. At the entrance of the PRO module, the inlet concentration of draw solution; is already known whereas the outlet concentration of draw solution is obtained from mass and flow balance of draw solution [22]:

$$C_{Do,x} = \frac{C_{Di,x} * Q_{Di,x}}{Q_{Do,x}} \quad [3]$$

where, Q_{Di-x} is the inlet flow rate of draw solution, C_{Di-x} is the inlet concentration of draw and Q_{Do-x} is the outlet flow rate of draw solution. The calculated output parameters from the previous section will be the input parameters of the next section. Furthermore, Q_{Do-x} is the sum of inlet flow rate of draw solution, Q_{Di-x} , and permeate flow rate, Q_{p-x} :

$$Q_{Do,x} = Q_{Di,x} - Q_{p,x} \quad [4]$$

Compensating equation 3 in Equation 2 to give:

$$C_{Db,x} = \frac{C_{Di,x} \left(1 + \frac{Q_{Di,x}}{Q_{Do,x}}\right)}{2} \quad [5]$$

Similarly, the bulk concentration of feed solution, C_{Fb-x} , is calculated from averaging the inlet and outlet concentrations of feed solution as in Equation 6:

$$C_{Fb,x} = \frac{C_{Fi,x} + C_{Fo,x}}{2} \quad [6]$$

547 here, C_{Fi-x} and C_{Fo-x} are the concentrations of inlet and outlet feed solution. Equation
 548 7 calculates the outlet concentration of feed solution form mass and flow balance at
 549 the draw solution side of the PRO membrane [2]:

550

$$551 \quad C_{Fo,x} = \frac{C_{Fi,x} * Q_{Fi,x}}{Q_{Fo,x}} \quad [7]$$

552

553 where, C_{Fi-x} is the feed solution inlet concentration, Q_{Fi-x} is the inlet flow rate of feed
 554 solution and Q_{Fo-x} is the outlet flow rate of feed solution. Q_{Fo-x} is equal to the
 555 difference between Q_{Fi-x} and Q_{p-x} . Compensating equation 7 in equation 6 gives:

556

$$557 \quad C_{Fb,x} = \frac{C_{Fi,x}(1 + \frac{Q_{Fi,x}}{Q_{Fo,x}})}{2} \quad [8]$$

558

559

560 Equations 5 and 8 calculate the bulk concentration of draw and feed solutions
 561 respectively; substituting equations 5 and 8 in equation 1 and using Van't Hoff
 562 equation for the osmotic pressure calculation:

563

$$564 \quad J_{w,x} = A_w \left\{ \frac{(nRT C_{Di,x} (1 + \frac{Q_{Di,x}}{Q_{Do,x}}) / 2) \exp\left(\frac{-J_{w,x}}{k_d}\right) - nRT C_{Fi,x} \left(1 - \frac{Q_{Fi,x}}{Q_{Fo,x}}\right) \exp\left(J_{w,x} K + \frac{J_{w,x}}{k_f}\right)}{1 + \frac{B}{J_{w,x}} \left(\exp\left(J_{w,x} \frac{J_{w,x}}{k_f}\right) - \exp\left(\frac{-J_{w,x}}{k_d}\right)\right)} - \Delta P \right\} \quad [9]$$

565 More information about the model used in calculating water flux in the PRO process
 566 can be found in literature [17].

567

568 *A2 Model validation:*

569

570 The computer model used in this study was validated using pilot plant data [21]. The
 571 hollow fibre PRO membrane has water permeability coefficient equal to 0.27
 572 L/m²h.bar and membrane area equal to 70.5 m² and 1.M NaCl and DI water draw
 573 and feed solution, respectively. Water flux calculated from the computer model, J_{w-m} ,
 574 was compared with the experimental flux, J_{w-exp} , data [Figure 5a-1, reference 21].
 575 Different draw solution flow rate (Q_{Ds}), feed solution flow rates (Q_{Fs}), draw solution
 576 pressure (P_{Ds}) and feed solution pressure (P_{Fs}) are used in the model validation.
 577 According to Table A1, there are good agreement between theoretical and
 578 experimental data, over 90%.

579

580 Table A1: Experimental and theoretical water flux from the pilot plant test at
 581 different draw feed solution flow rates, Q_{Ds} and Q_{Fs} respectively. Membrane
 582 structure parameter 1024 μ m and salt permeability coefficient 0.035 L/m²h.

P_{Ds} (bar)	P_{Fs} (bar)	Q_{Ds} (L/h)	Q_{Fs} (L/h)	J_{w-exp} (Lm ² /h)	J_{w-m} (Lm ² /h)	%Agreement
5	2.8	480	480	6	5.65	94.2
8	3.1			5.5	5.27	95.8
11.8	3.2			4.9	4.73	96.5

14.6	3.3			4.5	4.36	96.9
16	3.5			3.9	4.2	92.9
21.5	3.7			3.5	3.46	98.9
24	3.8			3.2	3.17	99.1
27.5	4.1			2.8	2.75	98.2
30	4.2			2.6	2.45	94.2
6.3	4	480	600	6.2	5.64	91.0
13	4.5			4.9	4.78	97.6
16	4.7			4.6	4.35	94.6
17.8	4.8			4.2	4.13	98.3
26	5.3			3.3	3.11	94.2

583

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