# UNIVERSITY OF TECHNOLOGY SYDNEY Faculty of Engineering and Information Technology

### NON-IID RECOMMENDER SYSTEMS: A MACHINE LEARNING APPROACH

by

#### Liang Hu

A Thesis Submitted in Partial Fulfillment of the Requirements for the Degree

Doctor of Philosophy

Sydney, Australia

Certificate of Original Authorship

I, Liang Hu declare that this thesis, submitted in fulfilment of the requirements

for the award of Doctor of Philosophy, in the Advanced Analytics Institute at the

University of Technology Sydney.

This thesis is wholly my own work unless otherwise reference or acknowledged. In

addition, I certify that all information sources and literature used are indicated in

the thesis.

This thesis is the result of a research candidature conducted jointly with Shanghai

Jiao Tong University as part of a collaborative Doctoral degree.

This document has not been submitted for qualifications at any other academic

institution.

This research is supported by an Australian Government Research Training Program

Scholarship.

**Production Note:** 

Signature removed Signature: prior to publication.

Date:

March 28, 2019

#### ABSTRACT

# NON-IID RECOMMENDER SYSTEMS: A MACHINE LEARNING APPROACH

by

#### Liang Hu

A recommender system (RS) comprises the core software, tools, and techniques that effectively and efficiently cope with information overload as well as locate information that is genuinely required. As one of the most widely used artificial intelligence (AI) systems, RSs have been integrated into daily life over the past two decades. In recent decade, the machine learning approach has dominated AI research in almost all areas. Therefore, modeling advanced RSs using the machine learning approach forms the basic methodology of this thesis.

Current RSs suffer from many problems, such as data sparsity and cold start, because they fail to consider the non-IIDness in data, which includes the heterogeneities and coupled relations within and between users and items, as well as their interactions. Thus, we propose non-IID recommender systems by modeling the non-IIDness in recommendation data with the machine learning approach. Specifically, we study non-IID RS modeling techniques from three perspectives: users, items, and interactions. This research not only promotes the design of new machine learning models and algorithms in theory, but also extensively influences the evolution of technology and society.

To construct the non-IID RS from a user perspective, we jointly model two aspects: (1) the heterogeneities of users and (2) the coupling between users. Specifically, we study the non-IID user modeling in two representative RSs: (1) a group-based RS (GBRS) and (2) a social network-based RS (SNRS). First, we perform an in-depth analysis of existing GBRSs and demonstrate their deficiencies in modeling

the heterogeneity and coupling between group members for making group decisions. A deep neural network is designed to learn a group preference representation, which jointly considers all members' heterogeneous preferences. Second, we model an SNRS by modeling the influential contexts that embed the influence of relevant users and items, because a user's selection is largely influenced by other users with social relationships.

To construct the non-IID RS from an item perspective, we target two modeling aspects: (1) the heterogeneities of items and (2) the coupling between items. Specifically, we study the non-IID item modeling in two representative RSs: (1) a cross-domain RS (CDRS) and (2) a session-based RS (SBRS). First, existing CDRSs may fail to conduct cross-domain transfer because of domain heterogeneity; thus, we propose an irregular tensor factorization model, which can more effectively capture the coupling between heterogeneous domains with learning the domain factors for each domain. Second, we construct an effective and efficient personalized SBRS to more effectively capture the couplings between items by modeling intra- and intersession contexts.

To construct the non-IID RS from an interaction perspective, we target two modeling aspects: (1) the heterogeneities of interactions and (2) the coupling between interactions. Specifically, we study the non-IID interaction modeling in two representative RSs: (1) a multi-objective RS (MORS) and (2) an attraction-based RS (ABRS). First, we study an MORS to tackle the challenges of recommendation for users and items in the long tail. Subsequently, a coupled regularization model is proposed to jointly optimize two objectives: the credibility and specialty. Existing content-based RSs can recommend new content according to similarity; however, they are not capable of interpreting the attraction points in user-item interactions. Therefore, to construct an interpretable content-based RS, we propose attraction modeling to learn and track user attractiveness.

In the last section, we summarize the contributions of our work and present the future directions that can improve and extend the non-IID RS.

## Dedication

To my parents, my wife, and my son.

#### Acknowledgements

Firstly, I would like to express my sincere gratitude to my supervisor Prof. Long-bing Cao for the continuous support of my Ph.D. study and related research, for his patience, motivation, and immense knowledge. His guidance helped me in all the time of research and writing of my research papers and this thesis. His advice on both research as well as on my career have been priceless. Prof. Longbing Cao shows strong motivation, ambition, and dedication in his work and research, which impressed me very much. Moreover, I'd like to thank my co-supervisor Prof. Guandong Xu. With his invitation, I first time came to Australia and visited Advanced Analytics Institute (AAi), University of Technology Sydney. His strong sociability shows me a great example of career development.

I would also like to thank my committee members, Professor Ling Chen, Professor Dong Xu, and Professor Jinyan Li for serving as my committee members even at hardship. I also want to thank you for letting my candidate assessment be an enjoyable moment, and for your brilliant comments and suggestions, thanks to you.

A special thanks to my family. Words cannot express how grateful I am to my mother, and father for all of the sacrifices that you have made on my behalf. Your prayer for me was what sustained me thus far. In the end, I would like express appreciation to my wife who was always my strongest back support. Thanks for her great efforts to and take care of my son. This thesis would not have been possible without their warm love, continued patience, and endless support.

I would like to thank all my lab mates for their continued support. I appreciate the discussion with Shoujin Wang, visiting Ph.D. student Xin Li and Sheng Luo, and visiting Professor Wenpeng Lu. Moreover, I thank all my coauthors in the lab, including Shoujin Wang, Qianqian Chen and Wei Cao. Especially, I'd like to thank Songlei Jian for coauthoring top-rank papers and co-tutoring in top-rank

conferences. I am impressed by her brilliance, diligence, optimism and great comprehension, and we got a lot of inspirations from our discussion. I hope all of them have a happy life and successful career.

Last but not least, there are still many other people that I would like to express my gratitude to them for their contribution during my Ph.D. study.

> Liang Hu Sydney, Australia, 2018.

#### List of Publications

#### Journal Papers

- J-1. Hu, L., Chen, Q, Jian, S., Cao, L., and Cao, J. Neural Cross-session Filtering: Next-item Prediction under Intra- and Inter-session Context. IEEE Intellegent System, vol. 33, pp. 57-67, 2018.
- J-2. Hu, L., Cao, L., Cao, J., Gu, Z., Xu, G., and Wang, J. Improving the Quality of Recommendations for Users and Items in the Tail of Distribution. ACM Trans. Inf. Syst. 35, 3, 1-37, 2017.
- J-3. Hu, L., Cao, L., Cao, J., Gu, Z., Xu, G., and Yang, D. Learning Informative Priors from Heterogeneous Domains to Improve Recommendation in Cold-Start User Domains. ACM Trans. Inf. Syst. 35, 2, 1-37, 2016.
- J-4. Hu, L., Cao, J., and Gu, Z. . Service Discovery and Recommendation in Rough Hierarchical Granular Space. Advanced Science Letters, 7(1), 135-139, 2012.
- J-5. Yang, D., Guo, J., Wang, Z.-J., Wang, Y., Zhang, J., Hu, L., Yin, J., and Cao, J. FastPM: An approach to pattern matching via distributed stream processing. Information Sciences 453, 263-280, 2018.
- J-6. Cao, J., Xu, W., Hu, L., Wang, J. and Li, M.. A social-aware service recommendation approach for mashup creation. International Journal of Web Services Research (IJWSR), 10(1), pp.53-72, 2013.
- J-7. Hu, L., Jian, S., Cao, L., and Chen, Q.. Attraction Modeling: Enhancing Content-based Recommender Systems with Statistical Interpretability. (To be submit to AIJ)

#### Conference Papers

- C-1. Hu, L., Jian, S., Cao, L., Chen, Q., and Z. Gu, "HERS: Modeling Influential Contexts with Heterogeneous Relations for Sparse and Cold-start Recommendation," in AAAI-19, 2019.
- C-2. Hu, L., Jian, S., Cao, L., and Chen, Q. Interpretable Recommendation via Attraction Modeling: Learning Multilevel Attractiveness over Multimodal Movie Contents. In Proceedings of the Twenty-Seventh International Joint Conference on Artificial Intelligence, IJCAI-18, 3400-3406, 2018.
- C-3. Hu, L., Cao, L., Wang, S., Xu, G., Cao, J., and Gu, Z. Diversifying Personalized Recommendation with User-session Context. In Proceedings of the Twenty-Sixth International Joint Conference on Artificial Intelligence, IJCAI-17, 1858–1864, 2017.
- C-4. Hu, L., Cao, W., Cao, J., Xu, G., Cao, L., and Gu, Z. Bayesian Heteroskedastic Choice Modeling on Non-identically Distributed Linkages. In Data Mining (ICDM), 2014 IEEE International Conference on, 851-856, 2014.
- C-5. Hu, L., Cao, J., Xu, G., Cao, L., Gu, Z., and Cao, W. Deep Modeling of Group Preferences for Group-Based Recommendation. In Twenty-Eighth AAAI Conference on Artificial Intelligence, 1861-1867, 2014.
- C-6. Hu, L., Cao, J., Xu, G., Cao, L., Gu, Z. and Zhu, C. Personalized recommendation via cross-domain triadic factorization. In Proceedings of the 22nd international conference on World Wide Web (pp. 595-606). ACM, 2013.
- C-7. Hu, L., Cao, J., Xu, G., Wang, J., Gu, Z. and Cao, L. Cross-domain collaborative filtering via bilinear multilevel analysis. In International Joint Conference on Artificial Intelligence. IJCAI-13, 2013.
- C-8. Hu, L., Cao, J., Xu, G. and Gu, Z.. Latent Informative Links Detection. In KES (pp. 1233-1242), 2012.
- C-9. Hu, L., Cao, J. and Gu, Z.. Service Discovery and Recommendation in Rough Hierarchical Granular Computing. In Services Computing Conference (AP-SCC), 2010 IEEE Asia-Pacific (pp. 191-198). IEEE, 2010, December.

- C-10. Jian, S., Hu, L., Cao, L., Lu, K., and Gao H., "Evolutionarily Learning Multi-aspect Interactions and Influences from Network Structure and Node Content," in AAAI-19, 2019.
- C-11. Jian, S., Hu, L., Cao, L., and Lu, K. Metric-Based Auto-Instructor for Learning Mixed Data Representation. In AAAI-18, 2018.
- C-12. Wang, S., Hu, L., Cao, L., Huang, X., Lian, D. and Liu, W.. Attention-based transactional context embedding for next-item recommendation. AAAI, 2018.
- C-13. Wang, S., Hu, L., and Cao, L. Perceiving the Next Choice with Comprehensive Transaction Embeddings for Online Recommendation. In Machine Learning and Knowledge Discovery in Databases: European Conference, ECML PKDD 2017, Skopje, Macedonia, September 1822, 2017.
- C-14. Cao, W., Hu, L., and Cao, L. Deep Modeling Complex Couplings within Financial Markets. In Proceedings of the Twenty-Ninth AAAI Conference on Artificial Intelligence, 2518-2524, 2015.
- C-15. Chen, Q., Hu, L., Xu, J., Liu, W., and Cao, L. Document similarity analysis via involving both explicit and implicit semantic couplings. In Data Science and Advanced Analytics (DSAA), 2015. 36678 2015. IEEE International Conference on, 1-10, 2015.
- C-16. Xu, W., Cao, J., Hu, L., Wang, J. and Li, M., June. A social-aware service recommendation approach for mashup creation. In 2013 IEEE 20th International Conference on Web Services (pp. 107-114). IEEE, 2013.
- C-17. You, Y., Huang, G., Cao, J., Chen, E., He, J., Zhang, Y. and Hu, L.. Geam: A general and event-related aspects model for twitter event detection. In International Conference on Web Information Systems Engineering (pp. 319-332). Springer, Berlin, Heidelberg, 2013, October.
- C-18. Shangguan, Q., Hu, L., Cao, J. and Xu, G.. Book Recommendation Based on Joint Multi-relational Model. In Cloud and Green Computing (CGC), 2012 Second International Conference on (pp. 523-530). IEEE, 2012, November.

### Contents

	Cert	tificate		ii			
	Abs	Abstract					
	Ded	ication		V			
	Ack	nowledg	gments	vi			
	List	of Pub	lications	viii			
	List	of Figu	ıres	xxi			
	Abb	reviatio	on	xxvi			
	Nota	ation	X	xviii			
[	Re	esearc	ch Background	1			
1	Intr	roducti	ion	2			
	1.1	Backg	ground	. 3			
		1.1.1	Recommender Systems	. 4			
		1.1.2	Recommendation Data Modeling with Machine Learning	8			
	1.2	Challe	enges in Modeling RSs	. 11			
		1.2.1	Challenges from Data Characteristics	. 11			
		1.2.2	Challenges from User Behavior	12			
		1.2.3	Challenges from Information Coupling	. 14			
	1.3	Resear	rch Objectives	15			
		1.3.1	Non-IID Modeling Aspects on Recommendation Data	. 16			

X1	1

		1.3.2	Non-IID RS Modeling	19
	1.4	Thesis	Organization	28
2	Lite	rature	Survey	31
	2.1	Basic 1	Recommendation Techniques	31
		2.1.1	CF	31
		2.1.2	CBF	34
		2.1.3	Hybrid CF and CBF	38
	2.2	Model	ing Implicit Feedback and Long-tail Distribution	40
		2.2.1	Implicit Feedback	40
		2.2.2	Long Tail	41
	2.3	SNRSs	3	42
		2.3.1	Summary of the Challenges to Target in an SNRS	43
		2.3.2	Social Media Data	44
		2.3.3	Trust Relation Modeling	44
		2.3.4	Deep Learning Models	45
	2.4	GBRS	S	46
		2.4.1	Summary of the Challenges to Target in GBRSs	46
		2.4.2	Aggregation Approach	46
		2.4.3	Deep Learning Approach	48
	2.5	CDRS	S	48
		2.5.1	Summary of the Challenges to Target in CDRSs	49
		2.5.2	Latent Factor Models	50
		2.5.3	Deep Learning Models	51
	2.6	SBRSs	5	52

		2.6.1	Summary of the Challenges to Target in SBRSs	53
		2.6.2	Markov Models	53
		2.6.3	Deep Learning Models	54
	2.7	MORS	Ss	55
		2.7.1	Summary of the Challenges to Target in MORSs	56
		2.7.2	Multi-criteria Ratings	56
		2.7.3	Multi-objective Ranking	57
3	Pre	limina	ries	<b>6</b> 0
	3.1	Neighl	porhood Method	60
	3.2	Latent	Factor Models	60
		3.2.1	Matrix Factorization	60
		3.2.2	Tensor Factorization	62
	3.3	Deep 1	Learning Models	64
		3.3.1	Restricted Boltzmann Machines	64
		3.3.2	Recurrent Neural Networks	65
	3.4	Evalua	ation Metrics	68
		3.4.1	Rating Prediction	68
		3.4.2	Ranking Prediction	69
		3.4.3	Diversity	70
	3.5	Baselin	ne Methods for Experiments	70
		3.5.1	Heuristic Methods	71
		3.5.2	CF Methods	71
		3.5.3	Factorization Machines	71
		3.5.4	Content-based Methods	71

				xiv
		3.5.5	Relation-based Method	72
		3.5.6	Session Methods	72
		3.5.7	Cross-domain Methods	72
II	N	on-II	D RS: Modeling Non-IIDness on Users	73
4	A C	Froup-	based Recommender System for Modeling Group	
	Pre	ference	e over Member Decisions	74
	4.1	Introd	uction	74
	4.2	Proble	em Formulation	76
	4.3	Model	and Inference	77
		4.3.1	Disentangling Collective and Individual Embedding	77
		4.3.2	A Comprehensive Representation of Group Preferences	80
		4.3.3	Recommendation for a Group	83
	4.4	Exper	iments	83
		4.4.1	Data Preparation	84
		4.4.2	Comparison Methods	84
		4.4.3	Results	85
	4.5	Summ	ary of Contributions	89
5	A S	ocial N	Network-based Recommender Systems for Modeling	
			Item Influential Contexts	90
	5.1	Introd	uction	90
	5.2	Proble	em Formulation	93
	5.3	Model	and Learning	94
		5.3.1	Architecture	94

		5.3.2	Influential-context Aggregation Unit	. 95
		5.3.3	User's Influential Context Embedding	. 96
		5.3.4	Item's Influential Context Embedding	. 99
		5.3.5	User-item Interaction Ranking	. 100
		5.3.6	Training Procedure	. 101
	5.4	Exper	iments	. 101
		5.4.1	Data Preparation	. 102
		5.4.2	Experimental Settings	. 103
		5.4.3	Recommendation Performance	. 104
		5.4.4	Recommendation for Cold-start Users and Items	. 106
		5.4.5	Visualization and Interpretation	. 108
	5.5	Summ	nary of Contributions	. 108
Π	I I	Von-I	ID RS: Modeling Non-IIDness on Items	
		1011 1	ID Its. Wodering Non-IID less on Items	111
6	AC		lomain Recommender System for Modeling the	111
3		Cross-d	G	111
6		Cross-d	lomain Recommender System for Modeling the	112
6	Cou	Cross-d	domain Recommender System for Modeling the over Heterogeneous Item Domains	<b>112</b> . 112
6	Cou	Cross-d  iplings  Introd	domain Recommender System for Modeling the over Heterogeneous Item Domains	112 . 112 . 113
6	Cou	Cross-d uplings Introd 6.1.1	domain Recommender System for Modeling the over Heterogeneous Item Domains  duction	112 . 112 . 113 . 116
6	Cou	Eross-d iplings Introd 6.1.1 6.1.2 6.1.3	domain Recommender System for Modeling the over Heterogeneous Item Domains  duction	112 . 112 . 113 . 116 . 116
6	6.1	Eross-d iplings Introd 6.1.1 6.1.2 6.1.3	domain Recommender System for Modeling the over Heterogeneous Item Domains  duction	112 . 112 . 113 . 116 . 116 . 118
6	6.1	Eross-diplings Introd 6.1.1 6.1.2 6.1.3 Proble	domain Recommender System for Modeling the over Heterogeneous Item Domains  duction	112 . 112 . 113 . 116 . 118 . 118

	6.3	Weigh	ted Irregular Tensor Factorization	. 121
		6.3.1	Transformation	. 121
		6.3.2	Parameter Learning	. 125
		6.3.3	Weight Matrix Configuration	. 128
	6.4	Remai	rks	. 131
		6.4.1	Tricks on Sparse Weight Matrices for Complexity Reduction	. 131
		6.4.2	Training with Additional Noisy Examples for Improving	
			Generalization	. 132
		6.4.3	Post-Learning	. 134
	6.5	Exper	iments	. 135
		6.5.1	Comparison Methods	. 135
		6.5.2	Evaluation Metric	. 137
		6.5.3	Rating Prediction on Epinions.com	. 137
		6.5.4	Click Prediction on Tmall.com	. 144
		6.5.5	Time Period as Domain on Movie Rating Prediction	. 153
	6.6	Summ	nary of Contributions	. 158
7	AS	ession.	-based Recommender System for Modeling the Intra-	
•			sessions Context	161
	7.1	Introd	luction	. 161
	7.2		em Formulation	
	7.3		l Cross-session Filtering	
	1.5	7.3.1	Historical Session Encoding	
		7.3.2	Current Session Encoding	
		7.3.3	Intra- and Inter-session Context Encoding	. 167

			XV	/ii
		7.3.4	Objective Function	37
		7.3.5	Learning and Prediction	38
	7.4	Empir	ical Study	39
		7.4.1	Data Preparation	39
		7.4.2	Comparison Methods	70
		7.4.3	Diversity Evaluation	73
	7.5	Summ	ary of Contributions	76
8 8			ID RS: Modeling Non-IIDness on Interactions17 bjective Recommender System for Modeling Specialty	7
	and	Credi	bility for Long-tail Recommendation 17	78
	8.1	Introd	uction	78
		8.1.1	Challenges of Tail Users and Items	<b>7</b> 9
		8.1.2	Optimizing Specialty and Credibility	32
	8.2	Prelin	ninaries	35
		8.2.1	Reputation Modeling	35
		8.2.2	Explicit and Implicit Rating	39
	8.3	Model	and Learning	<del>9</del> 0
		8.3.1	Overview of RMRM	<del>9</del> 0
		8.3.2	Learning Regularized C-HMF Model	94
		8.3.3	Learning Regularized S-HMF Model	)3
	8.4	Algori	thm and Prediction	)6
	8.5	Discus	ssion	)9

				xviii
		8.5.2	Social Regularization from PoGE Perspective	. 210
	8.6	Exper	iments	. 211
		8.6.1	A Comparison of the State-of-the-Art Methods	. 212
		8.6.2	Explicit Rating Data Evaluation	. 213
		8.6.3	Implicit Rating Data Evaluation	. 223
	8.7	Summ	nary of Contributions	. 228
9	Att	raction	n-based Recommender Systems for Capturing and	
			ng User Attraction in Content	231
	9.1	Introd	luction	. 231
	9.2	Attrac	etion Model	. 234
		9.2.1	Content Representation Module	. 235
		9.2.2	Attraction Filter Module	. 236
		9.2.3	Attractiveness Score Module	. 237
	9.3	Hierar	chical Attraction Model on Textual Content	. 238
		9.3.1	Multilevel Attraction	. 239
		9.3.2	Bidirectional Gated Recurrent Units	. 239
		9.3.3	Model Architecture	. 240
		9.3.4	Multilevel Attraction Filters	. 241
		9.3.5	Hierarchical Attractive Content Encoder	. 243
		9.3.6	Objectives and Parameter Learning	. 246
	9.4	Multin	modal Attraction Model on Movies	. 247
		9.4.1	Multimodal Attraction	. 249
		9.4.2	Model Architecture	. 249

9.4.3

$x_1$	X

		9.4.4	Cast Attraction Module	
		9.4.5	Multimodal Movie Attraction Scoring	
		9.4.6	Objective and Parameter Learning	
	9.5	Experi	ments	
		9.5.1	Comparison Methods	
		9.5.2	Attraction on Books for Classification	
		9.5.3	Attraction on Academic Papers for Ranking	
		9.5.4	Multimodal Attraction on Movies	
	9.6	Summ	ary of Contributions	
$\mathbf{V}$	Sı	ımma	ary and Prospect 273	
10	Con	clusio	n 274	
	10.1	Non-II	D RS Modeling on Users	
		10.1.1	GBRS Modeling: Learning Comprehensive Group Preference Representation	
		10.1.2	SNRS Modeling: Learning Comprehensive Group Preference	
			Representation	
	10.2	Non-II	D Recommender Systems Modeling on Items	
		10.2.1	CDRS Modeling: Leveraging Knowledge Across	
			Heterogeneous Domains	
		10.2.2	SBRS Modeling: Modeling Selection with Influential Users	
			and Items	
	10.3	Non-II	D RS Modeling on Complex Interaction	
		10.3.1	MORS Modeling: Optimizing Credibility and Novelty for	
			Long-tail Recommendation	

10.3.2 ABRS Modeling: Capturing and Interpreting Attraction	
Points in Content	278
11 Open Challenges and Future Directions	279
11.1 New Evaluation Methods and Metrics	279
11.2 SNRSs	280
11.3 GBRSs	281
11.4 CDRSs	282
11.5 SBRSs	283
11.6 MORSs	284
11.7 ABRSs	285
11.8 Unified and Ubiquitous RSs	286
Bibliography	288

# List of Figures

1.1 Overview of the non-IID RSs targeted in this thesis. Each mode		
	item for these systems is marked with one or two icons. Each icon	
	corresponds to one non-IID modeling aspect shown in the	
	right-hand section	20
1.2	Overview of machine learning methods used to model non-IID RSs	
	in this thesis. Each listed item for these systems is marked with one	
	or two icons. Each icon corresponds to one machine learning	
	approach listed in the right-hand section	21
3.1	The demonstration of CP factorization on a third-order tensor $\dots$	63
3.2	2 The structure of restricted Boltzmann machine	
3.3	B Long short-term memory [161]	
3.4	4 Gated recurrent unit	
4.1	Left: Overview of the two-layer collective DBN used to disentangle	
	high-level collective and individual embeddings. Right: More	
	detailed structure of the collective RBM at the top layer where the	
	collective embedding is connected to the member embedding w.r.t.	
	each member	78
4.2	A dual-wing RBM is placed on the top of DBN, which jointly	
	models the group choices and collective embedding to learn the	
	comprehensive embedding of group preference	81

4.3	MAP w.r.t. 2-member groups vs. 2 <sup>+</sup> -member groups 88	
5.1	A multi-relational RS consists of user-user relation, user-item relation and item-item relation. Each user-item interaction is influenced by the user context and the item context	
5.2	The architecture of ICE-MRS for modeling user's and item's influential contexts	
5.3	Influential-context Aggregation Unit (ICAU): A two-stage aggregation model to construct influential context embedding (ICE) . 97	
5.4	Item recommendation for cold-start users of Delicious and Lastfm 107	
5.5	User recommendation for cold-start items of Delicious and Lastfm 108	
5.6	The visualization of influential contexts of a sampled user selection on an artist in the Lastfm dataset. The artists in item network are labeled by their names and the anonymous users in user network are labeled with IDs. The thickness of edges specifies the significance of influence	
6.1	Demonstration of the occurrence of the blinder-transfer issue in CDMF114	
6.2	The feedback from the majority of users in each domain is scant due to the power law distribution, and users have different unfamiliar domains due to differences in interests	
6.3	Irregular triadic relation and regular triadic relation	
6.4	WITF transforms the slices with heterogeneous domain-specific items into a regular third-order tensor containing an identical virtual item set	
6.5	Rating distributions of items on Kids & Family and Hotel & Travel show obvious long tails	
6.6	RMSEs comparison over user groups with different number of ratings. 141	

6.7	RMSEs comparison over different number of noisy examples for each			
	user			
6.8	Mean APs over different values of confidence parameter c			
6.9	Recall@5 $\sim$ 20 of comparison methods on target domain D1 and D2 151			
6.10	Time period as domain to model the heterogeneities of user			
	preferences on movies			
6.11	MAE comparison with $\alpha_k$ increasing			
7.1	The motivation of this work: (a) Classic recommendation without considering session context; (b) Two sequences adding milk and			
	bread into the cart; (c) Rigid-order session vs. relaxed-order session;			
	(d) First-order Markov chain model vs. recurrent model; (e) Next			
	item prediction based on both intra- and inter-session contexts 162			
7.2	The architecture of NCSF. In the left part of split line, historical			
	sessions are used to build inter-session context. In the right part of			
	split line, the items in the current session are used to build			
	intra-session context			
7.3	REC@5 - REC@50 on test cases $LAST$ and $LOO$			
7.4	F1 scores on test cases $LAST$ and $LOO$			
8.1	Items (left) and users (right) are ranked by the number of their			
	ratings (truncated from 0 to 100) on Rich Epinions Dataset; they			
	are both clearly distributed with short heads and long tails 180			
8.2	A recurrent mutual regularization process couples S-HMF and			
	C-HMF using the user and item-factors learned from one another as			
	the empirical priors to couple the objectives specialty and credibility. 185			

8.3	The screen snapshots of reviews from Amazon.com (left) and Ciao.com (right), where the red, dotted boxes show the helpfulness		
	score		
8.4	The graphical representation of the RMRM framework, where S-HMF and C-HMF are recurrently regularized by the empirical priors, induced from one another		
8.5	The geometric illustration of the recurrent mutual regularization process, where the estimates of S-HMF and C-HMF are recurrently regularized by the empirical priors induced from one another		
8.6	Long-tail distributions for the number of ratings of items and users (truncated from 0 to 500)		
8.7	The distributions for the number of helpful scores w.r.t. items and users (truncated from 0 to 200)		
8.8	MAEs of rating prediction for the long-tail item distribution		
8.9	MAEs of rating prediction for the long-tail user distribution 218		
8.10	0 MAEs varying the numbers of involved (a) user trusters, and (b) system experts		
8.11	MAEs for head items and tail items with shilling attack		
8.12	Long-tail distributions over the number installations w.r.t. users and items (truncated)		
8.13	Recall@20-50 of tail-item recommendations for users		
8.14	Recall@20-50 of tail-user recommendations for users		
9.1	Users with different background may have quite different attractive points on an article [199]		
9.2	Architecture of Attraction Model		
9.3	The architecture of hierarchical attraction model		

9.4	The architecture of hierarchical attraction model over movies with
	two modalities: Cast (left) and Story (right)
9.5	Attractiveness visualization on the abstract of <i>Invitation to the</i>
	Game w.r.t. sentences and words in the most attractive sentences
	for two users. The larger size and deeper color of font denotes the
	larger attractiveness weight is assigned
9.6	Recall@5-50 on the Published Paper testing set and the New Paper
	testing set
9.7	Demonstration of the different of group attraction on the abstract of
	the paper Exploring complex networks. We list the most attractive
	word in each sentence for each group to illustrate their difference. $$ . $$ 266
9.8	Demonstration of two exemplary users' most attractive papers in
	the testing set. We list the most attractive word in each sentence of
	the recommended papers for interpretation
9.9	R@5-50 on the Released Movies and the New Movies
9.10	Two comparative testing samples of <i>User 182</i> : the left movie <i>Wild</i>
	America obtains a high attraction score because of the cast
	members in red appear in user's watched movies while the cast
	members of <i>Bogus</i> never appear in user's movie list
9.11	Statistical attractiveness on movie <i>Election (1999)</i> w.r.t. sentences,
	words in the most attractive sentences and cast members from the
	perspectives of User 156 and User 2163. The larger size and deeper
	color of font denote the larger attractiveness weight is assigned 271

#### Abbreviation

RS - Recommender System	RS -	Recommender	Systen
-------------------------	------	-------------	--------

- AI Artificial Intelligence
- CF Collaborative Filtering
- CBF Context-based Filtering
- NLP Natural Language Processing
- CV Computer Vision
- CNN Convolutional Neural Networks
- RNN Recurrent Neural Networks
- TSA Time Series Analysis
- CDRS Cross-domain Recommender Systems
- SNRS Social Network-based Recommender Systems
- CARS Context-aware Recommender Systems
- MORS Multi-objective Recommender Systems
- SBRS Session-based Recommender Systems
- GBRS Gruop-based Recommender Systems
- ABRS Attraction-based Recommender Systems
- MF Matrix Factorization
- TF Tensor Factorization
- RBM Restricted Boltzmann Machines
- GRU Gated Recurrent Units
- LSTM Long Short-Term Memory
- MAE Mean Absolute Error
- RMSE Root Mean Square Error

AP - Average Precision

MRR - Mean Reciprocal Rank

nDCG - Normalized Discounted Cumulative Gain

AUC - Area Under the ROC Curve

# Nomenclature and Notation

$(.)^{\top}$ denotes the transpose operation.
${f I}$ is the identity matrix.
$\mathbb{R}$ , $\mathbb{R}^+$ denote the field of real numbers, and the set of positive reals, respectively
$\mathcal X$ denotes a tensor (boldface script letter)
$\mathcal{X}^{I \times J \times K}$ denotes The dimensionality of each mode
${f X}$ denotes a matrix (boldface capital letter)
$\mathbf{X}_{i,:}$ denotes the <i>i</i> th row of matrix $\mathbf{X}$
$\mathbf{X}_{:,j}$ denotes the $j$ th column of matrix $\mathbf{X}$
$\mathbf{X}_{i,j}$ denotes the entry $(i,j)$ of matrix $\mathbf{X}$
${\bf x}$ denotes a vector (boldface lower-case letter)
$\mathbf{X}_{(n)}$ denotes mode-n matricization of a tensor
$\otimes$ denotes Kronecker product
⊙ denotes Khatri-Rao product
$\cdot^*$ denotes Hadamard product
./ denotes element-wise division
o denotes outer product

 $\|\mathcal{X}\|$  denotes the norm of a matrix or a tensor  $\mathcal{X}$ 

 $\mathcal{X} = [\![\mathbf{A},\mathbf{B},\mathbf{C}]\!]$  denotes the factorization form of a tensor

 $vec\mathbf{X}$  denotes vectorization of matrix