# Performance Analysis of Dense Small Cell Networks

Tian Ding

Doctor Degree

University of Technology Sydney

Faculty of Engineering and Information Technology

2019

CERTIFICATE OF ORIGINAL AUTHORSHIP

I, Tian Ding declare that this thesis, is submitted in fulfilment of the requirements for the

award of Doctor degree, in the School of Electrical and Data Engineering at the University

of Technology Sydney.

This thesis is wholly my own work unless otherwise reference or acknowledged. In

addition, I certify that all information sources and literature used are indicated in the thesis.

This document has not been submitted for qualifications at any other academic institution.

This research is supported by the Australian Government Research Training Program.

Signature: Production Note: Signature removed prior to publication.

June 04, 2019 Date:

## ACKNOWLEDGMENT

First I would like to express my sincerest gratitude to my principal supervisor Prof. Guoqiang Mao, for his encouragement and support. I would like to thank Dr. Ming Ding for his help in my research work. I would like to thank my parents for their love. I would like to thank the Graduate Research School and the School of Electrical and Data Engineering at the University of Technology Sydney for providing a favorable environment. Finally, I would like to thank the Faculty of Engineering and Information Technology at the University of Technology Sydney and the Australian Government for the financial support.

# THESIS FORMAT STATEMENT

This thesis is in the format of the Conventional thesis.

## **PUBLICATIONS**

- [J2] T. Ding, M. Ding, G. Mao, Z. Lin, A. Y. Zomaya and D. López-Pérez, "Performance Analysis of Dense Small Cell Networks With Dynamic TDD," in IEEE Transactions on Vehicular Technology, vol. 67, no. 10, pp. 9816-9830, Oct. 2018.
- [J1] T. Ding, M. Ding, G. Mao, Z. Lin, D. López-Pérez and A. Y. Zomaya, "Uplink Performance Analysis of Dense Cellular Networks With LoS and NLoS Transmissions," in IEEE Transactions on Wireless Communications, vol. 16, no. 4, pp. 2601-2613, April 2017.
- [C2] T. Ding, M. Ding and G. Mao, "MAC Layer Performance Analysis of Dense Small Cell Networks with Full Duplex", in 2018 24th Asia-Pacific Conference on Communications (APCC), pp. 1–5, November 2018, Invited Paper.
- [C1] T. Ding, M. Ding, G. Mao, Z. Lin, and D. López-Pérez, "Uplink Performance Analysis of Dense Cellular Networks With LoS and NLoS Transmissions," in 2016 IEEE International Conference on Communications (ICC), pp. 1–6, May 2016.

#### Abstract

It is envisaged that 5G wireless communications will embrace dense small cell networks (SCNs), which can achieve a high spatial reuse gain, further leading to a high network capacity. In this Thesis, I firstly analyse the coverage probability and the area spectral efficiency (ASE) for the uplink (UL) of dense SCNs considering a practical path loss model incorporating both lineof-sight (LoS) and non-line-of-sight (NLoS) transmissions. Compared with the existing work, I adopt the following novel approaches in my study: (i) I assume a practical user association strategy (UAS) based on the smallest path loss, or equivalently the strongest received signal strength; (ii) I model the positions of both base stations (BSs) and the user equipments (UEs) as two independent Homogeneous Poisson point processes (HPPPs); and (iii) the correlation of BSs' and UEs' positions is considered, thus making my analytical results more accurate. The performance impact of LoS and NLoS transmissions on the ASE for the UL of dense SCNs is shown to be significant, both quantitatively and qualitatively, compared with existing work that does not differentiate LoS and NLoS transmissions. Moreover, SCNs are envisioned to embrace dynamic time division duplexing (TDD) in order to tailor downlink (DL)/UL subframe resources to quick variations and burstiness of DL/UL traffic. The study of dynamic TDD is particularly important because it serves as the predecessor of the full duplex (FD) transmission technology. In this Thesis, I secondly study the performance of the dense SCNs with synchronous dynamic TDD, which has been widely adopted in the existing 4th-generation (4G) systems. I analyse the coverage probability and the ASE in the DL and UL of dense SCNs considering the synchronous dynamic TDD transmissions, and the performance impact of dynamic TDD transmissions on the ASE in the DL and UL of dense SCNs is discussed. Moreover, the performance impact of interference cancellation (IC) is also explored. Furthermore, SCNs are envisaged to embrace the FD transmission technology in order to increase the spectral efficiency of wireless systems. In this Thesis, I thirdly consider the FD communications in a practical SCN scenario, where BSs can select FD or half-duplex (HD) mode according to the real-time DL/UL traffic. I present analytical results on the probabilities of BS mode selection, which match the simulation results well. The analytical results in this Thesis shed new light on the performance of future 5th-generation (5G) dense SCNs.

# CONTENTS

Ι	Introdu	uction		1
II	Literature Review			7
	II-A	UL of D	ense SCNs	7
	II-B	Dense SCNs with Dynamic TDD		
	II-C	Dense So	CNs with Full Duplex	10
Ш	Perfori	nance An	alysis for the UL of Dense SCNs	12
	III-A	System I	Model	12
	III-B	Analysis	Based on the Proposed Path Loss Model	14
	III-C Study of A 3GPP Special Case		A 3GPP Special Case	16
		III-C1	The Result of $T_1^{\rm L}$	17
		III-C2	The Result of $T_1^{\rm NL}$	20
		III-C3	The Result of $T_2^L$	21
		III-C4	The Result of $T_2^{\rm NL}$	22
		III-C5	Evaluation Using the Gauss-Laguerre Quadrature	22
	III-D	Simulation	on and Discussion	23
		III-D1	Validation of the Analytical Results of $P^{\mathrm{cov}}\left(\lambda,T\right)$	24
		III-D2	The Results of $P^{\mathrm{cov}}\left(\lambda,T\right)$ vs. $\lambda$	26
		III-D3	The Results of $A^{\mathrm{ASE}}(\lambda, T_0)$ vs. $\lambda$	27
		III-D4	Discussion on Various Values of $\alpha^L$	29
		III-D5	Investigation of a Different Path Loss Model	31
		III-D6	Investigation of the Performance Impact of Ricean Fading	32
	III-E	Conclusi	on	33
IV	Perfori	nance An	alysis of Dense SCNs with Dynamic TDD	34
	IV-A	System Model		34
		IV-A1	General Network Scenario	34

36

		IV-A3	Performance Metrics	37
	IV-B	Main Res	ults of the MAC Layer Analysis	39
		IV-B1	The Distribution of the UE Number in an active BS: A	
			Truncated Negative Binomial Distribution	40
		IV-B2	The Distribution of the DL/UL Data Request Number in	
			an Active BS: A Binomial Distribution	41
		IV-B3	The Distribution of the DL/UL Subframe Number with	
			Dynamic TDD: An Aggregated Binomial Distribution	42
		IV-B4	The Subframe Dependent DL/UL TRU	43
		IV-B5	The Probabilities of Inter-Cell Inter-Link Interference	43
		IV-B6	The Average DL/UL/Total TRU	45
	IV-C	Main Res	ults of the PHY Layer Analysis	46
		IV-C1	Coverage Probability without Interference Cancellation	47
		IV-C2	Coverage Probability with Interference Cancellation	49
		IV-C3	Study of A 3GPP Special Case	50
	IV-D	Simulation	n Results	50
		IV-D1	Validation of the Results on the Probabilities of Inter-Cell	
			Inter-Link Interference	51
		IV-D2	Validation of the Results on the Time Resource Utilization	52
		IV-D3	Validation of the Analytical Results of $p^{\mathrm{cov},Link}\left(\lambda,\gamma\right)$	53
		IV-D4	The ASE Performance	55
	IV-E	Conclusio	on	58
V	Perform	nance Ana	lysis of Dense SCNs with Full Duplex	59
	V-A	System M	Iodel	59
		V-A1	Network Scenario	59
		V-A2	BS Mode Selection	59
		V-A3	Performance Metrics	61

IV-A2

	V-B	Main Resi	ults of MAC Layer Analysis	61
		V-B1	The Distribution of the UE Number in an Active BS	61
		V-B2	The Distribution of the Data Request Number in an Active	
			BS: A Multinomial Distribution	63
		V-B3	The Distribution of the Mode Selection in an Active BS .	64
	V-C	Simulation	and Discussion	65
		V-C1	Validation of the Results on the MAC Layer Analysis	65
		V-C2	Discussion of the Performance Impact of FD UE Ratio $p^{\rm FU}$	66
		V-C3	Discussion of the Performance Impact of FD Data Request	
			Probability	67
		V-C4	Discussion of the Performance Impact of UE Density $\boldsymbol{\rho}$ .	68
	V-D	Conclusio	n	69
VI	Conclus	sion		70
Refer	References			82

# LIST OF FIGURES

1	The coverage probability $P^{\text{cov}}(\lambda, T)$ vs. the SINR threshold in [4] with $\lambda =$	
	$10\mathrm{BSs/km^2},\ \alpha=3.75,\ \mathrm{and}\ \epsilon=0.7.\ \ldots$	24
2	The coverage probability $P^{\mathrm{cov}}\left(\lambda,T\right)$ vs. the SINR threshold with $\lambda=10\mathrm{BSs/km^2}$	
	and $\lambda = 10^3\mathrm{BSs/km^2}$	25
3	The coverage probability $P^{\mathrm{cov}}\left(\lambda,T\right)$ vs. the BS density with different $\epsilon$ and	
	SINR threshold $T=0$ dB	27
4	Area spectral efficiency $A^{\mathrm{ASE}}\left(\lambda,T_{0}\right)$ vs. the BS density with different $\epsilon$ and	
	SINR threshold $T_0=0$ dB. $\lambda_0$ and $\lambda_1$ correspond to the BS density when the	
	ASE given by the proposed analysis starts to suffer from a slow growth and	
	when it starts to pick up the growth, respectively	28
5	The coverage probability $P^{\mathrm{cov}}\left(\lambda,T\right)$ vs. the BS density with different $\epsilon$ and	
	$\alpha^{\rm L}$ . SINR threshold $T=0$ dB	30
6	Area spectral efficiency $A^{\mathrm{ASE}}\left(\lambda,T_{0}\right)$ vs. the BS density with the exponential	
	LoS probability model, different $\epsilon$ and SINR threshold $T_0=0$ dB	31
7	Area spectral efficiency $A^{\mathrm{ASE}}\left(\lambda,T_{0}\right)$ vs. the BS density with the linear LoS	
	probability model, different $\epsilon$ and SINR threshold $T_0=0$ dB, including the	
	Ricean fading.	32
8	Dynamic TDD scenarios	35
9	An example of the LTE TDD configurations. ('D' and 'U' denote a DL	
	subframe and an UL one, respectively.)	37
10	The probability of inter-cell inter-link interference	51
11	The average DL/UL TRU $\kappa^D$ and $\kappa^U.$	52
12	The DL coverage probability $p^{\mathrm{cov,D}}\left(\lambda,\gamma\right)$ vs. the BS density $\lambda$ with SINR	
	threshold $\gamma=0\mathrm{dB.}$	53
13	The UL coverage probability $p^{\mathrm{cov,U}}\left(\lambda,\gamma\right)$ vs. the BS density $\lambda$ with SINR	
	threshold $\gamma = 0  dB$	54

14	DL area spectral efficiency $ASE^{D}(\lambda, \gamma_0)$ vs. the BS density $\lambda$ with SINR	
	threshold $\gamma_0=0$ dB	56
15	UL area spectral efficiency $ASE^{\mathrm{U}}\left(\lambda,\gamma_{0}\right)$ vs. the BS density $\lambda$ with SINR	
	threshold $\gamma_0=0$ dB	57
16	A sketch of the four BS working modes	60
17	The full duplex BS ratio	66
18	The full duplex BS ratio vs. the FD UE ratio $p^{\mathrm{FU}}.$	67
19	The full duplex BS ratio vs. the FD data request probability	68
20	The full duplex BS ratio vs. the UE density $\rho$	69

# LIST OF TABLES

Ι	Notation Summary	6
II	Contributions of the Thesis Compared to Existing Works	11
III	Notation of Variables for Dynamic TDD	39
IV	Notation of Variables for FD	62