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1 investigated in this paper. Based on an equivalent circuit model of PEMFC stack and a
2 mechanism model for evaluating the LFCR effects on the PEMFC, this paper studies
3 primarily and systematically the comprehensive influences of LFCR and harmonics on
4 PEMFC performances and durability, such as (1) degrading the PEMFC performance,
5 (2) shortening the lifetime of PEMFC, (3) reducing the stack output power, (4) lowering
6 its availability efficiency, (5) producing more heat and raising the PEMFC temperature,
7 (6) consuming more fuel, and (7) decreasing the fuel utilization. Finally, a Horizon 300
8 W PEMFC stack is implemented and tested.

9 **Keywords:** Proton exchange membrane fuel cell; Low frequency current ripple; Fuel
10 cell performance and durability; Power conditioning system

11 **1. Introduction**

12 The proton exchange membrane fuel cell (PEMFC) using hydrogen fuel has a long
13 continuous run-time, high power density, and low operating temperature, and hence it is
14 very suitable to be used as a reliable power source in fuel cell (FC) power generation
15 system (PGS). Since the PEMFC is an electrochemical device, it must employ a power
16 conditioning system (PCS), e.g. a DC/DC converter to promote the low DC voltage
17 produced by an FC to a higher one, and/or a DC/AC inverter to obtain an AC voltage.
18 For instance, a DC/DC converter in an uninterruptible power supply (UPS) system can
19 boost a low PEMFC voltage of 36 V to ± 380 V for the DC/AC inverter, as depicted in
20 Fig. 1.

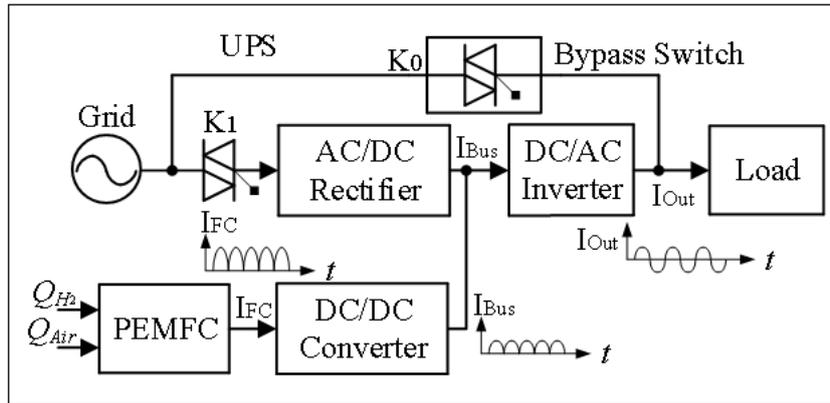


Fig. 1. Schematic diagram of a PEMFC UPS and low frequency current ripples (LFCRs).

As a low voltage and high current device, the low frequency current ripple (LFCR) is a major design issue for a power converter in a PEMFC PGS [1, 2]. The input LFCR must be limited to within 5% of the normal rated value to ensure the satisfactory PEMFC operation. For this reason, the USA National Energy Technology Laboratory published the limits of the LFCR for PEMFC, which suggests that the 100 Hz or 120 Hz ripple should be lower than 15% from 10% to 100% load, not to exceed 0.6 A for lighter loads, and the 50 Hz or 60 Hz ripple should be lower than 10% from 10% to 100% loads, not to exceed 0.4 A for lighter loads [3, 4].

Based on our research findings, the performance and durability influences of LFCR on FC, could be primarily and systematically summarized as that the LFCR is reflected into PEMFC stack and brings harmful influences on the FC stack, such as (1) degrading the FC performance, (2) shortening the lifetime of FC, (3) reducing the stack output power, (4) lowering its availability and efficiency, (5) producing more heat and raising the FC temperature, (6) consuming more fuel, and (7) decreasing the fuel utilization.

1 The influence mechanisms of the LFCR and harmonics on the FC and the involved
2 electrochemical processes are not completely understood yet, which have become an
3 important subject of investigation. Some research papers can be found in the literature
4 indicating that the LFCR can make the voltage-current performance of FC be a
5 hysteretic behavior and reduce the output power [5-8], it might also decrease the FC
6 durability [3, 9-10], and it can generate harmful influences on FC stack, such as
7 increasing more than 10% of fuel consumption, slowing cathode surface responses,
8 creating oxygen starvation, reducing the operating lifetime, and tripping the overload
9 situation [11-13].

10 Therefore, to control the high current ripple, limit the LFCR within the desired
11 range, i.e. 5%, and prolong the lifetime of FCs, three main types of ripple current
12 mitigation strategies have been studied in the power conditioning systems (PCS) as the
13 following: (1) Passive compensation approaches, (2) Active compensation approaches,
14 and (3) Passive and active hybrid compensation methods [14].

15 Regarding the other research work in this field, Ref. [15] proposed an interleaved
16 high gain boost converter topology with a diode clamped multilevel inverter as power
17 interface, which has the main advantages of input LFCR mitigation, high voltage
18 conversion ratio, and voltage balancing across output capacitors. In Ref. [16], based on
19 silicon carbide (SiC) semiconductors and inversely coupled inductors, the proposed
20 6-phase interleaved boost converter (IBC) has achieved low input LFCR, high
21 efficiency, high compactness, high voltage gain ratio and high redundancy. In Ref. [17],

1 a fractional order proportional integral (FOPI) controller was designed for regulating the
2 load voltage to achieve the system specification as compared to the classical integer
3 order proportional integral (IOPI) controller, which can improve the PEMFC dynamic
4 performance and reduce the LFCR under different operating conditions. Ref. [18] found
5 that the power converter has a very important role in lowering the performance and
6 efficiency of PEMFC PCS because of the input LFCR. Ref. [19] proposed a control
7 system, which can contribute significantly to increasing the lifetime, efficiency and
8 reliability of FC PGS, despite its input LFCR. Ref. [20] conducted a comparative study
9 for the hydrogen and oxygen concentration for the 60 Hz case of LFCR, when the
10 current amplitude factor increases, so does the deviation from the steady state of the
11 reactant concentration. The oxygen diffusion response is affected, when the hydrogen
12 utilization becomes a severe high current amplitude factor.

13 The rest of this paper is organized in the following. Section 2 presents the study on
14 the equivalent circuit model, and electrochemical generation steps of electricity in a
15 PEMFC. Section 3 describes the derivation of LFCR production mechanism and model
16 on FC stack. In Section 4, the experimental measurement results obtained from a Horizon
17 300 W prototype are presented to confirm the influences of LFCR on the PEMFC
18 performance, lifetime, power and efficiency, heat and temperature, fuel consumption
19 and utilization.

2. Equivalent circuit model of PEMFC stack

The PEMFC is a type of electrochemical energy conversion device. If the parameters for each single cell are lumped to represent the PEMFC stack, the output voltage of the stack can be expressed as [21]:

$$V_{stack} = E_{rev} - N \left\{ \frac{RT}{\alpha n F} \ln \left(\frac{i + i_n}{i_0} \right) + R_{Ohm} (i + i_n) + \frac{RT}{nF} \left(1 + \frac{1}{\alpha} \right) \ln \left[\frac{i_L}{i_L - (i + i_n)} \right] \right\} \quad (1)$$

where E_{rev} is the reversible voltage (V), N the number of cells in a PEMFC stack, α the transfer coefficient, n the number of electrons per molecule of H_2 (2 electrons per molecule), F the Faraday's constant (C/mol), T the stack or operation temperature (K), R the universal gas constant (J/mol·K), R_{Ohm} the area-normalized resistance, also known as area specific resistance (ARS) of the PEMFC measured ($\Omega \cdot \text{cm}^2$), i_0 the exchange current density (A/cm^2), i_n the internal current or parasitic current density that is wasted (A/cm^2), i_L the limiting current density at which the cell voltage will fall rapidly (A/cm^2), and i the PEMFC stack current density (A/cm^2).

The reversible voltage under different temperatures and pressures can be expressed as:

$$E_{rev} = N \left\{ E^0 + \frac{RT}{2F} \ln \left[\frac{P_{H_2} (P_{O_2})^{\frac{1}{2}}}{P_{H_2O}} \right] + \frac{\Delta \bar{s}_{298.15K}}{nF} (T - 298.15) \right\} \quad (2)$$

where P_i is the partial pressure of species i (i is H_2 , O_2 /air, or liquid water at cathode side) (kPa), E^0 the cell open-circuit voltage (OCV) at the Standard Temperature and Pressure (STP), $E^0 = 1.23 \text{ V}$, and $\Delta \bar{s}_{298.15K}$ the change in the molar entropy at STP

1 (J/mol·K).

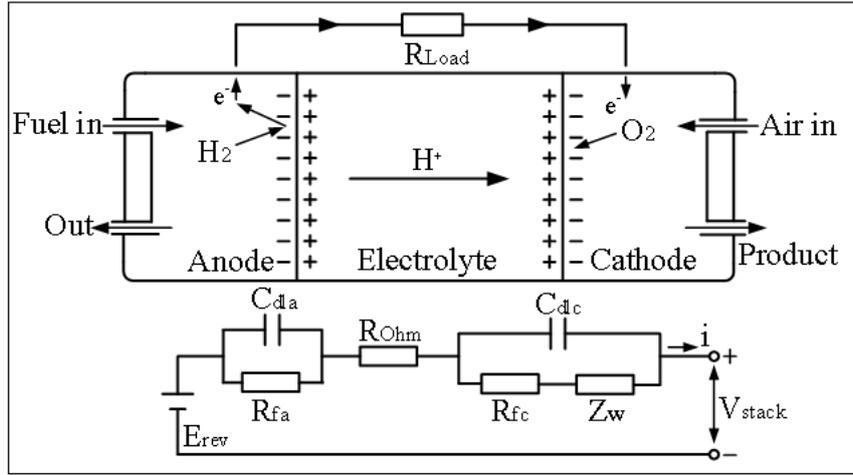
2 According to the above voltage output equation and electrochemical reaction
3 principle, an equivalent circuit model and electrochemical generation steps of electricity
4 in PEMFC are obtained, as shown in Fig. 2, where R_{fa} and R_{fc} are the anode and
5 cathode Faradaic resistances ($\Omega \cdot \text{cm}^2$), reflecting the kinetics of the electrochemical
6 reaction; C_{da} and C_{dc} are the anode and cathode double-layer capacitances (F),
7 reflecting the capacitance feature of the electrochemical reaction interface, respectively.
8 Z_w is the porous bounded Warburg impedance, modeling the mass transport in PEMFC,
9 and it can be expressed as [22]:

$$11 \quad Z_w = \frac{\sigma_i}{\sqrt{\omega}}(1-j) \tanh\left(\delta \sqrt{\frac{j\omega}{D_i}}\right) \quad (3)$$

12
13 where j is the imaginary part in a complex frequency domain coordinate system, δ
14 the diffusion layer thickness (m), D_i the diffusion coefficient of species i (m^2/s), and
15 σ_i the Warbury coefficient for species i (H_2 , O_2/air , N_2 , and H_2O), characterizing the
16 effectiveness of transporting species i to or away from a reaction interface. The
17 Warbury coefficient is defined as:

$$19 \quad \sigma_i = \frac{RT}{\sqrt{2}A(n_iF)^2} \left(\frac{1}{c_i^0 \sqrt{D_i}} \right) \quad (4)$$

20
21 where A is the cathode electrode area (m^2), c_i^0 the cathode bulk concentration of
22 species i (mol/m^3), and n_i the number of electrons per molecule of species i .



1

2 Fig. 2. Equivalent circuit diagram and electrochemical generation steps of electricity in a PEMFC.

3 3. LFCR production mechanism

4 According to the electrochemical impedance spectroscopy analysis methods and
 5 equivalent circuit model of PEMFC stack, it is assumed that the PEMFC must meet the
 6 requirement of a linear system, and it is guaranteed by the amplitude of disturbance
 7 signals injected into the PEMFC. Then, the fluctuation signal can be conducted in either
 8 the galvanic-static mode or the potential-static mode [23].

9 As mentioned above, when the LFCR is injected into a PEMFC stack and produces
 10 harmful influences on the FC current and voltage, the output current of the PEMFC
 11 stack can be expressed as:

12

$$13 \quad i = I_{DC} + I_{BUS} \sin(2\omega t + \theta) \quad (5)$$

14

15 where I_{DC} indicates the DC side current value of the DC/DC converter load, I_{BUS} , ω ,
 16 and θ are the amplitude, angular frequency and phase of the perturbation signal

1 (including the LFCR) from DC/DC converter, respectively.

2 According to the equivalent circuit model without LFCR injected into the PEMFC,
3 as shown in Fig. 2, the total AC impedance can be obtained as:

$$4 \quad Z(j\omega) = R_{Ohm} + \frac{R_{fa} \cdot \frac{1}{j\omega C_{dla}}}{R_{fa} + \frac{1}{j\omega C_{dla}}} + \frac{(R_{fc} + Z_W) \cdot \frac{1}{j\omega C_{dlc}}}{R_{fc} + Z_W + \frac{1}{j\omega C_{dlc}}} \quad (6)$$

6

7 When a PEMFC is injected by LFCR, $Z_W|_{\omega \rightarrow 0} = R_{conc} = \delta\sigma_i \sqrt{\frac{2}{D_i}}$, where R_{conc} is
8 known as the concentration resistance reflecting the mass transfer in PEMFC, Equation
9 (6) becomes:

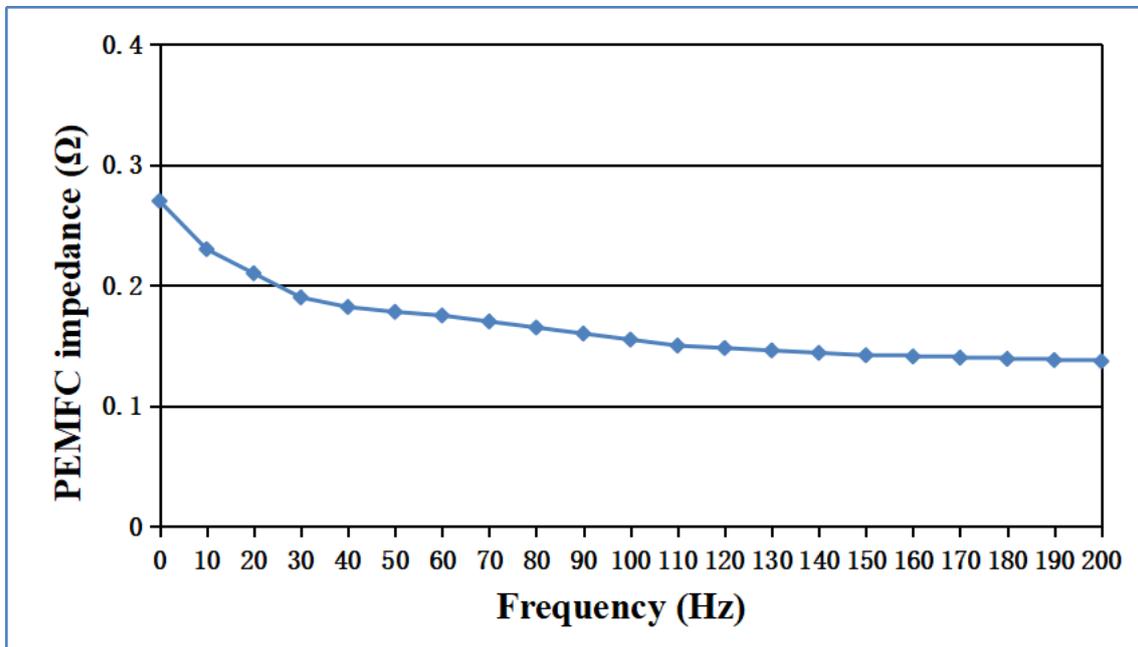
$$10 \quad \begin{aligned} Z'(j\omega) &= R_{Ohm} + \frac{R_{fa} \cdot \frac{1}{j\omega C_{dla}}}{R_{fa} + \frac{1}{j\omega C_{dla}}} + \frac{(R_{fc} + R_{conc}) \cdot \frac{1}{j\omega C_{dlc}}}{R_{fc} + R_{conc} + \frac{1}{j\omega C_{dlc}}} \\ &= R_{Ohm} + \frac{R_{fa}}{1 + \omega^2 \tau_a^2} + \frac{R_{fc} + R_{conc}}{1 + \omega^2 \tau_c^2} - j \left[\frac{\omega \tau_a \cdot R_{fa}}{1 + \omega^2 \tau_a^2} + \frac{\omega \tau_c (R_{fc} + R_{conc})}{1 + \omega^2 \tau_c^2} \right] \\ &= A(\omega) \angle \phi(\omega) \end{aligned} \quad (7)$$

11 where $\tau_a = C_{dla} R_{fa}$ is the anode time constant (s), $\tau_c = C_{dlc} (R_{fc} + R_{conc})$ is the cathode
12 time constant (s), and $A(\omega)$ and $\phi(\omega)$ are the amplitude and phase shift resulted
13 from $Z(j\omega)$, respectively.

14 Fig. 3 shows the measured AC impedance variation of a 300 W self-humidified,
15 air-breathing, 63-cell PEMFC from Horizon Fuel Cell Technologies in Singapore, with
16 frequency from 0 to 200 Hz under the rated power conditions. Moreover, the lower the
17 frequency of current ripples, the higher the impedance of the PEMFC. Therefore, the

1 LFCR and harmonics will cause detrimental effects on the PEMFC performance.

2 The AC impedance tests of the 300 W PEMFC were performed using a
3 programmable high power DC electronic load (IT8902A/E-150-200), a function
4 generator, and a computer data-acquisition system equipped with corresponding
5 software, as shown in Fig. 4 . The AC impedance measurement method is that the rated
6 power condition is set in constant current (CC) mode as the DC current test point of the
7 PEMFC. The sinusoidal signal of test frequency is output by signal generator, the sine
8 waveform of electronic load is controlled, the voltage and current data in the internal
9 cache area of electronic load is read, and the fast Fourier transform (FFT) analysis is
10 carried out. Finally, a mathematical function is used to divide the converted voltage by
11 the converted current to obtain the AC impedance of the PEMFC.



12

13

Fig. 3. Impedance variation of a 300 W PEMFC at the rated conditions.

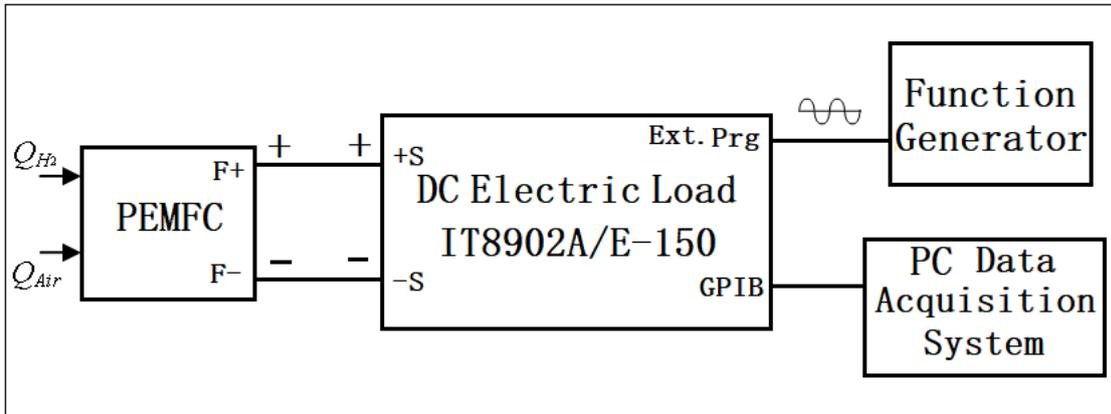


Fig. 4. Schematic diagram of PEMFC AC impedance measurement.

When the LFCR and harmonics are added to the PEMFC, the output voltage V_{stack} can be defined as:

$$V_{stack} = E_{rev} - N(R_{Ohm} + R_{fa} + R_{fc} + R_{conc})I_{DC} - NA(\omega)I_{BUS} \sin(\omega t + \theta + \phi) \quad (8)$$

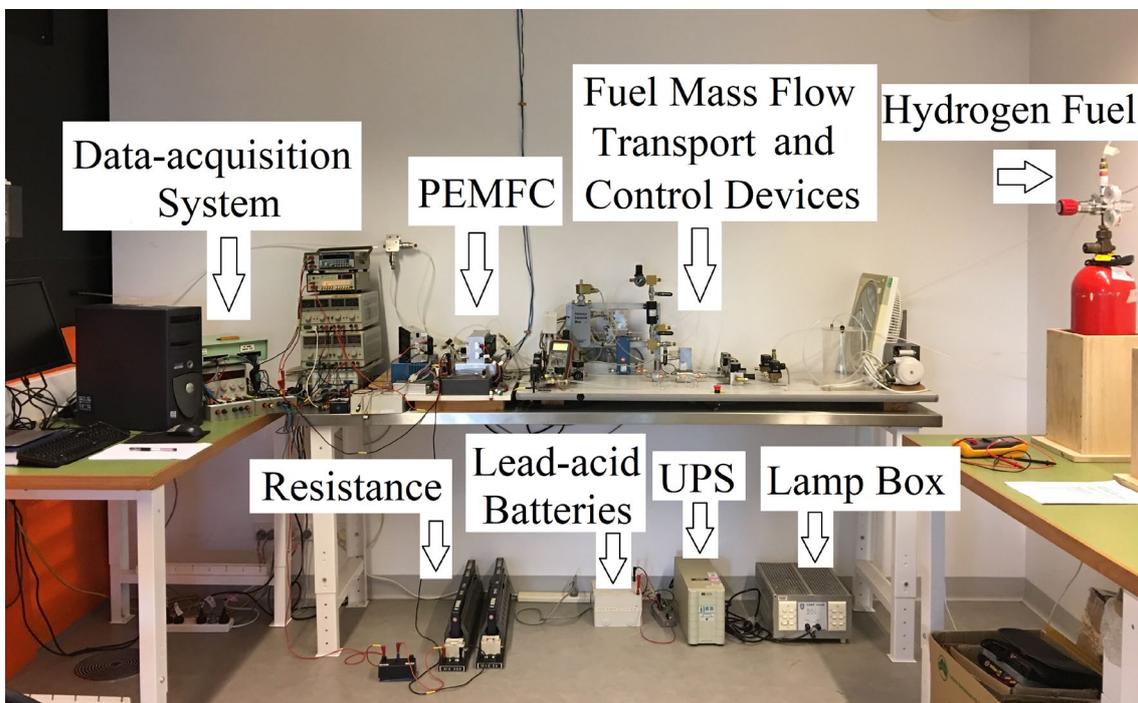
Consequently, it could be analyzed that the LFCR is reflected into PEMFC stack and brings harmful influences on the FC stack.

4. Experimental results and discussion

The experimental setup consists of a UPS system, PEMFC power generation and test system, lead-acid batteries, supercapacitors, and a data-acquisition system. In the PEMFC power generation and test system, a hydrogen flowmeter F-201C-GAS-22V (Bronkhorst) and an air flowmeter F-112AC-GAS-22V (Bronkhorst) are selected. The temperature and humidity of hydrogen and air are controlled by the hydrotransmitter HD2008TV1 (Delta OHM), and the pressure transmitter between the inlets of cathode

1 and anode is the AUS EX 1354X (Burkert). All the physical parameters, such as the
2 performance, lifetime, power and efficiency, heat and temperature, fuel consumption
3 and utilization are recorded with the data-acquisition system. Voltage and current
4 signals are measured by using an LA55-P and an LV25-P [24].

5 Fig. 5 shows a photo of the new experimental setup at the University of
6 Technology Sydney (UTS), Australia.

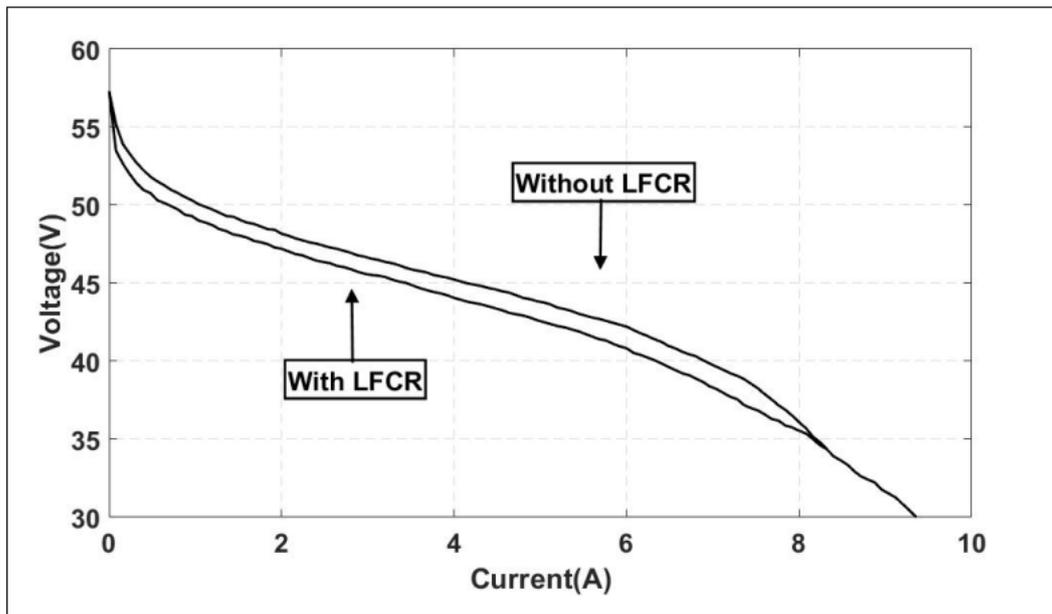


7
8 Fig. 5. Photograph of the new experimental setup.

9 10 4.1. Influence of LFCR on PEMFC stack performance

11 The LFCR injected into a PEMFC will influence the voltage-current performance,
12 which can be calculated from the mathematical model mentioned above and tested via
13 the experiments, as shown in Fig. 6, where one is with LFCR, and the other is without
14 LFCR. Fig. 6 illustrates the performance degradation of PEMFC with LFCR, compared
15 to that without LFCR. When there are perturbation signals, including the LFCR and

1 harmonics from the PCS, compared with the case of no perturbation signal, the
2 performance of PEMFC stack can be changed because of the AC component in
3 Equation (7). Furthermore, the enclosed area represents the performance degradation of
4 PEMFC because of the influence of LFCR and harmonics. That is the additional system
5 loss because of the action of $Z(j\omega)$ [5].



6
7 Fig. 6. Voltage-current curve of a 300 W PEMFC stack obtained for the ascending and descending
8 branches for the inversion point $I= 8.2$ A.

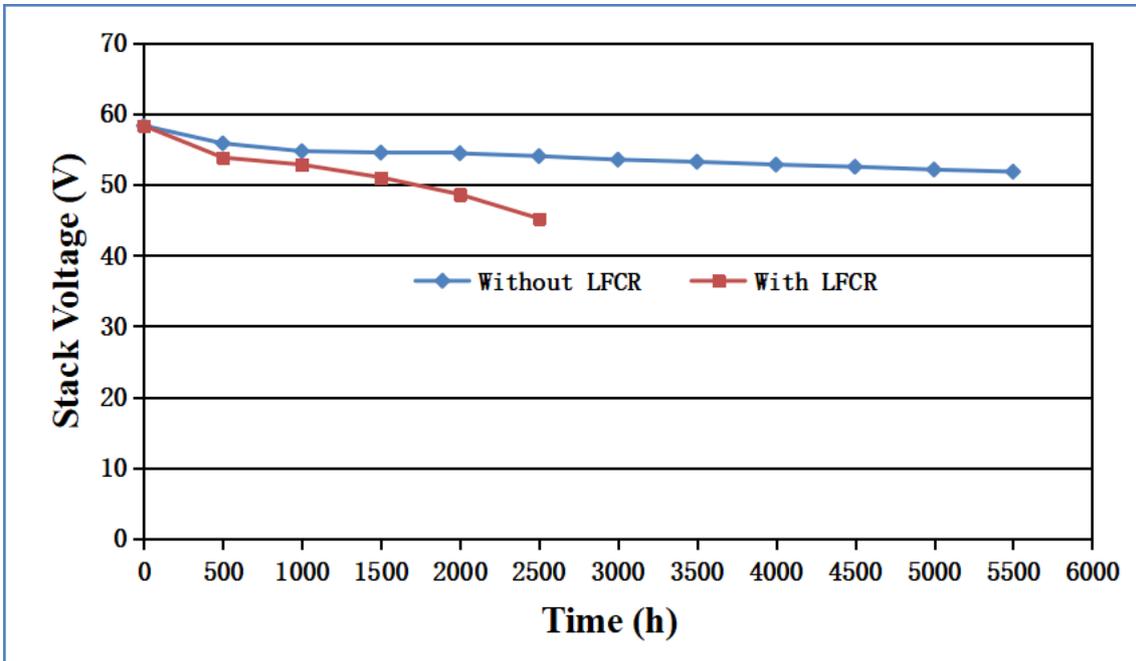
9 10 4.2. Influence on FC stack lifetime

11 The PEMFC is a complex electrochemical device, which constitutes many
12 components, such as catalysts, catalyst supports, proton exchange membranes, gas
13 diffusion layers (GDLs), bipolar plates, sealings and gaskets. Each of these components
14 could degrade or fail, leading to the FC system to degrade or fail.

15 In a designed PEMFC PCS, the LFCR and harmonics will decrease the FC lifetime.

16 Fig. 7 depicts the measured results of stack voltage versus time for two different cases
17 with and without LFCR when a 300 W PEMFC PGS is connected to a resistive load or a

1 UPS load with a DC/DC converter. As shown in Fig. 7, the lifetime of PEMFC with
2 LFCR is shorter than that without LFCR.



3 Fig. 7. Different lifetimes and performances of PEMFC stack with and without LFCR.
4
5

6 As mentioned above, the LFCR can produce influences of the performance
7 degradation and lifetime on PEMFC, because it has a great influence on the anode and
8 cathode double layer capacitor in the electrochemical reaction interface of PEMFC and
9 causes many other issues. The degradation of PEMFC basically involves the mechanical
10 degradation, chemical or electrochemical degradation, thermal degradation, and
11 material degradation through the action of the perturbation signal, such as LFCR and
12 harmonics, resulting in the static and dynamic performance degradation of PEMFC.
13 Moreover, it can increase the power loss and heat, and even reduce the FC durability
14 and reliability. The conclusion could be obtained according to the equivalent circuit
15 model of a PEMFC considering the degradation influences.

1 On the other hand, the component degradation includes that, but is not limited to,
2 (1) in catalyst, there are the platinum catalyst degradation of Pt agglomeration and
3 particle growth, Pt migration, Pt elemental loss, Pt catalyst contamination, and catalyst
4 support degradation, (2) in membrane, there are the membrane degradation on chemical
5 aspect and mechanical aspect, pinholes, delamination, and cracking of membrane, (3) in
6 porous transport layer, there are the degradation on mechanical and thermal physics
7 aspect, chemical and electrochemical aspect, and porosity and pore size distributions, (4)
8 in bipolar plates, there are the degradation of graphite composite bipolar plates and
9 metal bipolar plates, and (5) in other components, there are the degradation of the seals,
10 endplates, and bus plates [25].

11 Some degradation mechanisms for a PEMFC, such as the carbon corrosion for a
12 typical Pt/C catalyst, the Pt particle growth and dissolution/precipitation, and the chain
13 scission of perfluorosulfonic acid (PFSA) membrane, can offer deep understanding in
14 the FC degradation. In addition, the degradation processes of different components are
15 often related to the materials, control and design of an FC system. Therefore, it is
16 important to investigate, analyze, and systematically understand the degradation
17 phenomena of each component, so that some novel component materials and
18 manufacture technologies can be developed. Furthermore, the novel modeling, control
19 and design from cells to stacks can be achieved to mitigate the negative influences on
20 the FC durability and reliability under all kinds of operation conditions.

21 According to the 2016 US Department of Energy (DOE) report, the lifetime and cost

1 targets are to develop a 65% peak-efficient, direct hydrogen FC power system for
 2 transportation that can achieve 5,000 h durability (ultimate 8,000 h) and be mass
 3 produced at a cost of \$40/kW by 2020 (ultimate \$30/kW) [26]. Therefore, further
 4 investigation for improving the PEMFC performance and prolonging the lifetime of
 5 PEMFC seems to be necessary.

6 7 4.3. Influences on FC stack efficiency and power

8 Based on the electrochemical principle, assuming that all of the Gibbs free energy
 9 can be converted into electrical energy, in theory, the maximum possible
 10 electrochemical efficiency of an FC is the ratio between the Gibbs free energy and
 11 hydrogen higher heating value, or $\eta_{Theory} = \Delta G/\Delta H = 237.34/286.02 = 83\%$.

12 In practical application, because of various possibilities, such as the hydrogen
 13 diffusion through the membrane, combining with oxygen diffused through the
 14 membrane, and internal currents, some hydrogen is lost. On the other hand, due to the
 15 hydrogen stoichiometry ratio in the electrochemical reaction, the hydrogen consumption
 16 will be higher than that corresponding to the current generated, and the FC efficiency
 17 would be lower than given theoretical value. The FC efficiency is then [22]:

$$18 \quad \eta_{FC} = \frac{V_{Stack}}{1.482} \left(\frac{i}{i + i_{loss}} \right) \eta_{fu} \quad (9)$$

19 where η_{fu} is the fuel utilization, and i_{loss} the hydrogen loss current (A/cm²).

20 Consequently, when a pure resistive load is connected to the 300W PEMFC
 21 generation system without using PCS in the experiment, its measured efficiency η_{FC} is
 22 about 45%~55%, as shown in Fig. 8.

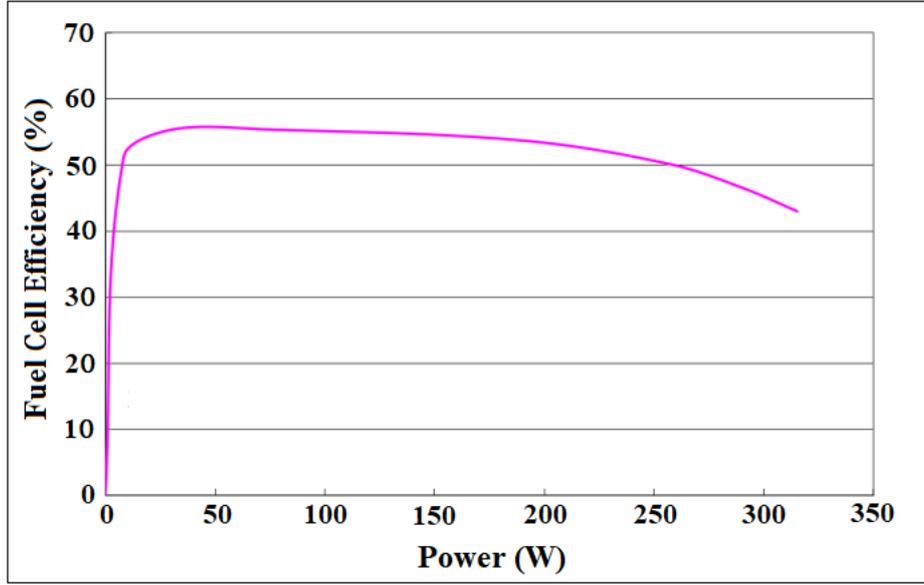


Fig. 8. Efficiency of a 300 W PEMFC stack without PCS.

When the PCS is used in the PEMFC power system, the overall efficiency of FC PCS system is

$$\eta_{sys} = \eta_{FC} \eta_{PCS} \eta_{ripple} \quad (10)$$

where η_{ripple} is the ripple efficiency of an FC associated with current ripples and harmonics, and η_{PCS} the efficiency of DC/DC or DC/AC power converter in PCS.

According to the measured value of the FC PCS system, the efficiency of PCS in PEMFC operating mode under the rated load of 270 W is $\eta_{PCS} = \eta_{DC/DC} \eta_{DC/AC} = 72\%$.

The definition of an FC efficiency associated with current ripple is:

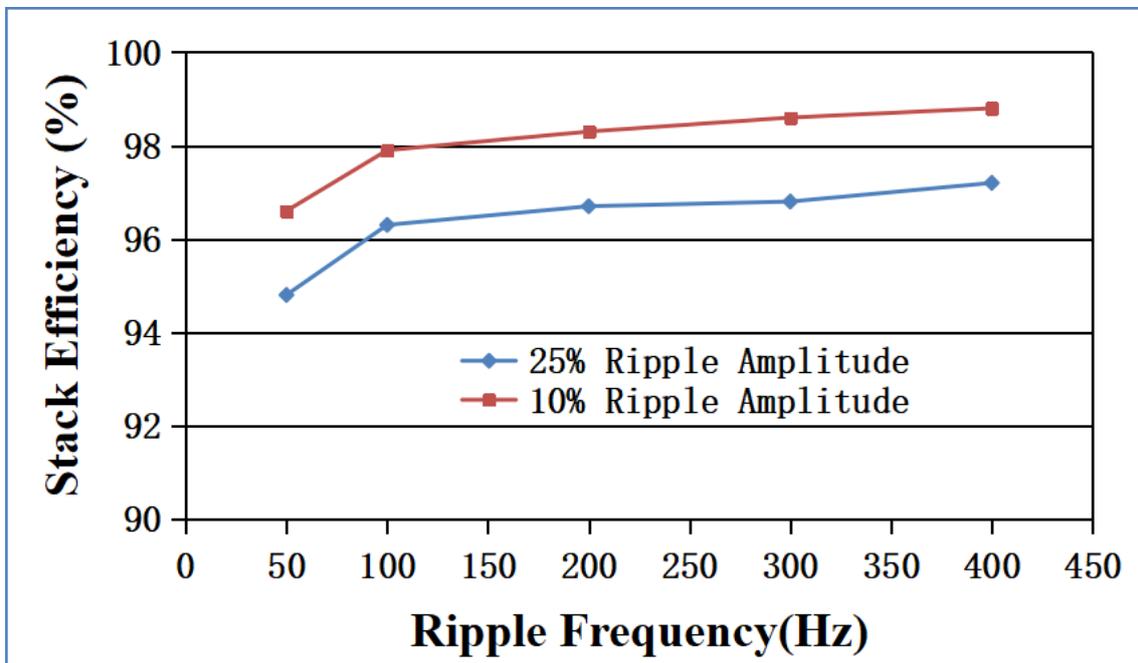
$$\eta_{ripple} = \frac{P_{Out}}{P_{Bus}} = 1 - \frac{P_{Ripple}}{P_{Bus}} \quad (11)$$

where $P_{Out} = P_{Bus} - P_{Ripple}$, $P_{Bus} = V_{Bus} I_{Bus}$ is the output power in the DC bus side and

$P_{Ripple} = |Z(j\omega)| I_{Ripple}^2$ represents the additional losses due to the current ripple itself.

Therefore, when the PEMFC is connected to the DC/DC converter without any mitigation control methods of LFCR and harmonics, the $|Z(j\omega)|$ will increase, and the

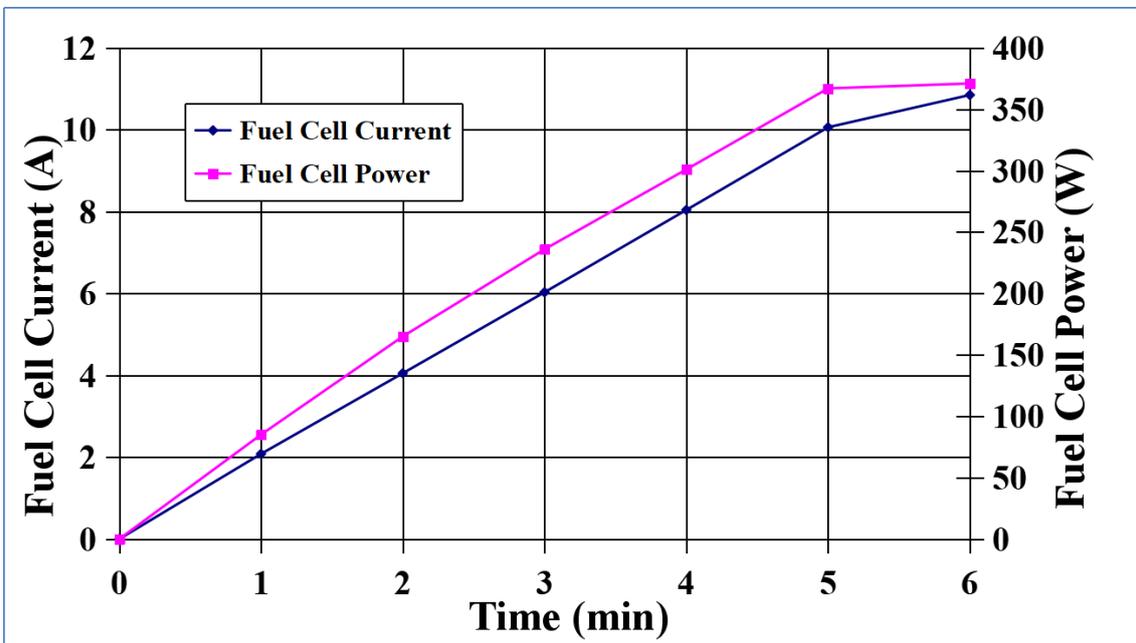
1 ripple current value will produce a ripple power loss. The practical output power of
 2 PEMFC will decrease. Fig. 9 illustrates the PEMFC stack efficiency measured as a
 3 function of ripple frequency of 50 Hz to 400 Hz and ripple amplitudes of 9.9% (when
 4 using a passive compensation method in PEMFC PCS), and 24.3% (without any
 5 compensation methods in PEMFC PCS) in the rated load (about 8.20 A). As expected in
 6 Fig. 9, the curves show that the efficiency of PEMFC stack decreases as the ripple
 7 amplitude increases, and an increase in the ripple frequency helps to increase the
 8 efficiency, and reduce hydrogen fuel utilization. On the contrary, the high frequency
 9 ripple currents, such as DC/DC converter switching at a frequency of 50 kHz, can be
 10 greatly weakened by the input capacitor, which has little or no influence on PEMFC
 11 efficiency.



12
 13 Fig. 9. Influences of different percentage amplitudes of LFCR on PEMFC stack efficiency.

14 Figs. 10(a) and 10(b) show the measured input power and current curves of the
 15 PEMFC with a pure resistive load and a DC/DC converter load, respectively, in a UPS

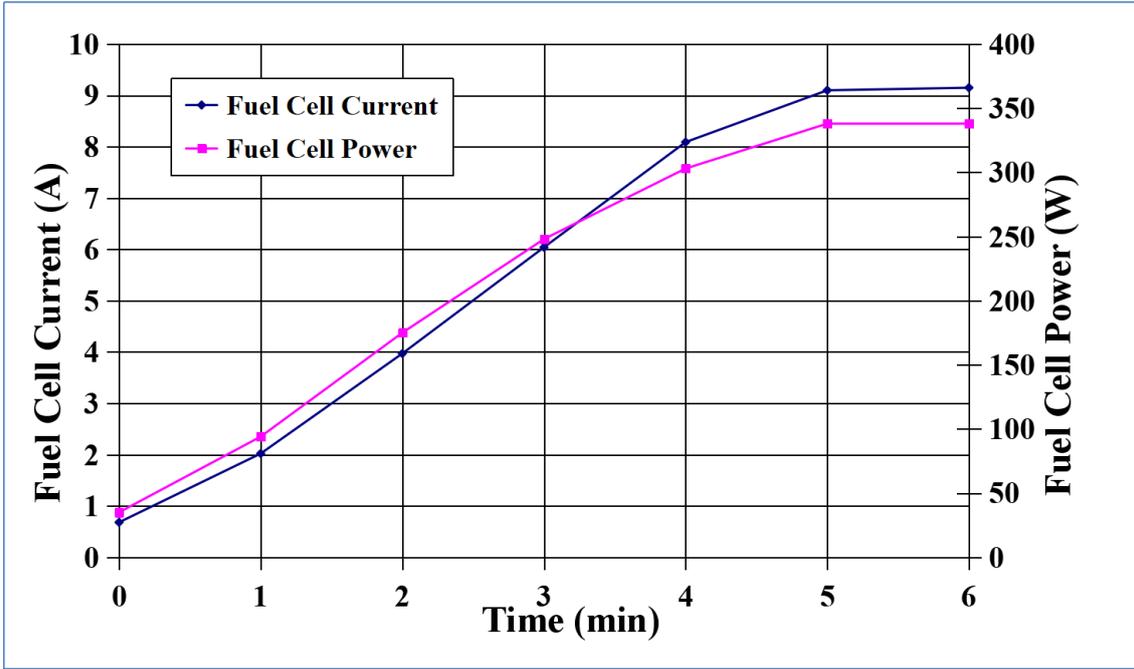
1 system under the same operation conditions. The output power of PEMFC with LFCR
 2 and harmonics with the DC/DC converter load is about 1.3%~2.6% more than that of
 3 PEMFC with a pure resistive load. Moreover, when the UPS without any load is
 4 connected to a running PEMFC, a 35 W power has been lost, as shown in Fig. 10(b). In
 5 Fig. 10(b), with the increase of the UPS load that has the same power as the resistance
 6 load, its power loss range of PEMFC stack is from 37 W to 49 W, which includes the
 7 power loss caused by the current ripple. Furthermore, the maximum output powers of
 8 PEMFC are 338 W and 371 W when connected to UPS system and resistance load,
 9 respectively. Therefore, the load ability of PEMFC connected to UPS system is poorer.



10

11

(a)



(b)

Fig. 10. Power and current characteristics of PEMFC under different types of loads: (a) pure resistive load, and (b) UPS system with DC/DC converter.

4.4. Influences of LFCR on fuel utilization

According to the definition, the fuel utilization η_{fu} in an FC power system can be expressed as:

$$\eta_{fu} = \frac{\dot{n}_{cons}}{\dot{n}_{cons} + \dot{n}_{loss} + \tau_{prg} f_{prg} \dot{n}_{purge}} \quad (12)$$

where \dot{n}_{cons} is the mass flow rate of fuel consumption (mol/s), \dot{n}_{loss} the mass flow rate of fuel loss (mol/s), \dot{n}_{purge} the mass flow rate of fuel purge (mol/s), τ_{prg} the duration of fuel purge (s), and f_{prg} the frequency of fuel purge (Hz).

In general, the fuel utilization is related to the fuel stoichiometric ratio. For instance, the hydrogen utilization η_{H_2} can be obtained from the current drawn by FC

1 power system as shown in the following expression:

$$2 \quad \eta_{H_2} = \frac{1}{S_{H_2}} \quad (13)$$

3 where S_{H_2} is the hydrogen stoichiometric ratio, and $S_{H_2} = \frac{\dot{n}_{H_2,act}}{\dot{n}_{H_2,theory}} = \frac{nF}{I} \dot{n}_{H_2,act}$.

4 Therefore, the hydrogen utilization, η_{H_2} , oxygen utilization, η_{O_2} , and air
5 utilization, η_{Air} , can be obtained from the current drawn by FC power system by using
6 the following expression:

$$7 \quad \eta_{H_2} = \frac{I}{nF\dot{n}_{H_2}} \quad (14)$$

8 where I is the FC output current (A), \dot{n}_{H_2} the hydrogen mass flow rate (mol/s), and
9 nF determines the charge flow between the anode and the cathode. In the same manner,
10 the oxygen and air utilization can be obtained as follows:

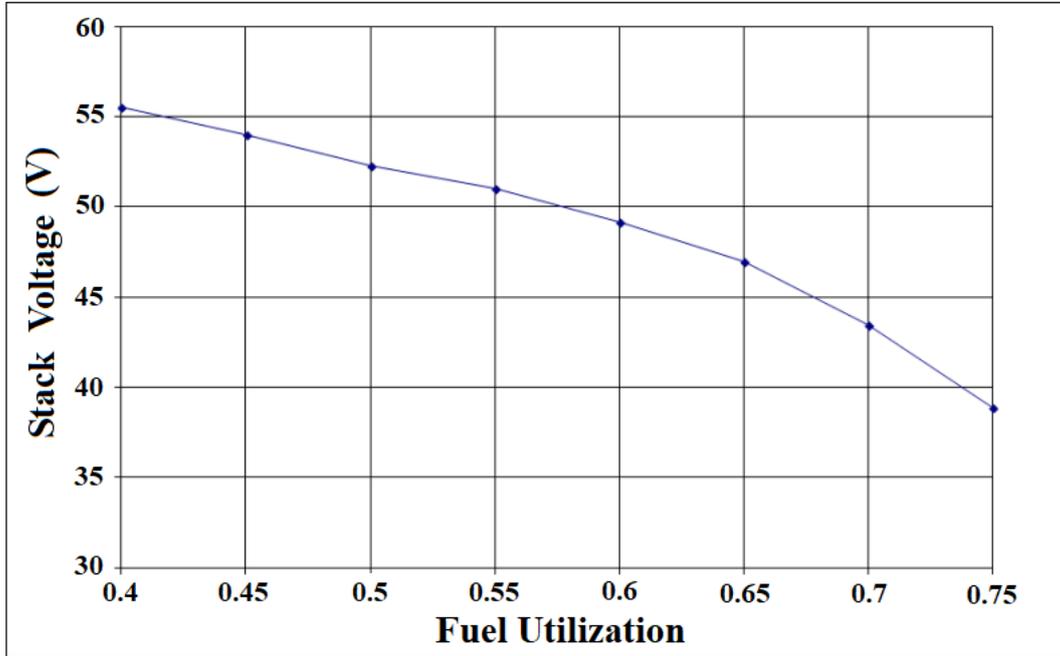
$$11 \quad \eta_{O_2} = \frac{I}{nF\dot{n}_{O_2}} \quad (15)$$

$$12 \quad \eta_{Air} = \frac{I}{nF\dot{n}_{Air}} \quad (16)$$

13 For the pure hydrogen and the dead-end purge mode, because $S_{H_2}=1.1$ to 1.2 ,
14 $S_{O_2}=1.2$ to 1.5 , and $S_{Air}=2$ to 2.5 , one can obtain that $\eta_{H_2}=83.3\%$ to 90.9% , $\eta_{O_2}=
15 66.7\%$ to 83.3% , and $\eta_{Air}=40\%$ to 50% . However, to improve the performance of FC,
16 the fixed cycle of purge mode has to be used in FC power system. At this point, it is
17 difficult to measure the fuel utilization accurately.

18 The influence of fuel utilization on the FC output voltage is because of the LFCR
19 and harmonics injected. Fig. 11 shows the impact of fuel utilization on the 300 W

1 PEMFC output voltages due to the LFCR and harmonics. The larger the initial fuel
 2 utilization, the larger the reactant consumption.



3
 4 Fig. 11. Impact of initial hydrogen utilization on fractional voltage drop.

5
 6 4.5. Influence of LFCR on FC stack heat and temperature
 7

8 In an FC, the internal heat transfer is derived from the electron transmission and
 9 ion transport behavior of electrochemical reaction resistance. Assume that the water
 10 within the FC is vaporized, and the steam produced has been removed out of FC, the
 11 heat flow q_{int} is generated by:

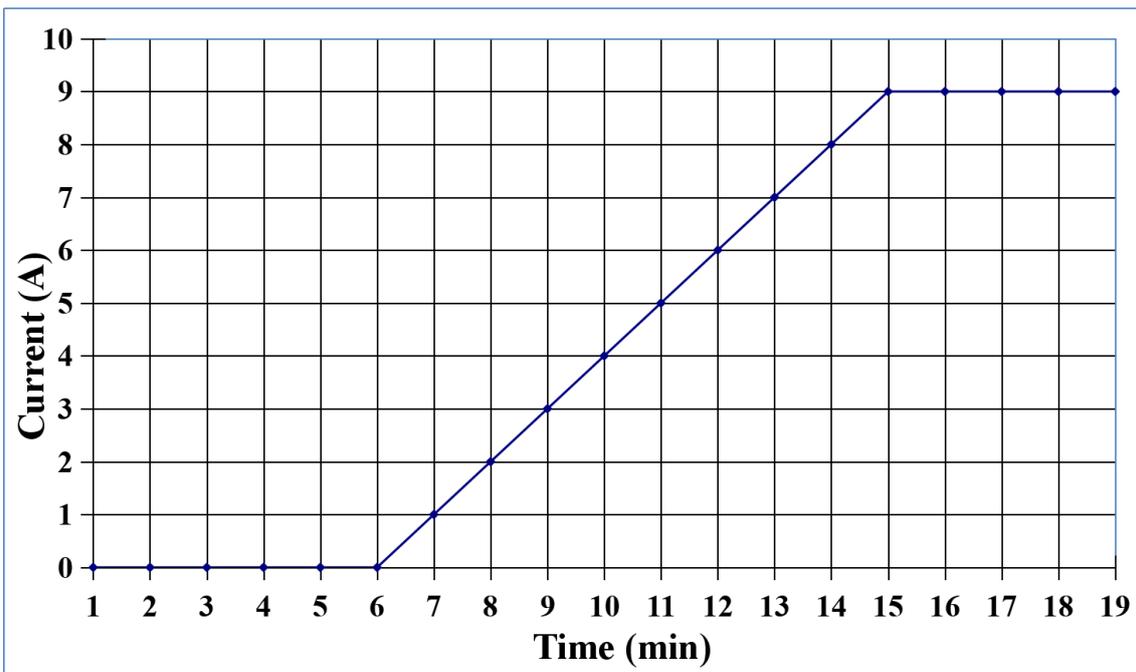
12
$$q_{int} = R_{Ohm} i^2 \quad (17)$$

13 When the LFCR is injected into the FC, it makes the resistance of PEMFC change,

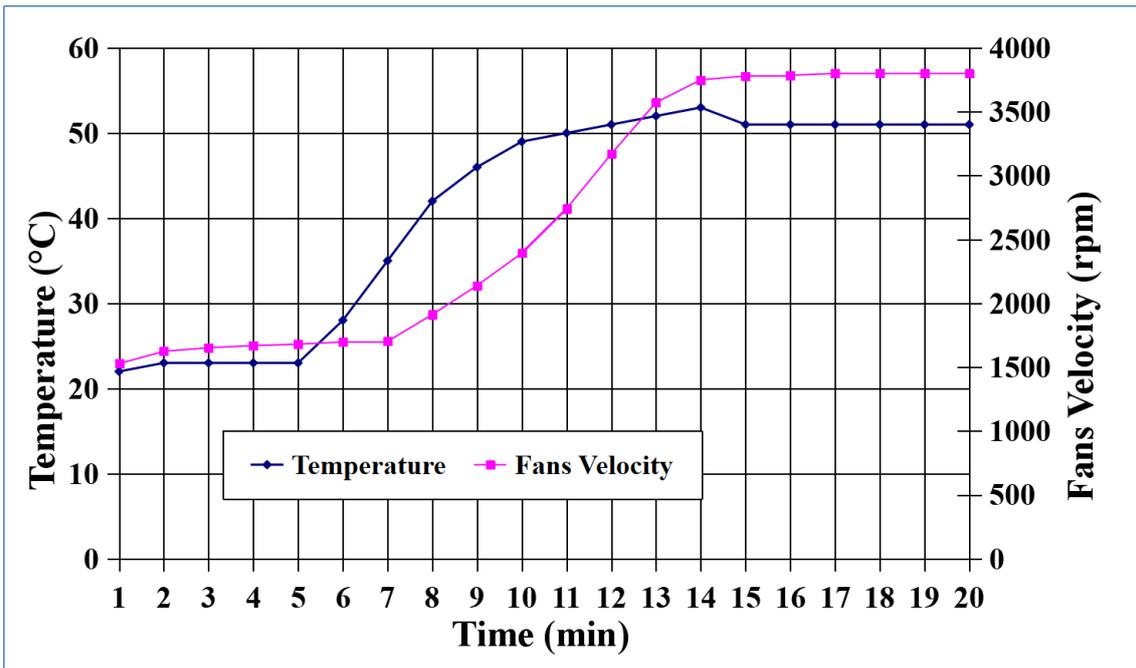
14 $R_{Ohm} \rightarrow R_{ripple}$, as shown in Fig. 3, the heat produced will increase as follows:

15
$$\Delta q_{int.ripple} = R_{ripple} i^2 \quad (18)$$

1 To keep the water balance and reduce the influence of the internal resistance or
2 Ohmic losses, the stack temperature will be controlled in the range of 50~60°C under
3 the rated load, as shown in Figs. 12(a) -12(c). In this experiment, when the load changes
4 as mentioned in Fig. 12(a), the stack temperature and fan velocity show that the
5 characteristics of temperature and fan velocity when connected to a resistive load are
6 smoother than those when connected to a UPS system with a DC/DC converter or
7 DC/AC inverter. However, in the steady state, the former's temperature and fan velocity,
8 as shown in Fig. 12(b), are smaller than those of the latter, as depicted in Fig. 12(c).



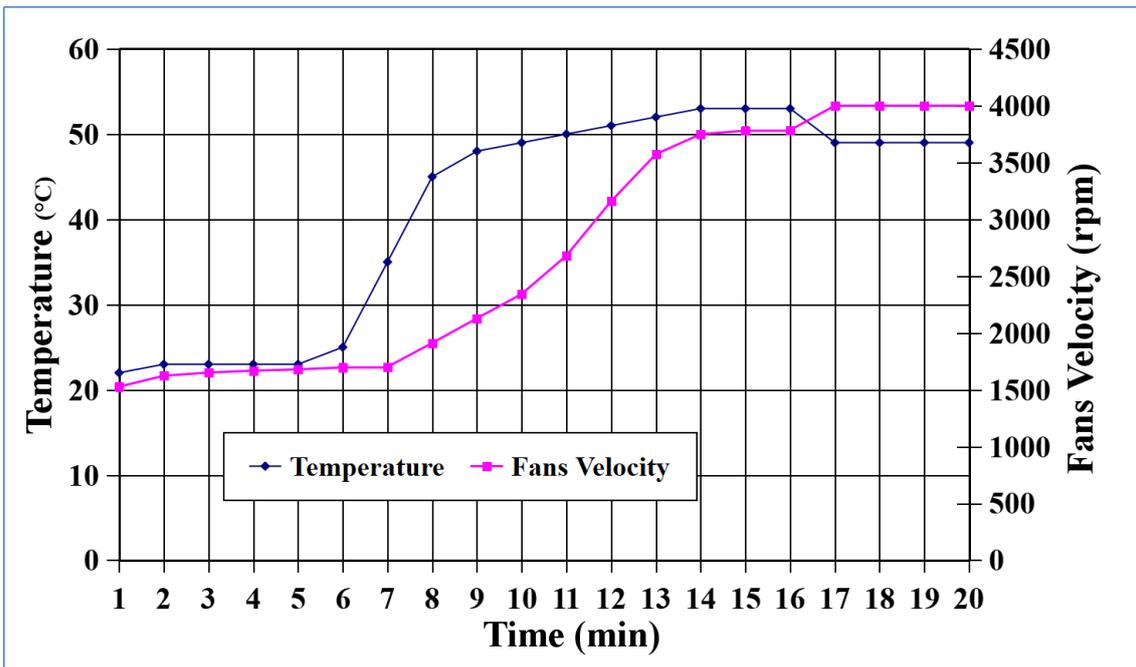
(a)



1

2

(b)



3

4

(c)

5 Fig. 12. PEMFC stack temperature and fan velocity charts under: (a) load variations, (b) resistance
6 load, and (c) UPS load.

7

According to Equation (18), the heat produced in the PEMFC, if not managed and

1 dissipated properly, can have a significant influence on the performance and lifespan of
2 the FC. The variations occur in the hydrogen utilization and the temperature of an air
3 supply pipe (ASP) with the ripple amplitude and frequency of the current in SOFC PCS.
4 The hydrogen utilization has to increase significantly to meet higher load demands.
5 Moreover, The ASP temperature varies with the load. Therefore, the influence of such
6 load transients on SOFC temperature distribution could be illustrated [13].

7 **5. Conclusion**

8 In this paper, using an equivalent circuit modeling and comprehensive analysis
9 methodology, the influences of LFCR on a PEMFC performance, lifetime, power and
10 efficiency, heat and temperature, fuel consumption and utilization are analyzed and
11 discussed. A 300 W PEMFC UPS prototype is implemented with an input voltage range
12 from 30 to 60 V. The experimental results show that the LFCR with large magnitudes
13 related to the angular frequency and phase of the perturbation signal from DC/DC
14 converter and DC/AC inverter in the UPS system result in the decreased variations in
15 the performance, lifespan, power and efficiency of a PEMFC, and increased variations
16 in the thermal and temperature, fuel consumption and utilization of the PEMFC.

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