Per-Dereference Verification of Temporal Heap Safety via Adaptive Context-Sensitive Analysis

Abstract. We address the problem of verifying the temporal safety of heap memory at each pointer dereference. Unlike separation-logic-based approaches, our whole-program analysis approach is undertaken from the perspective of pointer analysis, allowing us to leverage the advantages of and advances in pointer analysis to improve precision and scalability. A dereference ω , say, via pointer q is unsafe iff there exists a deallocation ψ , say, via pointer p such that on a control-flow path ρ , p aliases with q (with both pointing to an object o representing an allocation), denoted $\mathcal{A}^{\psi}_{\omega}(\rho)$, and ψ reaches ω on ρ via control flow, denoted $\mathcal{R}^{\psi}_{\omega}(\rho)$. Applying directly any existing pointer analysis, which is typically solved separately with an associated control-flow reachability analysis, will render such verification highly imprecise, since $\exists \rho. \mathcal{A}^{\psi}_{\omega}(\rho) \land \exists \rho. \mathcal{R}^{\psi}_{\omega}(\rho) \Rightarrow \exists \rho. \mathcal{A}^{\psi}_{\omega}(\rho) \land \mathcal{R}^{\psi}_{\omega}(\rho)$ (i.e., \exists does not distribute over \land). For precision, we solve $\exists \rho. \mathcal{A}^{\psi}_{\omega}(\rho) \land \mathcal{R}^{\psi}_{\omega}(\rho)$, with a control-flow path ρ containing an allocation o, a deallocation ψ and a dereference ω abstracted by a tuple of three contexts $(c_o, c_{\psi}, c_{\omega})$. For scalability, a demand-driven full context-sensitive (modulo recursion) pointer analysis, which operates on pre-computed def-use chains with adaptive context-sensitivity, is used to infer $(c_o, c_{\psi}, c_{\omega})$, without losing soundness or precision. Our evaluation shows that our approach can successfully verify the safety of 81.3% (or $\frac{93,141}{114,508}$) of all the dereferences in a set of 10 C programs totalling 1,166 KLOC.

1 Introduction

Unmanaged languages such as C/C++ still remain irreplaceable in developing performance-critical systems such as OSs, databases and web browsers. Such languages, however, suffer from memory safety issues. While spatial errors (e.g., buffer overflows) result in disastrous consequences (e.g., crashes, data corruption, information leakage, privilege escalation and control-flow hijacking), their temporal counterparts have been shown to be equally deadly [54,31]. In particular, verifying absence of dangling pointer dereferences, an important temporal heap safety (TH-safety hereafter), is thus desirable.

A quite flourishing research thread in the recent literature focuses on separation logic [44,19,58], which enables precise shape analysis for pointer-based data structures such as linked lists and trees in C/C++ programs. Much research effort has been devoted to improving scalability and automation of separation-logic-based verification [57,17]. In particular, bi-abduction [11] empowers separation-logic-based verification to generate program specifications automatically for large programs with millions of lines of code, in a compositional manner rather than as a whole-program analysis. However, one of its inevitable downsides (from the perspective of whole-program analysis) is the loss of precision due to a maximum size limit imposed on disjunctions of pre-conditions manipulated in order to improve performance [12]. Indeed, balancing precision and scalability is a never-ending battle. For practical purposes, Infer [10], a bi-abduction-based verifier, has recently surrendered soundness and evolved into a precise bug-hunter.

Memory errors can also be found by other techniques, such as data-flow analysis [43,18] and model checking [27,29,40]. Notably, pointer analysis [28,47,61,48,50]

has recently made significant strides, providing a solid foundation for developing many pointer-analysis-based static analyses for detecting memory errors [13,33,46,56,59]. In this paper, we present a fully-automated pointer-analysis-based approach, called D^3 (a **D**isprover of **D**angling pointer **D**ereferences), to verifying absence of (i.e., disproving presence of) dangling pointers on a per dereference basis. Compared to separationlogic-based approaches, our approach tackles this verification task from a different angle. Instead of focusing on reasoning about a variety of pointer-based data structures precisely in separation logic, we focus on reasoning about pointer aliasing and controlflow reachability context-sensitively in a whole-program setting *on-demand*.

Challenges We highlight three challenges, from the perspective of pointer analysis:

Challenge 1: Modeling the Triple Troublemakers. A TH-safety violation involves three distinct program locations, an allocation o (representing an allocation site), a deallocation ψ and a dereference ω , which must be all modelled precisely.

Challenge 2: Resolving Aliases. A dereference ω (via pointer q) is unsafe iff there exists a deallocation ψ (via pointer p) such that on a control-flow path ρ , p aliases with q (with both pointing to an object o), denoted $\mathcal{A}^{\psi}_{\omega}(\rho)$, and ψ reaches ω on ρ via control flow, denoted $\mathcal{R}^{\psi}_{\omega}(\rho)$. Pointer aliasing, a well-known difficult static analysis problem, must be solved to guarantee both soundness and precision scalably for large programs. For the TH-safety verification, this is particularly challenging. Any existing k-limited context-sensitive pointer analysis that scales for large programs [47,28] (where $k \leq 3$ currently) is not precise enough (as o, ψ and ω can often span across more than three functions). In addition, off-the-shelf pointer analyses provide the alias information between ψ and ω but are oblivious to the control-flow reachability information from ψ to ω (even if solved flow-sensitively), causing potentially a significant precision loss, since $\exists \rho.\mathcal{A}^{\psi}_{\omega}(\rho) \land \exists \rho.\mathcal{R}^{\psi}_{\omega}(\rho) \neq$ $\exists \rho.\mathcal{A}^{\psi}_{\omega}(\rho) \land \mathcal{R}^{\psi}_{\omega}(\rho)$ (i.e., \exists does not distribute over \land). Thus, increasing precision in our verification task requires pointer analysis to be not only more precise (with longer calling-contexts) but also synergistic with control-flow reachability analysis.

Challenge 3: Pruning the Search Space. To achieve high precision, a fine abstraction of control-flow paths (e.g., with adequate context-sensitivity) is required, but at a risk for causing path explosion. Furthermore, the presence of a large number of deallocation-dereference (ψ, ω) pairs that need to be checked further exacerbates the problem. Pruning the search space without any loss of precision is essential.

Our Solution In this paper, we present a whole-program analysis approach that verifies TH-safety for each dereference ω . Specifically, ω is considered safe iff there exists no deallocation ψ such that the pair (ψ , ω) causes a dangling pointer dereference at ω .

To meet Challenge 1, we model this verification problem context-sensitively with three contexts. We identify an allocation o, a deallocation ψ (via pointer p) and a dereference ω (via pointer q) by a context tuple $(c_o, c_{\psi}, c_{\omega})$ so that $\langle\!\langle c_o, o \rangle\!\rangle$ represents a context-sensitive heap object, i.e, an object o created under c_o , (c_{ψ}, p) deallocates what is pointed to by p under c_{ψ} , and (ω, q) dereferences pointer q under context c_{ω} . We verify TH-safety with respect to (o, ψ, ω) by disproving the presence of a control-flow path that contains a context tuple, $(c_o, c_{\psi}, c_{\omega})$, such that $\langle\!\langle c_o, o \rangle\!\rangle$, once deallocated at (c_{ψ}, p) , is still accessed subsequently at (c_{ω}, q) along the path.

To meet Challenge 2, we introduce a demand-driven pointer analysis that automatically infers the context information in pointer aliases so that the resulting alias analysis can correlate with an associated control-flow reachability analysis as required. Given a pointer p at a deallocation (resp. a pointer q at a dereference) without any context given, our pointer analysis will infer a context c_{ψ} (resp. c_{ω}), together with a context-sensitive object $\langle\!\langle c_o, o \rangle\!\rangle$, such that the context-sensitive pointer (c_{ψ}, p) (resp. (c_{ω}, q)) points to $\langle\!\langle c_o, o \rangle\!\rangle$, implying that $\exists \rho. \mathcal{A}^{\psi}_{\omega}(\rho)$. In addition, c_{ψ} and c_{ω} are also required to satisfy the control-flow reachability constraint $\exists \rho. \mathcal{R}^{\psi}_{\omega}(\rho)$ simultaneously so that $\exists \rho. \mathcal{A}^{\psi}_{\omega}(\rho) \land \mathcal{R}^{\psi}_{\omega}(\rho)$ holds. This avoids false positives that satisfy $\mathcal{R}^{\psi}_{\omega}$ and $\mathcal{A}^{\psi}_{\omega}$ only for two distinct paths, respectively, which happens when $\exists \rho. \mathcal{A}^{\psi}_{\omega}(\rho) \land \exists \rho. \mathcal{R}^{\psi}_{\omega}(\rho) \neq$ $\exists \rho. \mathcal{A}^{\psi}_{\omega}(\rho) \land \mathcal{R}^{\psi}_{\omega}(\rho)$. Finally, points-to queries are raised on-demand by traversing precomputed def-use chains (in order to improve efficiency) and by supporting full contextsensitivity (modulo recursion) to transcend k-limiting (in order to improve precision).

To meet Challenge 3, we make our context-sensitive analysis adaptive. A context tuple $(c_o, c_{\psi}, c_{\omega})$ is reduced to $(c'_o, c'_{\psi}, c'_{\omega})$ if c_o, c_{ψ} and c_{ω} share a common prefix c_{pre} , so that $c_o = cons(c_{pre}, c'_o)$, $c_{\psi} = cons(c_{pre}, c'_{\psi})$, and $c_{\omega} = cons(c_{pre}, c'_{\omega})$, where cons denotes string concatenation. This adaptive analysis aims to reduce exponentially many prefixes starting from main (), which would otherwise significantly impede scalability.

Contributions This paper makes the following main contributions:

- We propose a fully automated approach to TH-safety verification on a per dereference basis, with a precise context-sensitive model, which enables a control-flow path to be abstracted by three contexts for its allocation, deallocation and dereference. This provides a balanced trade-off between precision and scalability.
- We present a static whole-program analysis that solves this three-point verification problem in the presence of both data-dependence and control-flow constraints. To this end, we develop a demand-driven pointer analysis with full context-sensitivity (modulo recursion) that automatically infers the context information required.
- We present an adaptive context-sensitive policy for TH-safety verification that automatically truncates redundant context prefixes without losing soundness or precision. This enables our approach to scale to some large real-world programs.
- We have implemented D³ in LLVM and evaluated it using a suite of 10 real-world programs. Our results show that D³ scales to hundreds of KLOC, with a capability of verifying 81.3% of all the 114,508 dereferences to be safe.

2 Preliminaries

We describe our techniques using a small language in Figure 1. Function definitions and statements are identified by their labels or line numbers. The language is standard. Pointers are propagated via copy (x = y), load (x = *y), store (*x = y) and address-taking (x = &y) statements; heap objects are allocated and deallocated by malloc() and free(), respectively; the callee of a function call $(x = fp(\vec{y}))$ is specified by

Program P ::=	F^+	Function F ::=	l def $f(\vec{x})$ { $S;$ }
Statement $S ::=$	${}^{l}x = y \mid {}^{l}x = *y \mid {}^{l}*x = y$	$y \mid {}^{l}x = \& y \mid {}^{l}x =$	malloc() $ ^{l}$ free(y)
	$ {}^{l}x = fp(\vec{y}) {}^{l}ret x {}^{l}t$	if (*) S_1 else S_2	$ $ ^{<i>l</i>} while (*) $S S_1; S_2$

Fig. 1. A small unmanaged imperative language.

a function pointer (fp) with its parameters (\vec{y}) passed by value (as in LLVM-IR); and ret, if and while represent standard return, branching and looping statements. As with previous work [11,57,38,36], we currently do not handle concurrent programs.

Inter-Procedural Control-Flow Graph (ICFG) This is a directed graph (N, E), where each node $n \in N$ represents a statement and each edge $e = (src, dst) \in E$ represents the control flow from statement src to statement dst. In particular, if e represents a function call/return, then e is labeled with the corresponding call-site ID κ .

Contexts Given any statement in function f, a *calling context* (or *context*, for short) $c = [\kappa_1, \kappa_2, ..., \kappa_n]$ is a sequence of n call-site IDs in their invocation order that uniquely specifies an abstract call-path to f on the ICFG of the program.

Allocation, Deallocation and Dereference A context-sensitive (abstract) *object*, denoted $\langle\!\langle c_o, o \rangle\!\rangle$, represents the set of concrete objects created at allocation site o under context c_o . We write $\psi(c_{\psi}, l_{\psi}, p)$ to signify a context-sensitive *deallocation* of the object pointed to by p at line l_{ψ} under context c_{ψ} . Similarly, a context-sensitive *dereference* $\omega(c_{\omega}, l_{\omega}, q)$ accesses the object pointed to by q at line l_{ω} under context c_{ω} . Context-insensitively, these are identified by $o, \psi(l_{\psi}, p)$ and $\omega(l_{\omega}, q)$, respectively.

Pointer Analysis A context-sensitive pointer analysis conservatively computes a function $pt_{cs} : C \times V \to 2^{C \times O}$ that relates each context-sensitive pointer $(c, v) \in C \times V$ to the set of context-sensitive objects $\langle\!\langle c_o, o \rangle\!\rangle \in C \times O$ pointed to by (c, v). A pointer analysis is formulated by a set of inference rules that can be solved using a standard fixed-point algorithm. Andersen-style [6] subset-based context-insensitive pointer analysis $pt : V \to 2^O$ is given in Figure 2. $\mathcal{P}[\![s]\!]$ denotes that s appears in program \mathcal{P} .

We consider only field-sensitive pointer analysis techniques. As with previous techniques [8,25,41,57], we assume that our programs are ANSI-compliant that are devoid of buffer overflows and data misalignments. Arrays are handled monolithically. Any access to a member of an array or struct object with a statically unknown offset is viewed to be a non-deterministic operation on the given object (soundly but imprecisely).

TH-Safety Violation A context-sensitive *TH-safety violation*, denoted $\langle \langle c_o, o \rangle \rangle$, $\psi(c_{\psi}, l_{\psi}, p), \omega(c_{\omega}, l_{\omega}, q) \rangle$, occurs when $\langle \langle c_o, o \rangle \rangle$, which is deallocated at l_{ψ} under c_{ψ} , is accessed later at l_{ω} under c_{ω} . Our context-insensitive notation is $\langle o, \psi(l_{\psi}, p), \omega(l_{\omega}, q) \rangle$.

3 Illustrating Examples

In Section 3.1, we explain why aliasing and control-flow reachability must be solved synergistically rather than separately in order to achieve high precision in our verification task, no matter how precise pointer analysis is. In Section 3.2, we describe how our synergistic approach works on top of a demand-driven pointer analysis, by taming path explosion with full context-sensitivity (modulo recursion) adaptively.

[Addr]-	$\frac{\mathcal{P}[\![x = \& y]\!]}{y \in pt(x)}$	[Alloc]—	$\frac{P[[^{o}x = \text{malloc}()]]}{o \in pt(x)}$	$[Copy] \frac{\mathcal{P}[\![x = y]\!]}{pt(y) \subseteq pt(x)}$		
[Load]—	$\mathcal{P}[x = *y]$ $pt(o) \subseteq pt($	$o \in pt(y)$	[Store]-	$\mathcal{P}[\![*x = y]\!]$ $pt(y) \subseteq$	$o \in pt(x)$	

Fig. 2. Andersen-style subset-based, flow- and context-insensitive pointer analysis [6]. Passing arguments into and returning results from functions are handled as copy statements.

1:	def alloc() {	8:	def Reach_But_N	oAlias()	{
2:	x=malloc(); $//o_2$	9:	a=alloc();	$//\kappa_9$,	$\langle\!\!\langle [\kappa_9], o_2 \rangle\!\!\rangle$
3:	ret x; }	10:	<pre>b = alloc();</pre>	$//\kappa_{10},$	$\langle\!\!\langle [\kappa_{10}], o_2 \rangle\!\!\rangle$
		11:	dealloc(a);	// κ_{11}	
4:	def dealloc(y) {	12:	deref(b);	// κ_{12}	
5:	free(y); $\} //\psi(l_5,y)$	13:	def Alias_But_N	oReach()	{
		14:	c=alloc();	$//\kappa_{14},$	$\langle\!\!\langle [\kappa_{14}], o_2 \rangle\!\!\rangle$
6:	def deref(z) {	15:	deref(c);	// κ_{15}	
7:	temp=*z; } // $\omega(l_7, z)$	16:	<pre>dealloc(c);</pre>	$ \} / / \kappa_{16} $	

(a) Safe code, with a dereference in line 7



(b) ICFG (with relevant edges given), showing that $\psi(l_5, y)$ reaches $\omega(l_7, z)$ on the blue path but $\psi(l_5, y)$ aliases with $\omega(l_7, z)$ on the orange path, implying that the dereference at l_7 is safe

Fig. 3. An example without any TH-safety violation.

3.1 Aliasing and Control-Flow Reachability: Separately or Synergistically

Figure 3(a) gives a program, in which $\psi(l_5, y)$ does not cause a TH-safety violation at $\omega(l_7, z)$ (Figure 3(b)). The wrappers, alloc(), dealloc() and deref(), allocate o_2 , deallocate the object pointed by y at $\psi(l_5, y)$ and dereference z at $\omega(l_7, z)$, respectively. In Reach_But_NoAlias(), $\langle\!\langle [\kappa_9], o_2 \rangle\!\rangle$ is first deallocated in l_{11} and then another object $\langle\!\langle [\kappa_{10}], o_2 \rangle\!\rangle$ is accessed indirectly in l_{12} . In Alias_But_NoReach(), $\langle\!\langle [\kappa_{14}], o_2 \rangle\!\rangle$ is first accessed indirectly in l_{15} and then deallocated in l_{16} .

If aliasing and control-flow reachability for $\psi(l_5, y)$ and $\omega(l_7, z)$ are solved separately, a TH-safety violation will be reported (but as a false positive), no matter how precise the underlying pointer analysis is used. As illustrated in Figure 3(b), aliasing (the orange path) and reachability (the blue path) happen along two different paths in the ICFG, and consequently, cannot be satisfied simultaneously in the same path.

To avoid false positives like this, aliasing and control-flow reachability must be solved together. In our synergistic approach, we identify o_2 , $\psi(l_5, y)$ and $\omega(l_7, z)$ by their respective contexts c_o, c_{ψ} and c_{ω} , and disprove the presence of a context tuple $(c_o, c_{\psi}, c_{\omega})$, such that $\langle\!\langle c_o, o_2 \rangle\!\rangle$ is first deallocated in l_5 under c_{ψ} and subsequently accessed in l_7 under c_{ω} along the same path. Therefore, our approach will report no TH-safety violation for this program. Note that any context-insensitive analysis that merges $\langle\!\langle [\kappa_9], o_2 \rangle\!\rangle$ and $\langle\!\langle [\kappa_{10}], o_2 \rangle\!\rangle$ into o_2 would report a false violation as $\langle o_2, \psi(l_5, y), \omega(l_7, z) \rangle$.

```
17: def foo() {

18: d=bar(); //\kappa_{18}

19: deref(d); }//\kappa_{19}

20: def bar() {

21: e=alloc(); //\kappa_{21}, \langle\!\langle [\kappa_{21}], o_2 \rangle\!\rangle

22: dealloc(e); //\kappa_{22}

23: ret e; }
```

28: dealloc (g); // κ_{28} 29: deref (g); }// κ_{29}

f = alloc(); $//\kappa_{25}$, $\langle\!\langle [\kappa_{25}], o_2 \rangle\!\rangle$

 $//\kappa_{26}$

def baz() {

27: def qux(g) {

 $qux(f); \}$

24:

25:

26:

(a) Allocation and deallocation (via wrappers) in the same function bar()

(b) Deallocation and dereference (via wrappers) in the same function qux()



Fig. 4. Two representative TH-safety violations caused by $\psi(l_5, y)$ and $\omega(l_7, z)$ appearing in Figure 3, where the three wrappers, alloc(), dealloc() and deref() are defined.

3.2 Synergizing Pointer Analysis and Control-Flow Reachability Analysis: On-Demand with Adaptive Context-Sensitivity

Let us illustrate our approach further by expanding Figure 3 into Figure 4 by examining how it detects two representative TH-safety violations caused now by $\psi(l_5, y)$ and $\omega(l_7, z)$ considered earlier. In Figure 4(a) (with its relevant ICFG given in Figure 4(c)), o_2 and $\psi(l_5, y)$ are reached transitively via the two call sites in the same function, bar (), which is called by foo(), in which $\omega(l_7, z)$ is reached via a call to deref() transitively. In Figure 4(b) (with its relevant ICFG given in Figure 4(d)), $\psi(l_5, y)$ and $\omega(l_7, z)$ are reached transitively via the two call sites in the same function, qux(), which is called by baz(), in which o_2 is reached via a call to alloc() transitively.

We will only discuss Figure 4(a) as Figure 4(b) can be understood similarly.

Verifying TH-Safety by Synergizing Pointer and Reachability Analyses On-Demand Our approach relies on pt_{cs}^{dd} , a demand-driven version of pointer analysis pt_{cs} introduced in Section 2. For Figure 4(a), we report a TH-safety violation $\langle \langle [\kappa_{18}, \kappa_{21}], o_2 \rangle \rangle$, $\psi([\kappa_{18}, \kappa_{22}], l_5, \gamma), \omega([\kappa_{19}], l_7, z) \rangle$. To obtain this, we check to see if y aliases z by querying pt_{cs}^{dd} for the points-to sets of y and z, i.e., $pt_{cs}^{dd}([], \gamma)$ and $pt_{cs}^{dd}([], z)$, respectively, where their initial unknown contexts [] will be eventually filled up by pt_{cs}^{dd} . On-demand, pt_{cs}^{dd} traces backwards the flow of objects along the pre-computed def-use chains (obtained by a pre-analysis) in the program. To compute $pt_{cs}^{dd}([], \gamma)$, for example, starting from l_5, pt_{cs}^{dd} traces back to l_4 where y is defined; moves to the call-site κ_{22} where y receives the value of e via parameter passing; reaches l_{21} where e is defined; encounters l_3 where x is returned (by entering alloc () from its exit at κ_{21}); and finally, arrives at l_2 where x is defined, giving rise to $\langle [\kappa_{21}], o_2 \rangle \in pt_{cs}^{dd}([\kappa_{22}], \gamma)$. Note that the initial unknown context [] has been inferred to be $[\kappa_{22}]$ as desired. This implies that $\langle [\kappa_{18}, \kappa_{21}], o_2 \rangle \in pt_{cs}^{dd}([\kappa_{18}, \kappa_{22}], \gamma)$. Similarly we obtain $\langle [\kappa_{18}, \kappa_{21}], o_2 \rangle \in$ $pt_{cs}^{dd}([\kappa_{19}], z)$. Thus, $\psi([\kappa_{18}, \kappa_{22}], l_5, y)$ aliases with $\omega([\kappa_{19}], l_7, z)$ (with y and z both pointing to $\langle\!\langle [\kappa_{18}, \kappa_{21}], o_2 \rangle\!\rangle$), and in addition, the former also reaches the latter along the same path identified by $[\kappa_{18}, \kappa_{21}], [\kappa_{18}, \kappa_{22}]$ and $[\kappa_{19}]$. As a result, our approach reports this violation as $\langle\!\langle [\kappa_{18}, \kappa_{21}], o_2 \rangle\!\rangle, \psi([\kappa_{18}, \kappa_{22}], l_5, y), \omega([\kappa_{19}], l_7, z) \rangle$.

Taming Path Explosion with Adaptive Context-Sensitivity In our approach, pt_{cs}^{dd} applies context-sensitivity adaptively without analyzing the callers of foo(), avoiding the possible path explosion that may occur between main() and foo() in Figure 4(c). Soundness is still guaranteed, since the context elements between main() and foo() do not affect the value-flows of $\langle [\kappa_{18}, \kappa_{21}], o_2 \rangle$ and are thus redundant. To see this, if we extend the two contexts in $\psi([\kappa_{18}, \kappa_{22}], l_5, y)$ and $\omega([\kappa_{19}], l_7, z)$ with two distinct prefixes, $[\kappa_{a1}]$ and $[\kappa_{a2}]$, we will fail to obtain any additional violation witness, since both are no longer aliased: $pt_{cs}^{dd}([\kappa_{a1}, \kappa_{18}, \kappa_{22}], y) = \{\langle [\kappa_{a1}, \kappa_{18}, \kappa_{21}], o_2 \rangle\} \neq \{\langle [\kappa_{a2}, \kappa_{18}, \kappa_{21}], o_2 \rangle\} = pt_{cs}^{dd}([\kappa_{a2}, \kappa_{19}], z)$. If we use the the same prefix instead, we will end up with a finer abstraction, yielding the results already subsumed.

4 Our Approach

The workflow of our four-stage approach is given in Figure 5. To start with (①), we perform a fast but imprecise pre-analysis for a program using Andersen's pointer analysis pt (Figure 2). Then (②), we build a value-flow graph to capture the flow of values across the program based on the points-to information obtained in the pre-analysis (Section 4.1). Next (③), we obtain the points-to set at each dereference by querying pt_{cs}^{dd} , a demand-driven version of pt_{cs} (discussed in Section 2) that now operates on the value-flow graph (Section 4.2). This way, pt_{cs}^{dd} will traverse pre-computed def-use chains rather than control-flow, achieving better efficiency. Finally (④), we verify absence of a TH-safety violation at a dereference by considering aliasing and control-flow reachability synergistically with adaptive context-sensitivity (Sections 4.3 and 4.4).



Fig. 5. The workflow of our approach on synergizing pointer analysis with reachability analysis.

4.1 Value-Flow Graph Construction

We construct a *value-flow graph* for a program, following [16,50,46], based on the points-to information discovered during the pre-analysis to capture the flow of values across the program. This entails building the def-use chains for its top-level variables (which are conceptually regarded as register variables) and address-taken variables (which are all referred to as memory objects or objects for short in this paper).

The def-use chains for top-level variables are readily available. However, those for address-taken variables (accessed indirectly at loads, stores and call sites) are implicit. To make such indirect memory accesses explicit, we resort to the rules in Figure 6. For an address-taken variable o, there are two types of annotations: $[[\mu(o)]]$, which represents a potential use of o, and $[[o = \chi(o)]]$, which represents both a potential definition and a

$[Mu] \underbrace{- \mathcal{P}\llbracket^l x = *y \rrbracket o \in pt(y)}_{\llbracket \mu(o) \rrbracket \in \Delta(l, \prec)}$	$[\text{Chi}] \frac{\mathcal{P}[\![{}^l \ast x = y]\!] o \in pt(x)}{[\![o = \chi(o)]\!] \in \Delta(l, \succ)}$
$ \begin{split} & \mathcal{P}[\![{}^{l}_{-} = fp(_)]\!] f \in pt(fp) \\ & \mathcal{P}[\![{}^{lf} \det f(_)\{\}]\!] l_{s} \in L(f) \\ & \underline{\ \mu(o)\ } \in \Delta(l_{s}, \prec) \\ \hline & \underline{\ \mu(o)\ } \in \Delta(l, \prec) [\![o = \chi(o)]\!] \in \Delta(l_{f}, \prec) \end{split} $	$ \begin{split} & \mathcal{P}[\![{}^l_{-}=fp(_)]\!] f\in pt(fp) \\ & \mathcal{P}[\![{}^{l_f}\det f(_)\{\}]\!] l_s\in L(f) \\ & \boxed{[\![o=\chi(o)]\!]\in \Delta(l_s,\times)} \\ \\ & \boxed{[\![\mu(o)]\!]\in \Delta(l,\prec) [\![o=\chi(o)]\!]\in \Delta(l_f,\prec)} \\ & \boxed{[\![\mu(o)]\!]\in \Delta(l_f,\times) [\![o=\chi(o)]\!]\in \Delta(l,\times)} \end{split} $

Fig. 6. Rules for adding two types of annotations, $[\![\mu(o)]\!]$ and $[\![o = \chi(o)]\!]$, to make explicit the accesses of a memory object *o*. L(f) denotes the set of statement labels in function *f*. $\Delta(l, \prec)$ and $\Delta(l, \succ)$ represent the sets of annotations added just before and after *l*, respectively.



Fig. 7. A program (referred to in Example 1 (annotations), Example 2 (value-flow edges) and Example 3 (pointer analysis)), decorated with μ and χ annotations and all the value-flow edges 1 - 9 that capture the flow of o_2 from bone in line 10 through to feedDog in line 16.

potential use of *o*. We define Δ : L × ORD $\rightarrow 2^{\text{ANNOT}}$, where ANNOT is the set of annotations (shown in brackets), L is the set of statement labels, and ORD = {<, >} indicates if an annotation appears immediately before (<) or after (>) a statement.

Let us go through the rules in Figure 6. For a load statement x = *y at l, if y points to o, then $\llbracket \mu(o) \rrbracket$ is added before l to indicate that o may be used at this load (Rule [Mu]). For a store statement *x = y at l, if x points to o, then $\llbracket o = \chi(o) \rrbracket$ is added after l to indicate that o (LHS) may be redefined in terms of o (RHS) in the case of a weak update and y at this store (Rule [Chi]). Rules [Ref] and [Mod] prescribe the standard inter-procedural MOD/REF analysis. Let a function f be defined at l_f and called at a call site l via a function pointer fp. Consider [Ref] first. If $\llbracket \mu(o) \rrbracket$ is annotated inside f, then $\llbracket \mu(o) \rrbracket$ is added before l (as o may be used in f directly or indirectly), and $\llbracket o = \chi(o) \rrbracket$ is added before f's definition at l_f (as o may be passed indirectly as a parameter to f). Consider [Mod] now. If $\llbracket o = \chi(o) \rrbracket$ is annotated inside f, then we add not only the same annotations at l and l_f as in [Ref], but also $\llbracket \mu(o) \rrbracket$ after l_f (as o may be returned to its call sites) and $\llbracket o = \chi(o) \rrbracket$ after l (as o may be modified at l_j .

Once a program has been annotated, its top-level variables and objects appearing in the annotations are put into SSA form [15], with their versions denoted in *superscripts*. **Example 1.** Let us see how to add o_5 -related annotations in Figure 7. For now, the value-flow edges shown are irrelevant. In line 8, $[o_5^2 = \chi(o_5^1)]$ is added after l_8 , i.e.,

$[\mathbf{D}^{\mathrm{T}}] \frac{\mathcal{P}[\![{}^{l}x = _]\!]}{l \in \mathcal{D}(x)} \qquad [\mathbf{U}_{\mathrm{Copy}}^{\mathrm{T}}] \frac{\mathcal{P}[\![{}^{l}_=x]\!]}{l \in \mathcal{U}(x)} \qquad [\mathbf{U}_{\mathrm{Copy}}^{\mathrm{T}}] \frac{\mathcal{P}[\![{}^{l}_=x]\!]}{l \in \mathcal{U}(x)}$	$\mathcal{V}_{\text{Load}}^{\text{T}}] \frac{\mathcal{P}[\![{}^{l}_{-} = *x]\!]}{l \in \mathcal{U}(x)} \qquad [U_{\text{Store}}^{\text{T}}] \frac{\mathcal{P}[\![{}^{l}_{-} *x = _]\!]}{l \in \mathcal{U}(x)}$
$[\boldsymbol{U}_{Addr}^{T}] \frac{\mathcal{P}[\![{}^{l}_{-} = \& x]\!]}{l \in \mathcal{U}(x)} [\boldsymbol{U}_{Free}^{T}] \frac{\mathcal{P}[\![{}^{l}_{free}(x)]\!]}{l \in \mathcal{U}(x)} [\boldsymbol{U}_{Call}^{T}]$	$]\frac{\mathcal{P}[\!\![^l_{-}=fp(\vec{x})]\!] x \in \vec{x}}{l \in \mathcal{U}(x)} [\mathbf{D}^{\mathrm{A}}]\frac{[\!\![o=_{-}]\!] \in \Delta(l, \succ)}{l^{^{>}} \in \mathcal{D}(o)}$
$[\mathrm{U}_{\chi}^{\mathrm{A}}] \frac{\llbracket_{-}=\chi(o)\rrbracket \in \Delta(l, \succ)}{l^{^{\times}} \in \mathcal{U}(o)} [\mathrm{U}_{\mu}^{\mathrm{A}}] \frac{\llbracket\mu(o)\rrbracket \in \Delta(l, \prec)}{l^{^{<}} \in \mathcal{U}(o)}$	$[VF^{Intra}] \frac{l_d \in \mathcal{D}(o) l_u \in \mathcal{U}(o) F(l_d) = F(l_u)}{\langle l_d, o \rangle \longrightarrow \langle l_u, o \rangle}$
$\begin{bmatrix} \mathcal{P}[\![{}^{l}_{-} = fp(\vec{x})]\!] & x_{i} \in \vec{x} y_{i} \in \vec{y} \\ \mathcal{P}[\![{}^{l}_{f} \det f(\vec{y}) \{\}]\!] & f \in pt(fp) \\ \hline \langle l, x_{i} \rangle \longrightarrow \langle l_{f}, y_{i} \rangle \end{bmatrix}$	$[\mathrm{VF}_{\mathrm{Ret}}^{\mathrm{T}}] \xrightarrow{\mathcal{P}} \begin{bmatrix} {}^{l}y = fp(_) \end{bmatrix} \begin{array}{c} f \in pt(fp) \\ \mathcal{P} \begin{bmatrix} {}^{l_{f}} \mathrm{def} f(_) \{ \dots {}^{l_{r}} \mathrm{ret} x; \} \end{bmatrix}}{\langle l_{r}, x \rangle \longrightarrow \langle l, y \rangle}$
$ \mathcal{P}[\![{}^{l}_{-} = fp(_)]\!] [\![\mu(o^{i})]\!] \in \Delta(l, \prec) $ $ \mathcal{P}[\![{}^{l}_{-} \det f(_)\{\}]\!] f \in pt(fp) $ $ [\![_= \chi(o^{j})]\!] \in \Delta(l_{f}, \prec) $	$\mathcal{P}\llbracket^{l}_{-} = fp(_) \rrbracket \llbracket \mu(o^{i}) \rrbracket \in \Delta(l_{f}, \succ)$ $\mathcal{P}\llbracket^{l_{f}} \det f(_) \{ \dots \} \rrbracket f \in pt(fp)$ $\llbracket_{-} = \chi(o^{j}) \rrbracket \in \Delta(l, \succ)$
$[VF_{Call}] \longrightarrow \langle l^{\prec}_{f}, o^{i} \rangle \longrightarrow \langle l^{\prec}_{f}, o^{j} \rangle$	$[VF_{Ret}] \xrightarrow{\qquad} \langle l_f^{h}, o^i \rangle \longrightarrow \langle l^{h}, o^j \rangle$

Fig. 8. Rules for building the value-flow graph $G_{\rm vfg}$ for an annotated program in SSA form (with the version of a SSA variable omitted when it is irrelevant to avoid cluttering). $\mathcal{D}(v)$ ($\mathcal{U}(v)$) denotes the set of definition (use) sites of a variable v. F(l) identifies the function containing l.

as 8⁵, in put () as pctn is found to point to o_5 by the pre-analysis in Figure 2 (Rule [Chi]). As a result, this inter-procedural MOD/REF effect needs to be reflected at its definition and call sites, by adding 7⁴, 7⁵, 14⁴, 14⁵, 15⁴, and 15⁵ (Rule [Mod]). In line 16, $[[\mu(o_5^2)]]$ is added before l_{16} since tray is found to point to o_5 (Rule [Mu]).

Given an annotated program in SSA form, we build its value-flow graph, $G_{vfg} = (L \times V, E)$, to capture the flow of values through its def-use chains and inter-procedural call/return edges, by using the rules in Figure 8 to construct its value-flow edges. We make use of two mappings, $\mathcal{D} : V \to 2^{L}$ and $\mathcal{U} : V \to 2^{L}$ that map a variable $v \in V$ to the set of its definition sites $l_{def} \in L$ and use sites $l_{use} \in L$, respectively. We write $\langle l_{src}, v \rangle \longrightarrow \langle l_{dst}, v' \rangle$ to denote the flow of a value initially in v at l_{src} to v' at l_{dst} . For a top-level variable $x \in V^{T}$, Rule $[D^{T}]$ adds the definition site l to $\mathcal{D}(x)$ and Rules $[U_{Copy}^{T}], [U_{Load}^{T}], [U_{Addr}^{T}], [U_{Free}^{T}]$ and $[U_{\alpha l}^{T}]$ simply collect its definition and use sites into $\mathcal{D}(o)$ and $\mathcal{U}(o)$, respectively. The last five rules construct the edges in G_{vfg} by connecting a definition site with all its use sites. $[VF_{ntra}^{Intra}]$ adds intra-procedural value-flow edges while other four add inter-procedural value-flow edges (with $[VF_{Call}^{T}]$ and $[VF_{Ret}^{R}]$ for top-level variables and $[VF_{Call}^{R}]$ and $[VF_{Ret}^{R}]$ for address-taken variables. Once G_{vfg} has been constructed, the SSA versions of a variable will be ignored.

Example 2. Figure 7 shows all the value-flow edges 1 - 9 capturing the flow of o_2 via fd, bone, pfd, o_5 and feedDog. We obtain these edges by applying the following rules (Figure 8): 1 for $\langle l_2, fd \rangle \longrightarrow \langle l_3, fd \rangle$ ($[VF^{Intra}]$); 2 for $\langle l_3, fd \rangle \longrightarrow \langle l_{10}, bone \rangle$ ($[VF^{T}_{Rel}]$); 3 for $\langle l_{10}, bone \rangle \longrightarrow \langle l_{14}, bone \rangle$ ($[VF^{Intra}]$); 4 for $\langle l_{14}, bone \rangle \longrightarrow \langle l_{10}, bone \rangle$ ($[VF^{T}_{Call}]$); 5 for $\langle l_7, pfd \rangle \longrightarrow \langle l_8, pfd \rangle$ and 6 for $\langle l_8^2, o_5^2 \rangle \longrightarrow \langle l_7^2, o_5^2 \rangle ([VF^{Intra}])$; 7 for $\langle l_7^2, o_5^2 \rangle \longrightarrow \langle l_{14}^2, o_5^2 \rangle$ ($[VF^{Intra}]$); and 8 for $\langle l_{14}^2, o_5^1 \rangle \longrightarrow \langle l_{15}^2, o_5^2 \rangle \longrightarrow \langle l_{16}^2, o_5^2 \rangle$ ($[VF^{Intra}]$).

In Figure 13 (Appendix A), we give a version of Figure 7 with all value-flow edges.

Fig. 9. Rules for demand-driven context-sensitive pointer analysis pt_{cs}^{dd} (with \diamond denoting a demand query issued and $n_{src} \rightsquigarrow n_{dst}$ denoting the flow of a value from n_{src} to n_{dst} on G_{vfg}).

4.2 Demand-Driven Context-Sensitive Pointer Analysis

Our context-sensitive pointer analysis pt_{cs}^{dd} operates on the value-flow graph G_{vfg} of a program. We write $pt_{cs}^{dd}(c,l,v) = \diamond$ to signify a demand query for the points-to set of variable v at statement l under context c. In the case of $pt_{cs}^{dd}([],l,v) = \diamond$ with an empty context [], pt_{cs}^{dd} will find all pointed-to objects $\langle\!\langle c_o, o \rangle\!\rangle\! \in pt_{cs}^{dd}(c,l,v)$, where c is also inferred automatically. This automatic context inference is essential for achieving high precision as it provides a mechanism for us to synergize alias and control-flow reachability analyses as needed. As $pt_{cs}^{dd}(c,l,v) = \diamond$ is solved on-demand (with possibly many other points-to queries raised along the way), by traversing backwards only the value-flow edges in G_{vfg} established on the fly, imprecision in G_{vfg} (due to spurious value-flow edges) will affect only the efficiency but not precision of pt_{cs}^{dd} .

Figure 9 gives the rules for answering $pt_{cs}^{dd}(c, l, v) = \diamondsuit$, where \leadsto , which is transitive by $[VF_{Trans}]$, represents the flow of a value across one or more value-flow edges in G_{vfg} actually traversed. Note that $\langle\!\langle c_o, o \rangle\!\rangle$ is essentially $\langle c_o, o, o \rangle$ since o is the line number for the corresponding allocation site. We say that x flows to y if $\langle \neg, \neg, x \rangle \rightsquigarrow \langle \neg, \neg, y \rangle$. To solve $pt_{cs}^{dd}(c, l, v) = \diamondsuit$, we solve $\diamondsuit \rightsquigarrow \langle c, l, v \rangle$, i.e., find

what flows to $\langle c, l, v \rangle$ (Rule [QRY]). If $\langle c_o, o \rangle$ flows to $\langle c, l, v \rangle$, then $\langle c, l, v \rangle$ points to $\langle c_o, o \rangle$ (Rule [PT]). If $\langle c, l, v \rangle$ has been reached, we need to continue exploring backwards what may flow to $\langle c, l, v \rangle$ on-demand (Rule [DD_{Back}]).

Rules $[VF_{Addr}]$ and $[VF_{Alloc}]$ handle allocation statements that allocate memory for an address-taken variable on the stack and in the heap, respectively.

For a load ${}^{l}x = *y$ with a query $\Leftrightarrow \rightsquigarrow \langle c, l, x \rangle$, pt_{cs}^{dd} first checks to see if $\langle \langle c_o, o \rangle \rangle \rightsquigarrow \langle c, l, y \rangle$ holds by issuing a demand query $\diamondsuit \rightsquigarrow \langle c, l, y \rangle$ (Rule [DD_{Load}]), and if this is the case, then $\langle c, l^{\checkmark}, \langle \langle c_o, o \rangle \rangle \rightsquigarrow \langle c, l, x \rangle$ is established (Rule [VF_{Load}]). Similarly, for a store ${}^{l}*x = y$ with a query $\diamondsuit \rightsquigarrow \langle c, l^{\succ}, \langle \langle c_o, o \rangle \rangle$, pt_{cs}^{dd} checks to see if $\langle \langle c_o, o \rangle \rangle \rightsquigarrow \langle c, l, x \rangle$ is established (Rule [DD_{Load}]), and if this is the case, then $\langle c, l, x \rangle \rightarrow \langle c, l^{\succ}, \langle c_o, o \rangle \rangle$, pt_{cs}^{dd} checks to see if $\langle \langle c_o, o \rangle \rangle \rightsquigarrow \langle c, l, x \rangle$ holds by issuing a demand query $\diamondsuit \rightsquigarrow \langle c, l, x \rangle$ (Rule [DD_{Store}]), and if this is the case, then $\langle c, l, y \rangle \rightsquigarrow \langle c, l^{\flat}, \langle c_o, o \rangle \rangle$ is established (Rule [VF_{Store}]).

Rules $[VF_{Copy}]$, $[VF^{T}]$ and $[VF^{A}]$ simply propagate values across assignments (with the former for copy statements and the latter two for def-use chains). In particular, $[VF^{A}]$ performs a weak update at a store. Note that pt_{cs}^{dd} is also flow-sensitive with strong updates performed for singleton objects as is standard [32,22,50].

To support the inter-procedural analysis at the function calls and returns, $[VF_{Call}^{I}]$ and $[VF_{Ret}^{T}]$ handle top-level variables while $[VF_{Call}^{A}]$ and $[VF_{Ret}^{A}]$ handle address-taken variables. Context-sensitivity is achieved by maintaining a context with push (\oplus) and pop (Θ) operations in a stack-like manner. When handling a function call at a call site l, a new context c^{-} is generated by popping off l from the current context c, denoted $c^{-} = c \Theta l$, to track the value-flow backwards outside the callee (c^{-}) from inside the callee (c). Conversely, when handling a callee function's return statement that returns to a call site l, a new context c^{+} is created by pushing l to the top of the current context c, denoted $c^{+} = c \oplus l$, to represent the fact that the backward analysis will now enter the callee (c^{+}) at its return statement from the call-site l outside the callee (c).

Example 3. Given $pt_{cs}^{dd}([], 16, \text{feedDog}) = \diamondsuit$ for the program in Figure 7, pt_{cs}^{dd} yields the following facts related to the nine value-flow edges marked as 1 - 9:

$\langle\!\langle [\kappa_{10}], o_2 \rangle\!\rangle$	$\leadsto \langle [\kappa_{10}], 2, fd \rangle$	$\xrightarrow{(1)} \langle [\kappa_{10}], 3, fd \rangle$
2 ₩ ([],10,bone	3/√ √[],14,bone	$\xrightarrow{(4)}_{\checkmark} \langle [\kappa_{14}], 7, \text{pfd} \rangle$
$\xrightarrow{5}$ $\langle [\kappa_{14}], 8, pfd \rangle$	$\rightsquigarrow \langle [\kappa_{14}], 8^{\succ}, \langle \langle [\kappa_{12}], o_5 \rangle$	$\langle \rangle \rangle \xrightarrow{[6]{}} \langle [\kappa_{14}], 7^{2}, \langle \langle [\kappa_{12}], o_{5} \rangle \rangle$
$\xrightarrow{[7]{}} \langle [], 14^{\scriptscriptstyle >}, \langle [\kappa_{12}], o_5 \rangle \rangle$	$\xrightarrow{(8)} \langle [], 15^{\flat}, \langle [\kappa_{12}], o_5 \rangle \rangle$	$\rangle \xrightarrow{(0)} \langle [], 16^{\checkmark}, \langle [\kappa_{12}], o_5 \rangle \rangle \xrightarrow{(0)} \langle [], 16, \text{feedDog} \rangle$

This means that $\langle\!\langle [\kappa_{10}], o_2 \rangle\!\rangle \rightsquigarrow \langle [], 16, \text{feedDog} \rangle$ by Rule [VF_{Trans}]. Finally, we can conclude that $\langle\!\langle [\kappa_{10}], o_2 \rangle\!\rangle \in pt_{cs}^{dd}([], 16, \text{feedDog})$ by Rule [PT].

In Appendix A, Table 2 gives a step-by-step trace of $pt_{cs}^{dd}([], 16, feedDog) = \diamondsuit$ when operating on Figure 13, a version of Figure 7 with a complete value-flow graph.

4.3 Synergizing Aliasing and Control-Flow Reachability

Given a pair of deallocation $\psi(l_{\psi}, p)$ and dereference $\omega(l_{\omega}, q)$, we proceed to prove absence of $\langle \langle c_o, o \rangle \rangle, \psi(c_{\psi}, l_{\psi}, p), \omega(c_{\omega}, l_{\omega}, q) \rangle$ on all the control-flow paths ρ across the ICFG of the program, where $c_{\psi} \in C_{\psi}$ and $c_{\omega} \in C_{\omega}$ are calling contexts for l_{ψ} and l_{ω} , respectively. We abstract ρ with a context tuple $(c_o, c_{\psi}, c_{\omega})$, which is shortened to (c_{ψ}, c_{ω}) , since c_o can be automatically inferred by pt_{cs}^{dd} from c_{ψ} and c_{ω} . Two properties

[AliasingAndReaching] $\frac{\mathcal{R}}{\mathcal{R}}$	$rac{\Delta a_{\omega}^{\psi}(c_{\psi},c_{\omega}) - \mathcal{A}_{\omega}^{\psi}(c_{\psi},c_{\omega})}{\mathcal{S}_{\omega}^{\psi}(c_{\psi},c_{\omega})}$
$pt_{cs}^{dd}(c_{\psi}, l_{\psi}, p) = \diamondsuit \vdash \langle\!\langle hc_{\psi}, o \rangle\!\rangle \in pt(c)$ $pt_{cs}^{dd}(c_{\omega}, l_{\omega}, q) = \diamondsuit \vdash \langle\!\langle hc_{\omega}, o \rangle\!\rangle \in pt(c)$ $cons(_, hc_{\psi}) = hc_{\omega} \lor (cons(_, hc_{\omega}) = \mathcal{A}_{\omega}^{\psi}(c_{\psi}, c_{\omega})$	$\frac{c_{\psi}, l_{\psi}, p)}{c_{\omega}, l_{\omega}, q)} = \frac{\overline{l_{\psi}} = car(cons(c_{\psi}, l_{\psi}))}{\overline{l_{\omega}} = car(cons(c_{\omega}, l_{\omega}))}$ $\frac{R_{Intra}(\overline{l_{\psi}}, \overline{l_{\omega}})}{\mathcal{R}_{\psi}^{\psi}(c_{\psi}, c_{\omega})}$

Fig. 10. Rules for synergizing aliasing and control-flow reachability.

are checked context-sensitively: (1) aliasing, $\mathcal{A}_{\omega}^{\psi} : C_{\psi} \times C_{\omega} \to \{true, false\}$, indicating if (c_{ψ}, p) aliases (c_{ω}, q) , and (2) reachability, $\mathcal{R}_{\omega}^{\psi} : C_{\psi} \times C_{\omega} \to \{true, false\}$, indicating if l_{ψ} reaches l_{ω} on the ICFG by going through first the return edges specified by c_{ψ} and then the call edges specified by c_{ω} . We consider aliasing and reachability together, $\mathcal{S}_{\omega}^{\psi} : C_{\psi} \times C_{\omega} \to \{true, false\}$, by requiring $\mathcal{A}_{\omega}^{\psi}$ and $\mathcal{R}_{\omega}^{\psi}$ to be satisfied for the same context pair (c_{ψ}, c_{ω}) . We report a TH-safety violation at the dereference iff $\mathcal{S}_{\omega}^{\psi}$ is satisfied, thereby avoiding false-positives that satisfy both constraints on two different paths only.

Figure 10 gives our rules. Rule [Aliasing] computes an abstract path, (c_{ψ}, c_{ω}) , on which p aliases q. Note that $\langle\!\langle hc_{\psi}, o \rangle\!\rangle$ and $\langle\!\langle hc_{\omega}, o \rangle\!\rangle$ may represent the same (concrete) object if one of these two contexts is a suffix of (i.e., coarser than) the other. Rule [Reaching] computes an abstract path, (c_{ψ}, c_{ω}) , on which l_{ψ} reaches l_{ω} , which happens if l_{ψ} first reaches $\overline{l_{\psi}}$ inter-procedurally via the return edges specified by c_{ψ} , then $\overline{l_{\psi}}$ reaches $\overline{l_{\omega}}$ intra-procedurally in the same function (denoted $\mathcal{R}_{Intra}(\overline{l_{\psi}}, \overline{l_{\omega}})$), and finally, $\overline{l_{\omega}}$ reaches l_{ω} inter-procedurally via the call edges specified by c_{ω} .

4.4 Adaptive Context-Sensitivity

To guarantee soundness, all context pairs $(c_{\psi}, c_{\omega}) \in C_{\psi} \times C_{\omega}$ in the program must be considered, making [Aliasing] in Figure 10 prohibitively costly to verify. To tame path explosion, we use the two rules in Figure 11 instead with adaptive context-sensitivity, thereby reducing significantly the number of context pairs considered without losing soundness or precision. We explain these two rules, illustrated in Figure 12, below.

The key insight behind is that $pt_{cs}^{dd}([], l, v)$, when asked to compute the points-to set of (l, v) with an empty context [], which represents an abstraction of all possible contexts (from main ()), will return $\langle\!\langle hc, o \rangle\!\rangle \in pt_{cs}^{dd}(c, l, v)$, where the contexts c and hc are automatically inferred. In particular, c and hc are appropriately k-limited (with any unnecessary context prefix c_{pre} from main () truncated), since

$pt_{cs}^{dd}([],l,v) = \Leftrightarrow \vdash \langle \langle hc, o \rangle \rangle \in pt_{cs}^{dd}(c,l,v) \iff$	$\langle cons(c_{pre}, hc), o \rangle \in pt_{cs}^{dd}(cons(c_{pre}, c), l, v)$
--	---

In [Aliasing], there are three possibilities for $\langle\!\langle hc_{\psi}, o \rangle\!\rangle$ and $\langle\!\langle hc_{\omega}, o \rangle\!\rangle$ to be aliases: (1) $hc = hc_{\psi} = hc_{\omega}$. This case, illustrated in Figure 12(a), is handled by [Aliasing-

EqHeapCtx], which says that it suffices to consider only $(\overline{c_{\psi}}, \overline{c_{\omega}})$ by removing any common prefix c_{pre} from c_{ψ} and c_{ω} , since $(\overline{c_{\psi}}, \overline{c_{\omega}})$ is coarser than (c_{ψ}, c_{ω}) . In addition, all context pairs $(cons(c_{pre}^1, c_{\psi}), cons(c_{pre}^2, c_{\omega}))$, where $c_{pre}^1 \neq c_{pre}^2$, can also

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	$pt_{cs}^{dd}(\fbox{1}, l_{\psi}, p) = \Leftrightarrow \vdash \langle \langle hc, o \rangle \rangle \in pt_{cs}^{dd}(c_{\psi}, l_{\psi}, p)$ $pt_{cs}^{dd}(\fbox{1}, l_{\omega}, q) = \Leftrightarrow \vdash \langle \langle hc, o \rangle \rangle \in pt_{cs}^{dd}(c_{\omega}, l_{\omega}, q)$	$egin{aligned} c_\psi &= cons(c_{pre}, \overline{c_\psi}) \ c_\omega &= cons(c_{pre}, \overline{c_\omega}) \end{aligned}$
[/masing-Eqreapetx]	$\mathcal{A}^\psi_\omega(\overline{c_\psi},\overline{c_\omega})$	
	$pt_{cs}^{cd}([1], l_{\psi}, p) = \Leftrightarrow \vdash \langle \langle hc_{\psi}, o \rangle \rangle \in pt_{cs}^{cd}(c_{\psi}, l_{\psi}, p)$	$\overline{c_{\psi}} = cons(c_{pre}, c_{\psi})$
[Aliasing-NeqHeapCtx]	$= \frac{pt_{cs}^{-}([]], l_{\omega}, q) = \diamondsuit \vdash \langle \langle hc_{\omega}, o \rangle \rangle \in pt_{cs}^{-}(c_{\omega}, l_{\omega}, q)}{\mathcal{A}_{\omega}^{\psi}(\overline{c_{\omega}}, c_{\omega})}$	$hc_{\omega} = cons(c_{pre}, hc_{\psi})$



Fig. 11. Two rules for replacing [Aliasing] in Figure 10 with adaptive context-sensitivity.

Fig. 12. An illustration of the two rules in Figure 11, where a fat dot represents a function and an arrow represents a sequence of (transitive) function calls across the functions in the program.

be soundly removed, since $\langle cons(c_{pre}^1, hc), o \rangle$ is not aliased with $\langle cons(c_{pre}^2, hc), o \rangle$. By construction, $car(cons(\overline{c_{\psi}}, l_{\psi}))$ and $car(cons(\overline{c_{\omega}}, l_{\omega}))$ are guaranteed to be in the same function, allowing $\mathcal{R}^{\psi}_{\omega}$ in [Reaching] to be checked trivially.

(2) $hc_{\omega} = cons(c, hc_{\psi})$. To check \Re_{ω}^{ψ} in [Reaching] efficiently, [Aliasing-NeqHeapCtx], as shown in Figure 12(b), constructs $\overline{c_{\psi}}$ by extending c_{ψ} such that $car(cons(\overline{c_{\psi}}, l_{\psi}))$ and $car(cons(c_{\omega}, l_{\omega}))$ reside in the same function. As in [Aliasing-EqHeapCtx], all context-pairs $(cons(c_{pre}, \overline{c_{\psi}}), cons(c_{pre}^2, c_{\omega}))$, where $c_{pre}^1 \neq c_{pre}^2$, are ignored soundly. In addition, $car(cons(\overline{c_{\psi}}, l_{\psi}))$ and $car(cons(c_{\omega}, l_{\omega}))$ always reside in the same function, allowing \Re_{ω}^{ψ} in [Reaching] to be checked trivially as above.

(3) $hc_{\psi} = cons(c, hc_{\omega})$. This case, which indicates a use-before-free, is always safe.

Our approach D^3 is adaptive since its search space exploration selects calling contexts with appropriate lengths adaptively without losing soundness or precision.

Example 4. Let us apply our rules to Figure 4(a) to detect the TH-safety violation $\langle \langle [\kappa_{18}, \kappa_{21}], o_2 \rangle \rangle, \psi([\kappa_{18}, \kappa_{22}], l_5, y), \omega([\kappa_{19}], l_7, z) \rangle$. Consider [Aliasing-NeqHeapCtx] first. For the two points-to queries $pt_{cs}^{dd}([], l_5, y) = \Diamond$ and $pt_{cs}^{dd}([], l_7, z) = \Diamond$ issued, we obtain $\langle [\kappa_{21}], o_2 \rangle \in pt_{cs}^{dd}([\kappa_{22}], l_5, y)$ and $\langle [\kappa_{18}, \kappa_{21}], o_2 \rangle \in pt_{cs}^{dd}([\kappa_{19}], l_7, z)$. As $hc_{\omega} = [\kappa_{18}, \kappa_{21}] = cons([\kappa_{18}], [\kappa_{21}]) = cons(c_{pre}, hc_{\psi})$, we have $\overline{c_{\psi}} = cons(c_{pre}, c_{\psi}) = [\kappa_{18}, \kappa_{21}]$. By [Aliasing-NeqHeapCtx], $\mathcal{A}^{\psi}_{\omega}([\kappa_{18}, \kappa_{21}], [\kappa_{19}])$ holds. Let $\overline{l_{\psi}} = \kappa_{18}$ and $\overline{l_{\omega}} = \kappa_{19}$. By [Reaching], $\mathcal{R}^{\psi}_{\omega}([\kappa_{18}, \kappa_{21}], [\kappa_{19}])$ holds. By [Aliasing-NeqHeapCtx], $\mathcal{A}^{\psi}_{\omega}([\kappa_{18}, \kappa_{21}], [\kappa_{19}])$ holds.

4.5 Soundness

For a program P considered in Section 2, D^3 (Figure 5) is sound. First, G_{vfg} constructed for P, based on the rules in Figure 8, over-approximates the flow of any value in P as Andersen's analysis (Figure 2) is sound. Second, pt_{cs}^{dd} (Figure 9) is sound as it

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over-approximates the points-to information in P. Third, we suppress a TH-safety violation warning soundly according to [AliasingAndReaching] (Figure 10). Finally, our adaptive analysis (Figure 11) is sound as the context pairs (c_{ψ}, c_{ω}) pruned for [AliasingAndReaching] during the search space exploration are redundant (Section 4.4).

5 Evaluation

We strive to show that D^3 can accomplish our TH-safety verification task for reasonably large C programs efficiently with good precision in the context of the prior work.

5.1 Methodology

We have implemented D^3 in the open-source program analysis framework, SVF [51], which is implemented in LLVM [30]. Given a program, its source files are first compiled individually into LLVM IR by the Clang compiler front-end, before linked together into a single whole-program IR file by the LLVM Gold Plugin. Our TH-safety verification task is then performed statically on the whole-program LLVM IR file.

Two sets of benchmark are used. One set consists of 138 test cases with the ground truth for use-after-free vulnerabilities (CWE-416) from the NIST Juliet Test Suite for C [1], which are all TH-safety violations extracted from real-world scenarios, with one per test case. The other set consists of 10 popular open-source C programs (with 40 - 260 KLOC) given in Table 1, containing a total of 114,508 pointer dereferences.

We compare D^3 with a C bounded model checker, CBMC (version 5.11) [29]. CBMC, as confirmed by the authors, does not provide an option to verify TH-safety only by disabling other types of memory errors. Thus, we have configured it with the "pointercheck" option to detect all pointer-related errors and then manually extracted all the TH-safety violations reported. For the small test cases in the NIST Juliet Test Suite, loops are not bounded. For the 10 real-world programs, loops are unwound by using "unwind 2" to accelerate termination (at the expense of losing soundness).

Infer [10] (i.e., Abductor earlier [11]) has evolved into a bug detector by sacrificing soundness, with its older verification-oriented versions no longer available (as confirmed by its authors). So we will not compare such separation-logic-based verifiers, as Infer, for example, will now lower its false positive rate by tolerating for false negatives.

In addition, we also evaluate D^3 against a version of D^3 , denoted D^{SEP} , for which aliasing and control-flow reachability are considered separately.

As pt_{cs}^{dd} is demand-driven, the time budget for a points-to query issued from [Aliasing] (Figure 11) is set to be a maximum of 10,000 value-flow edges traversed. On time out, pt_{cs}^{dd} will fall back to the result computed by Andersen's pointer analysis, pt, soundly (Figure 2). We have done our experiments on a machine with a 3.5 GHz Intel Xeon 16-core CPU and 256 GB memory, running Ubuntu OS (version 16.04 LTS). The analysis time of a program is the average of five runs. For D^3/D^{SEP} , the analysis times from all its stages (Figure 5) are included, except the pre-analysis, since Andersen's analysis is expected to be reused by many other static analyses for the program.

5.2 Results and Analysis

5.2.1 Juliet Test Suite: Soundness Both CBMC and D^3 report soundly all the 138 use-after-free bugs without any false positives. Each test case is small, with a few hundreds of LOC, costing less than one second to verify by either tool.

Program	Chara	cteristics	Value-Fl	ow Graph		D ^{SEP}			D	1	
Fiogram	KLOC	#Derefs	#Nodes	#Edges	Time (s)	#Safe	%Safe	Time (s)	#Safe	%Safe	%Impr
a2ps-4.14	65	12,601	35,201	58,255	428	7,000	55.6%	5,653	9,944	78.9%	52.6%
cpio-2.12	94	5,211	13,486	23,379	10	3,805	73.0%	180	4,964	95.3%	82.4%
ctags-5.8	42	14,628	56,320	152,846	54	10,538	72.0%	520	14,014	95.8%	85.0%
MCSim-6.0.1	60	8,718	17,914	28,365	64	5,233	60.0%	1,010	8,105	93.0%	82.4%
parted-3.2	138	1,493	7,703	16,415	9	1,133	75.9%	14	1,371	91.8%	66.1%
patch-2.7.6	88	5,334	16,926	35,269	50	4,065	76.2%	480	4,961	93.0%	70.6%
sendmail-8.15	260	21,536	128,312	328,892	1,332	12,368	57.4%	3,277	15,570	72.3%	34.9%
tar-1.31	191	11,671	54,594	109,269	225	7,741	66.3%	7,672	9,200	78.8%	37.1%
tmux-2.8	54	24,877	91,373	185,594	166	12,366	49.7%	12,295	18,266	73.4%	47.2%
wget-1.20	174	8,439	31,460	63,738	100	5,957	70.6%	1,920	6,746	79.9%	31.8%
Avg.	117	11,451	45,329	100,202	244	7,021	65.7%	3,302	9,314	85.2%	59.0%
Total	1,166	114,508	453,289	1,002,022	2,438	70,206	61.3%	33,022	93,141	81.3%	51.8%

Table 1. Results for verifying 10 open-source C programs. D^{SEP} is a version of D^3 with aliasing $\mathcal{A}^{\psi}_{\omega}$ and reachability $\mathcal{R}^{\psi}_{\omega}$ checked separately. %Impr is computed as $\frac{D^3.#Safe-D^{SEP}.#Safe}{#Deref-D^{SEP}.#Safe} \times 100\%$.

5.2.2 10 Open-Source Programs: Precision and Scalability For any of these programs, CBMC, which is bounded by even "unwind 2", cannot terminate within a 1-day time budget. We have decided to evaluate D^3 against a version, D^{SEP} , in which both aliasing and control-flow reachability are considered separately, as shown in Table 1. **Precision.** For a total of 114,508 dereferences in the 10 programs, D^3 proves success-

fully 81.3% (or $\frac{93,141}{114,508}$) to be safe. This translates into an average of 85.2% per program, ranging from 72.3% in sendmail to 95.8% for ctags. In contrast, D^{SEP} finds only 61.3% of all the dereferences to be safe, with an average of 65.7% per program, ranging from 49.7% for tmux to 76.2% for patch.

 D^3 is significantly more precise than D^{SEP} (as measured by %Impr). For a total of 44,302 dereferences that cannot be verified to be safe by D^{SEP} , D^3 recognizes 51.8% of these (i.e., $\frac{22,935}{44,302}$) as being safe. The largest improvements are observed for ctags (85.0%), cpio (82.4%) and MCSim (82.4%), which contain many cases as in Figure 3, causing D^{SEP} to fail but D^3 to succeed, since aliasing and reachability must be considered together. On the other hand, the precision improvements for wget (31.8%) and sendmail (34.9%), where linked lists are heavily used, are the least impressive. **Scalability.** For a program, the size of its value-flow graph affects the time complexity of our approach. D^3 scales reasonably well to these programs, spending a total of 33,022 seconds on analyzing a total of 1,166 KLOC, while D^{SEP} is faster (finishing in 2,438 seconds) but less precise. For sendmail (the largest with 260 KLOC), D^3 takes 3,277 seconds to complete. For ctags (the smallest with 42 KLOC), D^3 finishes in 520

seconds. D^3 is the fastest for parted, which has the smallest value-flow graph with the smallest number of dereferences. D^3 is the slowest for tmux, which has the second largest value-flow graph with the largest number of dereferences.

6 Related Work

As a static verifier, D^3 differs fundamentally from static bug detectors that trade soundness for precision. In designing D^3 , it appears crucial to synergize aliasing and reach-

ability analyses to achieve high precision while maintaining soundness. In comparison with separation-logic-based approaches that emphasize compositional and modular reasoning, D^3 is demand-driven, by analyzing also only the code relevant to a TH-safety query (although it can be accelerated by a fast but imprecise pre-analysis).

Pointer Analysis Substantial progress has been made for whole-program [35,26,49] and demand-driven [23,48,52] pointer analyses, with flow-sensitivity [22,34], call-site-sensitivity [42,60], object-sensitivity [39,55] and type-sensitivity [47,28]). These recent advances in both precision and scalability have resulted in their widespread adoption in detecting memory bugs [3,21], such as memory leaks [13,53], null dereferences [38,36], uninitialized variables [59,37] and buffer overflows [33,14], and typestate verification [20,16]. Recent pointer-analysis-based tools [46,56] can detect TH-safety violations with low false-positive rates, but at the expense of missing true bugs. In contrast, D^3 is designed to be a verifier for finding TH-safety violations with good precision soundly by considering aliasing and control-flow reachability synergistically.

Separation Logic As an extension of Hoare logic for heap-manipulating programs, separation logic [44] provides the basis for a long line of research on memory safety verification. At its core is the separating conjunction * that splits the heap into disjoint heaplets, allowing program reasoning to be confined in heaplets [58,19]. For separation-logic-based verification, scalability has considerably improved with techniques like biabduction at the expense of sacrificing some precision [11,57], leading to industrial-strength tools such as Microsoft's SLAyer [8] and Facebook's Infer [10]. By giving up also some soundness, many industrial-strength static analyzers, such as Clang Static Analyzer [5,45] and Infer (the current release 0.15.0) are bug detectors, which reduce false positives at the expense of exhibiting false negatives as well. Unlike separation-logic-based approaches that support compositional and modular reasoning, D³ takes a pointer-analysis-based approach by analyzing also only the relevant code on-demand.

Model Checking Model checking represents a powerful framework for reasoning about a wide range of properties [27]. To analyze pointer-intensive C programs, model checkers like SLAM [7] and BLAST [24] rely on pre-computed pointer analysis. However, as pointed out in [29], model checking still suffers from limitations in fully automated TH-safety verification for large-sized programs, partly due to complex pointer aliasing. *Dynamic Analysis* TH-safety violations can be detected soundly and completely at runtime by enforcing full (i.e., both spatial and temporal) memory safety with program instrumentation [41]. To avoid high overheads (116% [41]), weaker security policies, including various flavors of control-flow integrity [2], have been proposed. Whenever a TH-safety violation is detected, the execution of the program is aborted to protect against exploits. Alternatively, one can resort to safe allocators [9,4], which disallow deallocated heap chunks from being reused, to mitigate memory corruption errors.

7 Conclusion

This paper presents D^3 , a novel approach for addressing the TH-safety verification problem based on a demand-driven context-sensitive pointer analysis. D^3 achieves its precision (by considering both aliasing and control-flow reachability simultaneously) and scalability (with adaptive context-sensitivity). In future work, we plan to empower D^3 by also considering (partial) path-sensitivity and shape analysis.

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A Tracing a Points-to Query

In Example 3, we provide a partial trace of $pt_{cs}^{dd}([], 16, feedDog) = \&$ for the program given in Figure 7, explaining how to infer $\langle\!\langle [\kappa_{10}], o_2 \rangle\!\rangle \in pt_{cs}^{dd}([], 16, feedDog)$ by restricting us to the \rightsquigarrow facts obtained for the nine value-flow edges shown. Here, we give a full trace for obtaining this pointed-to object in Table 2, including the \rightsquigarrow facts obtained for all the value-flow edges traversed in the complete value-flow graph of this program given in Figure 13.



Fig. 13. The program given in Figure 7 decorated with all the value-flow edges.

For the step-by-step trace in Table 2, we intend to highlight the following aspects:

(1) Value-Flow Transitivity. The flow of $\langle\!\langle [\kappa_{10}], o_2 \rangle\!\rangle$ into $\langle\!\langle [], 16, \text{feedDog} \rangle\!\rangle$, i.e., $\langle\!\langle [\kappa_{10}], o_2 \rangle\!\rangle \rightsquigarrow \langle\!\langle [], 16, \text{feedDog} \rangle\!\rangle$, discussed in Example 3, is obtained by Steps #11 - #13 - #32 - #34 - #36 - #51 - #53 - #55 - #57 - #59 - #61 - #63.

(2) Generating Demand Points-to Queries. In addition to $pt_{cs}^{dd}([], 16, feedDog) =$ \Leftrightarrow , the other demand queries \Leftrightarrow are issued in by firing (1) Rule [DD_{Back}] (e.g., Steps #4, #6 and #8) to start a new backward traversal, and (2) Rules [DD_{Load}] and [DD_{Store}] (e.g., Steps #2 and #19) at a load or store statement to resolve a dereferenced pointer.

(3) Context-sensitivity. Starting with $pt_{cs}^{dd}([], 16, \text{feedDog}) = \diamond$, i.e., $\diamond \rightsquigarrow \langle [], 16, \text{feedDog} \rangle$ at Step #1, we obtain $\langle [\kappa_{12}], o_5 \rangle \sim \langle [], 16, \text{tray} \rangle$ in Steps #2 – #10. There are two call sites, κ_{14} and κ_{15} , for put (). Once we know what tray points to, we can enter put () backwards from its exit at line 7[>] in two different ways, depending on whether it is called from κ_{15} or κ_{14} or not.

By performing Steps #11 – #18 (with the assumption that put () is called from κ_{15}), we reach line 8, where we issue a demand query at Step #19,

Alternatively, after having performed Steps #32 – #37 (with the assumption that put () is called from κ_{14}), we reach line 8 again, where we issue another query at Step #38, $\Leftrightarrow \rightsquigarrow \langle [\kappa_{14}], 8, \text{pctn} \rangle$. This time, however, we obtain $\langle [\kappa_{12}], o_5 \rangle \rightsquigarrow \langle [\kappa_{14}], 8, \text{pctn} \rangle$, i.e., at the end of Steps #38 – #50. By completing Steps #51 – #64, as already demonstrated in Example 3, we obtain $\langle [\kappa_{10}], o_2 \rangle \in pt_{cs}^{dd}([], 16, \texttt{feedDog})$.

Step #	~~~*	Rule	Step #	~~~*	Rule
1	$\diamond \rightsquigarrow \langle [], 16, feedDog \rangle$	[QRY]	33	$ \diamondsuit \rightsquigarrow \langle [], 14^{\flat}, \langle \langle [\kappa_{12}], o_5 \rangle \rangle \rangle $	[DD _{Back}
2	$\diamond \rightsquigarrow \langle [], 16, tray \rangle$	[DD _{Load}]	34	$ \langle [\kappa_{14}], 7^{\flat}, \langle \! \langle [\kappa_{12}], o_5 \rangle \! \rangle \rangle \leadsto \langle [], 14^{\flat}, \langle \! \langle [\kappa_{12}], o_5 \rangle \! \rangle \rangle $	$[VF_{Ret}^A]$
3	$\langle [], 12, tray \rangle \rightsquigarrow \langle [], 16, tray \rangle$	[VF ^T]	35	$ \diamondsuit \rightsquigarrow \langle [\kappa_{14}], 7^{\flat}, \langle \! \langle [\kappa_{12}], o_5 \rangle \! \rangle \rangle $	[DD _{Back}]
4	$\diamond \rightsquigarrow \langle [], 12, tray \rangle$	[DD _{Back}]	36	$\langle [\kappa_{14}], 8^{\diamond}, \langle [\kappa_{12}], o_5 \rangle \rangle \longrightarrow \langle [\kappa_{14}], 7^{\diamond}, \langle [\kappa_{12}], o_5 \rangle \rangle$	[VF ^A]
5	$\langle [\kappa_{12}], 6, \operatorname{ctn} \rangle \rightsquigarrow \langle [], 12, \operatorname{tray} \rangle$	$[VF_{Ret}^T]$	37	$ \diamondsuit \rightsquigarrow \langle [\kappa_{14}], 8^{\diamond}, \langle [\kappa_{12}], o_5 \rangle \rangle \rangle $	[DD _{Back}]
6	$\diamond \rightsquigarrow \langle [\kappa_{12}], 6, \operatorname{ctn} \rangle$	[DD _{Back}]	38	$\diamond \rightsquigarrow \langle [\kappa_{14}], 8, \texttt{pctn} \rangle$	[DD _{Store}]
7	$\langle [\kappa_{12}], 5, \operatorname{ctn} \rangle \leadsto \langle [\kappa_{12}], 6, \operatorname{ctn} \rangle$	[VF ^T]	39	$\langle [\kappa_{14}], 7, \texttt{pctn} \rangle \leadsto \langle [\kappa_{14}], 8, \texttt{pctn} \rangle$	$[VF^T]$
8	$\diamond \rightsquigarrow \langle [\kappa_{12}], 5, \operatorname{ctn} \rangle$	[DD _{Back}]	40	$\diamond \rightsquigarrow \langle [\kappa_{14}], 7, \texttt{pctn} \rangle$	[DD _{Back}
9	$\langle\!\!\langle [\kappa_{12}], o_5 \rangle\!\!\rangle \leadsto \langle [\kappa_{12}], 5, \operatorname{ctn} \rangle$	[VF _{Alloc}]	41	$\langle [], 14, tray \rangle \rightsquigarrow \langle [\kappa_{14}], 7, pctn \rangle$	$[VF_{Call}^T]$
10	$\langle\!\langle [\kappa_{12}], o_5 \rangle\!\rangle \rightsquigarrow \langle [], 16, tray \rangle$	[VF _{Trans}]	42	$\diamond \rightsquigarrow \langle [], 14, tray \rangle$	[DD _{Back}
11	$ \langle [], 16^{\checkmark}, \langle \! \langle [\kappa_{12}], o_5 \rangle \! \rangle \rangle \leadsto \langle [], 16, \texttt{feedDog} \rangle $	[VF _{Load}]	43	$\langle [], 12, tray \rangle \rightsquigarrow \langle [], 14, tray \rangle$	$[VF^T]$
12	$\Leftrightarrow \leadsto \langle [], 16^{<}, \langle [\kappa_{12}], o_5 \rangle \rangle \rangle$	[DD _{Back}]	44	$\diamond \rightsquigarrow \langle [], 12, \texttt{tray} \rangle$	[DD _{Back}]
13	$\langle [], 15^{\diamond}, \langle [\kappa_{12}], o_5 \rangle \rangle \leadsto \langle [], 16^{\diamond}, \langle [\kappa_{12}], o_5 \rangle \rangle$	[VF ^A]	45	$\langle [\kappa_{12}], 6, \operatorname{ctn} \rangle \rightsquigarrow \langle [], 12, \operatorname{tray} \rangle$	$[VF_{Ret}^T]$
14	$ \diamondsuit \rightsquigarrow \langle [], 15^{\diamond}, \langle \langle [\kappa_{12}], o_5 \rangle \rangle \rangle $	[DD _{Back}]	46	$\diamond \rightsquigarrow \langle [\kappa_{12}], 6, \operatorname{ctn} \rangle$	[DD _{Back}]
15	$\langle [\kappa_{15}], 7^{\rangle}, \langle \langle [\kappa_{12}], o_5 \rangle \rangle \longrightarrow \langle [], 15^{\rangle}, \langle \langle [\kappa_{12}], o_5 \rangle \rangle$	[VF ^A _{Ret}]	47	$\langle [\kappa_{12}], 5, \operatorname{ctn} \rangle \leadsto \langle [\kappa_{12}], 6, \operatorname{ctn} \rangle$	$[VF^T]$
16	$ \diamondsuit \rightsquigarrow \langle [\kappa_{15}], 7^{\diamond}, \langle [\kappa_{12}], o_5 \rangle \rangle \rangle $	[DD _{Back}]	48	$\diamond \rightsquigarrow \langle [\kappa_{12}], 5, \operatorname{ctn} \rangle$	[DD _{Back}]
17	$ \langle [\kappa_{15}], 8^{\scriptscriptstyle >}, \langle \! \langle [\kappa_{12}], o_5 \rangle \rangle \leadsto \langle [\kappa_{15}], 7^{\scriptscriptstyle >}, \langle \! \langle [\kappa_{12}], o_5 \rangle \! \rangle \rangle $	[VF ^A]	49	$\langle\!\langle [\kappa_{12}], o_5 \rangle\!\rangle \rightsquigarrow \langle [\kappa_{12}], 5, \operatorname{ctn} \rangle$	[VF _{Alloc}]
18	$\Leftrightarrow \leadsto \langle [\kappa_{15}], 8^{\flat}, \langle \! \langle [\kappa_{12}], o_5 \rangle \! \rangle \rangle$	[DD _{Back}]	50	$\langle\!\langle [\kappa_{12}], o_5 \rangle\!\rangle \leadsto \langle [\kappa_{14}], 8, \texttt{pctn} \rangle$	[VF _{Trans}]
19	$\diamond \rightsquigarrow \langle [\kappa_{15}], 8, \texttt{pctn} \rangle$	[DD _{Store}]	51	$\langle [\kappa_{14}], 8, pfd \rangle \rightsquigarrow \langle [\kappa_{14}], 8^{\diamond}, \langle [\kappa_{12}], o_5 \rangle \rangle$	[VF _{Store}]
20	$\langle [\kappa_{15}], 7, \texttt{pctn} \rangle \leadsto \langle [\kappa_{15}], 8, \texttt{pctn} \rangle$	[VF ^T]	52	$\diamond \rightsquigarrow \langle [\kappa_{14}], 8, pfd \rangle$	[DD _{Back}]
21	$\diamond \rightsquigarrow \langle [\kappa_{15}], 7, \texttt{pctn} \rangle$	[DD _{Back}]	53	$\langle [\kappa_{14}], 7, pfd \rangle \rightsquigarrow \langle [\kappa_{14}], 8, pfd \rangle$	[VF ^T]
22	$\langle [], 15, bowl \rangle \rightsquigarrow \langle [\kappa_{15}], 7, pctn \rangle$	$[VF_{Call}^T]$	54	$\diamond \rightsquigarrow \langle [\kappa_{14}], 7, pfd \rangle$	[DD _{Back}]
23	$\diamond \rightsquigarrow \langle [], 15, bowl \rangle$	[DD _{Back}]	55	$\langle [], 14, bone \rangle \rightsquigarrow \langle [\kappa_{14}], 7, pfd \rangle$	$[VF_{Call}^T]$
24	$\langle [], 13, bowl \rangle \rightsquigarrow \langle [], 15, bowl \rangle$	[VF ^T]	56	♦ ~~→ ([],14,bone>	[DD _{Back}]
25	$\diamond \rightsquigarrow \langle [], 13, \texttt{bowl} \rangle$	[DD _{Back}]	57	$\langle [], 10, bone \rangle \rightsquigarrow \langle [], 14, bone \rangle$	[VF ^T]
26	$\langle [\kappa_{13}], 6, \operatorname{ctn} \rangle \rightsquigarrow \langle [], 13, \operatorname{bowl} \rangle$	$[VF_{Ret}^T]$	58	♦ ~~→ ([], 10, bone)	[DD _{Back}]
27	$\diamond \leadsto \langle [\kappa_{13}], 6, \texttt{ctn} \rangle$	[DD _{Back}]	59	$\langle [\kappa_{10}], 3, fd \rangle \rightsquigarrow \langle [], 10, bone \rangle$	$[VF_{Ret}^T]$
28	$\langle [\kappa_{13}], 5, \operatorname{ctn} \rangle \rightsquigarrow \langle [\kappa_{13}], 6, \operatorname{ctn} \rangle$	$[VF^T]$	60	$\diamond \rightsquigarrow \langle [\kappa_{10}], 3, fd \rangle$	[DD _{Back}]
29	$\diamond \rightsquigarrow \langle [\kappa_{13}], 5, \operatorname{ctn} \rangle$	[DD _{Back}]	61	$\langle [\kappa_{10}], 2, fd \rangle \rightsquigarrow \langle [\kappa_{10}], 3, fd \rangle$	[VF ^T]
30	$\langle\!\langle [\kappa_{13}], o_5 \rangle\!\rangle \rightsquigarrow \langle [\kappa_{13}], 5, \operatorname{ctn} \rangle$	[VF _{Alloc}]	62	$\diamond \rightsquigarrow \langle [\kappa_{10}], 2, fd \rangle$	[DD _{Back}]
31	$\langle\!\langle [\kappa_{13}], o_5 \rangle\!\rangle \rightsquigarrow \langle [\kappa_{15}], 8, \text{pctn} \rangle$	[VF _{Trans}]	63	$\langle\!\langle [\kappa_{10}], o_2 \rangle\!\rangle \rightsquigarrow \langle [\kappa_{10}], 2, \mathrm{fd} \rangle$	[VF _{Alloc}
32	$\langle [], 14^{\flat}, \langle \langle [\kappa_{12}], o_5 \rangle \rangle \leadsto \langle [], 15^{\flat}, \langle \langle [\kappa_{12}], o_5 \rangle \rangle \rangle$	[VF ^A]	64	$\langle\!\langle [\kappa_{10}], o_2 \rangle\!\rangle \rightsquigarrow \langle [], 16, feedDog \rangle$	[VF _{Trans}]

Table 2. A step-by-step trace of $pt_{cs}^{dd}([], 16, \text{feedDog}) = \diamondsuit$, for computing $\langle\!\langle [\kappa_{10}], o_2 \rangle\!\rangle \in pt_{cs}^{dd}([], 16, \text{feedDog})$, with pt_{cs}^{dd} operating on the value-flow graph of the program in Figure 13 by applying the rules given in Figure 9.