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Short-term traffic prediction under non-recurrent incident conditions integrating data-driven models and traffic simulation

--Manuscript Draft--

Full Title:	Short-term traffic prediction under non-recurrent incident conditions integrating data-driven models and traffic simulation
Abstract:	<p>Predicting the traffic condition in urban networks is a priority for all traffic management centers around the world. This becomes very challenging especially when the network is affected by traffic incidents which vary in both time and space. Although data-driven machine learning (ML) modeling can be considered as an ideal tool for short-term traffic predictions, its performance is severely degraded when little historical traffic information is available under non-recurrent incident conditions. This paper addresses this challenge by integrating both data-driven and traffic simulation modeling. Instead of directly predicting the traffic states using limited historical data, we apply data-driven models to reinforce the traffic microsimulation. More explicitly, we employ ML models to predict origin-destination (OD) demand flows based on historical day-to-day demand flows. The traffic simulation uses the freshly reported incident information and the predicted OD demand flows obtained from ML models to forecast the future traffic states under non-recurrent incident conditions. Since accurate OD flows cannot directly measured in large-scale areas, we propose an OD demand rolling-horizon estimation problem to estimate demand flows based on the most recent measured link volumes. Results show that Decision Tree method outperforms other ML models in OD demand flow prediction. Finally, we showcase the capability of the proposed data-driven enforced traffic simulation platform for incident impact analysis in a real -life sub-network from Sydney, Australia.</p>
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2 **conditions integrating data-driven models and traffic simulation**

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1 ABSTRACT

2 Predicting the traffic condition in urban networks is a priority for all traffic management
3 centers around the world. This becomes very challenging especially when the network is
4 affected by traffic incidents which vary in both time and space. Although data-driven
5 machine learning (ML) modeling can be considered as an ideal tool for short-term traffic
6 predictions, its performance is severely degraded when little historical traffic information is
7 available under non-recurrent incident conditions. This paper addresses this challenge by
8 integrating both data-driven and traffic simulation modeling. Instead of directly predicting
9 the traffic states using limited historical data, we apply data-driven models to reinforce the
10 traffic microsimulation. More explicitly, we employ ML models to predict origin-destination
11 (OD) demand flows based on historical day-to-day demand flows. The traffic simulation uses
12 the freshly reported incident information and the predicted OD demand flows obtained from
13 ML models to forecast the future traffic states under non-recurrent incident conditions. Since
14 accurate OD flows cannot directly measured in large-scale areas, we propose an OD demand
15 rolling-horizon estimation problem to estimate demand flows based on the most recent
16 measured link volumes. Results show that Decision Tree method outperforms other ML
17 models in OD demand flow prediction. Finally, we showcase the capability of the proposed
18 data-driven enforced traffic simulation platform for incident impact analysis in a real –life
19 sub-network from Sydney, Australia.

20
21 **Keywords:** *demand estimation and prediction, micro-simulation, incident impact*
22 *management*

1 INTRODUCTION

2 Short-term traffic forecasting is a necessary step for efficient network operations and is an
3 integral part of Intelligent Transportation System (ITS) applications. The abundance and
4 recent increase of various traffic data sources have led many researchers and data scientists
5 to employ a wide range of data-driven models to predict future traffic conditions. There are
6 various parametric and non-parametric methods for the short-term forecast of speed (1, 2),
7 travel time (3–5), and traffic volume (6, 7), which offer a prediction in the range of a few
8 minutes to a few hours into the future. However, two challenges are highlighted in the
9 previous studies as the main critical limitations of the majority of data-driven models (8).
10 Firstly, the majority of data-driven forecasting models have been applied to freeways or
11 arterial corridors rather than regular urban networks. The complex spatial configuration of
12 all network connections and the dynamics of the travel demand makes the traffic forecasting
13 in urban networks very challenging, particularly for large suburban networks. Secondly, an
14 important challenge is the wide variability of traffic incidents that can occur at different times
15 of the day, rarely in the same location or with the same severity. These incidents can range
16 from temporary lane closures due to car breakdowns and small-scale accidents to more
17 complicated ones such as sudden weather changes and train system breakdowns. All these
18 varying characteristics of traffic disruptions increase the complexity of forecasting and make
19 it almost impossible to find similar patterns in any historical dataset. To address this issue,
20 some studies focus only on a particular type of incidents (9) or for example on highway lane
21 closures due to roadway reconstruction projects (10, 11). However, in most cases, there is
22 limited recorded data for each particular type of incident, and thus, forecasting traffic
23 measurements such as traffic volume, speed, or travel time can result in inaccurate outcomes.
24 On a parallel research track, an approach to predict the traffic state incorporating incidents is
25 using reliable traffic assignment models (12–14). In these models, each traveler attempts to
26 minimize his/her travel time/cost and their decision will impact the other travelers' decisions
27 to move in the network (15). By considering this essential principle, the intricate traveler
28 route decisions can be modeled in the traffic network. Moreover, the propagation of traffic
29 along the network is replicated by traffic flow theories that determine the traffic flows and
30 the associated travel times on network links (16). However, the traffic assignment models
31 require several demand and supply inputs which should be predicted as well for operational
32 applications (17).

33 In this paper, instead of directly predicting the link traffic features using only historical data,
34 we use data-driven models to reinforce a traffic micro-simulation by providing the required
35 inputs. In our proposed framework, once an incident is categorized as severe by an AI-engine
36 (18), a summary of incident characteristics such as the location and the number of affected
37 lanes is transferred to the traffic simulation. Moreover, a machine learning method predicts
38 short-term OD demand flows and feeds them to the traffic simulator. With knowledge of the

1 incident information and predicted OD demand flows, the simulator applies traffic flow
2 principles to predict the traffic state under non-recurrent incident conditions.

3 We make the assumption that network commuters hardly cancel their short-term trips even
4 if affected by disruptions. This assumption holds particularly for morning peak hours in
5 which a large proportion of trips like home-to-work or home-to-education still need to
6 continue. The travelers mainly respond to a new prevailing bad network condition by
7 updating/changing their route trips. Such behavioral phenomena can be modeled accurately
8 in traffic simulations. We propose a rolling horizon bi-level optimization model to keep the
9 traffic simulation model calibrated based on the most recent measured traffic data. To
10 summarize, we present our main contributions for this paper as:

- 11 - A dynamic OD estimation problem is formulated and solved to keep the traffic
12 simulation updated based on the most recent measured traffic data. The estimated day-
13 to-day OD flows are archived for the OD demand prediction module.
- 14 - Several machine learning models are deployed for OD demand prediction to reinforce
15 the traffic simulator.
- 16 - A prototype for an integrated incident management platform is developed to make use
17 of data-driven and dynamic traffic simulation modelling.
- 18 - The impacts of traffic incidents are investigated for a real application in an urban sub-
19 network.

20 The rest of the paper is organized as follow: Section 2 describes the methodology applied
21 over a real sub-network in Sydney, Australia and Section 3 showcases the results. Finally,
22 Section 4 provides the concluding remarks and outlines some research extensions for future
23 studies.

24 **METHODOLOGY**

25 *1.1. Incident management platform*

26 In this section, we explain the general data flow used for building an operational incident
27 management platform tailored to the needs of the Traffic Management Center in Sydney,
28 Australia. Figure 1 presents the proposed incident impact analysis platform using integrated
29 data-driven and traffic simulation models. The methodological diagram treats the cases of
30 recurrent versus non-recurrent incidents differently, by triggering various modules detailed
31 here below.

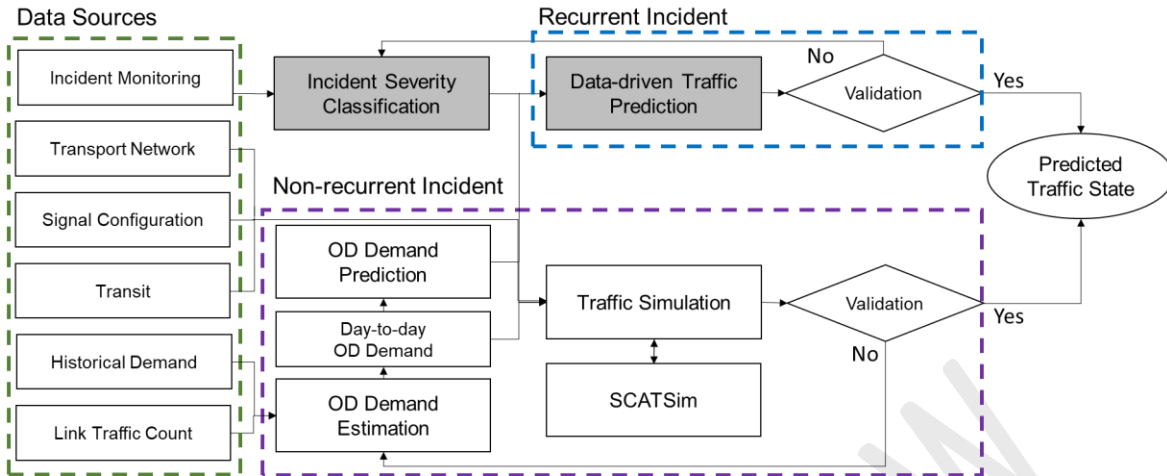


Figure 1. Data-driven and simulation platform for incident impact analysis. The gray modules are beyond the scope of this paper.

Our proposed framework is based on various data types including:

- **measured link traffic count:** Link traffic counts are essential inputs for the OD demand estimation module as well as to validate the framework's output.
- **supply/demand data:** which contains the primary information of the links of the network, public transport lines and their frequency, and signal configuration. This data is exported and used to construct the simulation model once offline.
- **incident data logs:** includes the incident location ([x,y] coordinates), the number of affected lanes, the start time of the incident, the incident duration and more details about the incident severity.

By having such information, the proposed framework predicts traffic state in two streams of recurrent and non-recurrent conditions using the following modules:

- **Incident severity classification:** This module includes raw data processing and uses machine learning techniques to classify reported incidents into severe and non-severe. When an incident is categorized as a severe incident, its data is transferred to the traffic simulation model for further impact analysis. For non-severe incidents, the data-driven traffic model is used for short traffic prediction, This module is not a focus of this study and readers can refer to our previous work (18).
- **Data-driven traffic prediction:** This module is based on our previous study (19) which proposed a deep learning methodology for travel speed prediction involving feature generation, model development, and model deployment. The proposed neural network model is used for recurrent incident conditions.
- **OD demand estimation:** the purpose of this module is to adjust a-priori demand data by using link traffic observations. We estimate the OD flows through a bilevel optimization

1 framework in which the a-priori demand flow is updated based on the latest measured
2 traffic in several links of the network.

- 3 • **OD demand prediction:** The demand prediction model will forecast the OD trip flows for
4 short time intervals into the future (up to an hour ahead) by using the OD demand flows
5 obtained by the OD demand estimation module.
- 6 • **Traffic simulation:** is used to understand the allocation of the predicted OD demand flows
7 with consideration of the freshly reported incident information. The outputs of the traffic
8 microsimulation are: travel times, link traffic volumes, delay and so on.
- 9 • **SCATSIM:** is a simulator plug-in which responds to the simulated traffic state by
10 changing: a) the total cycle times inside each SCATS-controlled intersection, b) the ratio
11 of the cycle time assigned to each phase and c) the offset between adjacent signal controls.
12 As a result, the real-life SCATS control logic is applied to the simulated vehicles in the
13 simulator which offers a realistic replication of real-world traffic control conditions.
- 14 • **Validation:** the inputs of the simulation model are regulated by the updated traffic
15 measurements observed consistently from the network at each time-interval, in order to
16 ensure the predicted results reflect the actual real-life conditions. If the error between the
17 predicted and the corresponding observed values is less than an acceptable threshold
18 defined in NSW traffic modelling guidelines (20), then we accept the outputs of the
19 platform as the final predicted traffic state.

20 1.2. Demand estimation and prediction

21 The success of the traffic simulation relies on the quality of this fundamental input and how
22 well it captures the travelers' movement in the city from one-time interval to another.
23 Accurate demand flow information is difficult to obtain directly and normally it is estimated
24 based on link traffic measurements (21). The main objective of the OD demand estimation
25 problem is to minimize the error between the simulated and the observed traffic
26 measurements. Many studies apply a bi-level optimization formulation where demand flows
27 are estimated in the upper-level and the feedback of estimated demand in the network is
28 evaluated by a lower-level traffic assignment model (22). Some relevant works for dynamic
29 OD estimation problems are conducted in the literature such as a) using advanced traffic
30 surveillance data to improve the accuracy of estimated OD flows (23), b) proposing
31 methodological enhancements to deal with nonlinearity problem in congested networks (24,
32 25), and c) applying simultaneous adjustment of supply and demand parameters to consider
33 the complex interactions of demand and supply components (26).

34 Dynamic OD demand estimation based on traffic measurements is often performed offline
35 for planning and operational applications. However, the offline procedure is not sufficient
36 for real-time traffic management applications. The offline demand flow estimation problem
37 requires measured traffic data, while in the real-time applications, the model should be able

1 to predict the traffic data actively for the near future. Offline dynamic OD estimation provides
2 a reliable initial OD demand for online applications to estimate the OD flows within a
3 reasonable computational time (27).
4 The OD demand estimation problem is expressed as a system of equations in which the
5 unknown parameters are OD flows and each equation represents the observed link flow. In
6 this study, we used a bi-level optimization problem in which the OD demand flows are
7 estimated by solving the system of equations in the upper level, and the estimated OD
8 demands are evaluated in the lower level. In addition to reducing the Euclidean distance
9 between simulated and observed traffic data, the objective function seeks to keep the
10 estimated demand as close as possible to the initial demand. In this way the solution does not
11 explore the local optima far from the initial demand flows. Our optimization OD demand
12 estimation problem is mathematically expressed as follows:

$$\min F(X) = \omega \cdot \sum_{i=1}^I \sum_{t=0}^T f(\hat{x}_i^t, x_i^t) + (1 - \omega) \cdot \sum_{a=1}^A \sum_{t=0}^T f(\hat{y}_a^t, y_a^t) \quad (1)$$

$$y_a^t = \sum_{\tau=1}^t \sum_{i=1}^I p_{a,i}^{\tau,t}(X) x_i^{\tau}$$

13 where each parameter is explained here below:

- f Euclidean distance function,
- a Link index, $a \in [1, A]$, A is the total number of observed links in the network
- t, τ Time index $t, \tau \in [1, T]$, T is the total number of modeling discrete times,
- i OD pair index $i \in [1, I]$, I is the total number of OD pairs in the network,
- \hat{x}_i^t Estimated demand flow for an OD pair $i \in I$ at time t ,
- x_i^t Initial demand flow for an OD pair $i \in I$ at time t ,
- \hat{X} Estimated demand vector, $\hat{X} = [\hat{x}_1^1, \hat{x}_2^1, \hat{x}_3^1, \dots, \hat{x}_I^1, \dots, \hat{x}_{I-1}^T, \hat{x}_I^T]$
- \hat{y}_a^t Estimated link flow in link a at time $t \in T$,
- y_a^t Observed link flow in link a at time $t \in T$,
- $p_{a,i}^{\tau,t}$ Assignment proportion of x_i^t that passes through a link a during time period τ ,
- ω Reliability weight for the demand deviation.

14 To solve the problem in Eq.(1, the partial derivative of function F with respect to the demand
15 flow for the OD pair η at time h (x_η^h $h \in [0, T]$, $\eta \in I$) is determined as follows:

$$\frac{\partial F}{\partial x_\eta^h} = \frac{\partial}{\partial x_\eta^h} \left(\omega \sum_{t=1}^T \sum_{i \in I} (x_i^t - \hat{x}_i^t)^2 + (1 - \omega) \sum_{a=1}^A \sum_{t=1}^T (y_a^t - \hat{y}_a^t)^2 \right) \quad (2)$$

$$= 2\omega(x_\eta^h - \hat{x}_\eta^h) + 2(1 - \omega) \left(\sum_{a=1}^M \sum_{\tau=h}^T p_{a,\eta}^{\tau,h}(X^*) \left(\sum_{t=1}^{\tau} \sum_{i \in I} p_{a,i}^{\tau,t}(X^*) x_i^t - \hat{y}_a^\tau \right) \right)$$

1 In addition to determining of the gradient, we also need to calculate the step size (λ). To do
 2 so, the sub-optimization problem in Eq.3 is solved in each iteration:

$$3 \min_{\lambda} F\left(X + \frac{\partial F}{\partial x} \lambda\right) \quad (3)$$

4
 5 We use the golden section algorithm, as a line search minimization solution for solving the
 6 sub-optimization problem defined in Eq.(3). The algorithm includes the following steps:

7 Step 1: if $\lambda^* \in [0,1], \zeta = 0, \varrho = 1, \lambda_1 = \psi, \lambda_2 = 1 - \psi$ where $\psi = \frac{\sqrt{5}-1}{2}$

8 Step 2: if $F\left(X + \frac{\partial F}{\partial x} \lambda_1\right) > F\left(X + \frac{\partial F}{\partial x} \lambda_2\right)$

9 $\zeta = \lambda_2, \lambda_2 = \lambda_1, \varrho = \varrho, \lambda_1 = \psi$

10 if $F\left(X + \frac{\partial F}{\partial x} \lambda_1\right) < F\left(X + \frac{\partial F}{\partial x} \lambda_2\right)$

11 $\zeta = \zeta, \varrho = \lambda_1, \lambda_1 = \lambda_2, \lambda_2 = \varrho - \psi$

12 Step 3: if $\zeta - \varrho < \varepsilon$ then: $\lambda^* = \frac{\zeta + \varrho}{2}$; otherwise, go to, step 2.

13 With the knowledge of the gradient $\left(\frac{\partial F}{\partial x_\eta^\tau}\right)$ and the step size (λ), the demand flow (\hat{x}_η^τ) is then
 14 updated as:

$$15 \hat{x}_\eta^\tau = x_\eta^\tau + \lambda \frac{\partial F}{\partial x_\eta^\tau} x_\eta^\tau \quad (4)$$

16 The proposed OD demand estimation model is performed in two stages. First, we execute the
 17 procedure offline to estimate OD demands for a typical weekday. In this stage, an initial static
 18 OD demand obtained from the strategic model is used to estimate sixteen 15-minute OD
 19 demand matrices for a 4-hour simulation during peak hours. Second, the time-dependent OD
 20 demand matrices estimated from the first stage are adjusted in a rolling-horizon estimation
 21 procedure based on the most recent observed traffic counts. As a result, the simulation model
 22 is kept updated in real-time using the newly observed data. Moreover, the estimated OD
 23 demand flows are archived for different days of the week. The archived demand is considered
 24 as a reliable training demand set for any demand prediction module. Let the current time be
 25 't'. Then, the demand prediction model has to predict demand flow for the next time intervals
 26 (\hat{x}_i^{t+1}) given the value of the 'm+l' previous demand flow values ($\hat{x}_i^{t-m}, \dots, \hat{x}_i^{t-1}, \hat{x}_i^t$). Thus,
 the prediction model is expressed as:

$$\hat{x}_i^t = P(\hat{x}_i^t, \hat{x}_i^{t-1}, \dots, \hat{x}_i^{t-m}, t) \quad (5)$$

1 For building this OD demand prediction module, we use different predictors which are
2 presented in the next sections.

3 *1.3. Data-driven models*

4 In this section, we provide a brief description of various algorithms that we used for demand
5 flow prediction, among which we cite: support vector machines (SVM), decision trees (DT),
6 and autoregressive moving average (ARMA).

7 *Support Vector Machines*

8 Support vector machines (SVM) in statistical learning theory have been widely applied for
9 solving classification and regression problems (28). In general, SVM is a well-established
10 prediction method in complex systems which can deal with noisy databases (29). The SVM
11 model is formulated as a constrained optimization problem specified in Eq.(6). The problem
12 consists of two conflicting objectives: minimizing the Euclidean distance of ω to increase the
13 margin and reducing the instance margin violations (ξ_i). Constant C makes a balance between
14 the two objective terms. A small value for hyper-parameter C allows a higher generalization
15 ability while a big C value enforces serious penalty to limit instances (in our application
16 demand flow x_i^t) that violate the determined margin.

$$\underset{\omega, b}{\text{minimize}} \quad 0.5 \omega^T \cdot \omega + C \sum_{i=1} \xi_i \quad (6)$$

so that:

$$\xi_i = \begin{cases} |\omega \cdot \Gamma(x_i^t) + b - x_i^t| - \varepsilon & |\omega \cdot \Gamma(x_i^t) + b - x_i^t| \geq \varepsilon \\ 0 & |\omega \cdot \Gamma(x_i^t) + b - x_i^t| < \varepsilon \end{cases}, \forall i$$

17
18 where Γ is a transformation function that can be replaced with a kernel function. Different
19 kernel functions such as linear, polynomial, Gaussian radial basis function (RBF), and
20 Sigmoid are commonly used in SVM modelling (28). Regardless of the kernel functions used,
21 the main goal is to estimate the value of coefficients of ω and b in the Eq.(6). To do this, the
22 parameters C , ε , and ξ should first be defined. Once they are determined, there will be a
23 global optimal solution found for the convex Problem Eq.(6) to obtain ω and b values. In
24 Section 2.2, we explore different values to find the best combination for our application.

1 *Decision Trees*

2 Decision Trees (DT) are versatile non-parametric supervised ML algorithms that are capable
3 of fitting complex datasets. Decision Trees are considered as white box models because their
4 decisions are intuitive and easy to interpret. This algorithm is also widely used in both
5 classification and regression (28). The following cost function is minimized to determine the
6 subsets and their thresholds:

7

$$J = \frac{m_{left}}{m} G_{left} + \frac{m_{right}}{m} G_{right}$$

$$G = 1 - \sum_{k=1}^n p_k^2 \quad (7)$$

$\begin{cases} G_{left/right} & \text{the impurity measurement of the left/right subset,} \\ m_{left/right} & \text{the number of examples in the left/right subset.} \end{cases}$

8 where p_k is the ratio of subset k among the training data. If all training instances belong to
9 the same subset then the impurity measurement would equal to zero ($G=0$). In this study, the
10 Classification and Regression Tree (CART) algorithm is employed (30). The algorithm splits
11 various instances into several subsets and defines a threshold. The CART algorithm
12 investigates greedily for the optimum split thresholds from the top level and continues the
13 process to lower levels. The algorithm stops splitting once it reaches the maximum depth for
14 the decision (regression) tree, or the impurity measurements are not reduced by splitting the
15 instances.

16 *ARMA*

17 We used the ARIMA model as a traditional time series model only for the demand prediction
18 (not for the incident classification). The ARMA-family models include an autoregressive
19 (AR) and a moving average (MA) part. The models predict the main variable for one or more
20 discrete time intervals by using the time-lagged values. Therefore, the historical variation of
21 the variable along with subtle time series dynamics is handled. The ARMA model with “ p
22 autoregressive terms” and “ q moving-average terms” takes the following form:

$$\phi(L)x_i^t = \theta(L)\epsilon^t + \delta \quad (8)$$

23 where $\phi(L)$ and $\theta(L)$ are respectively the autoregressive operator on variables and the
24 autoregressive operator on residuals, L is the backshift (lag) operator ($Lx_i^t = x_i^{t-1}$), ϵ_t
25 represents the residuals between the real and the estimated variable at time t , and δ is a
26 constant. $\theta(L)$ and $\phi(L)$ can be presented as a polynomial relationship in the lag operator,
27 defined as:

$$\begin{aligned}\theta(L) &= 1 - \theta_1 L - \dots - \theta_q L^q, \\ \phi(L) &= 1 - \phi_1 L - \dots - \phi_p L^p\end{aligned}\tag{9}$$

1 Consequently, if Eq.(9) is replaced in Eq.(8), we have:

$$(1 - \phi_1 L - \dots - \phi_p L^p)x_i^t = (1 - \theta_1 L - \dots - \theta_q L^q)\epsilon^t + \delta\tag{10}$$

2 Producing an ARMA model requires defining parameters p and q in order to specify $\theta(L)$
 3 and $\phi(L)$. Identification of p and q terms involves investigating a tentative formulation for
 4 the model as a starting point. After the general model is specified, the $\theta(L)$ and $\phi(L)$ are
 5 estimated using the least-squares method.

6 **NUMERICAL RESULTS**

7 *1.4. Study Area*

8 In this study, we evaluate the proposed framework models for one of the major subnetworks
 9 in Sydney, stretching alongside the Victoria Road corridor from CBD to western city (see
 10 Figure 2). The subnetwork includes 1,310 links and 428 nodes. The General Transit Feed
 11 Specification (GTFS) data is used to import public transport information such as bus time
 12 schedules, lines, and bus stop data. There are 81 signalized intersections with the adaptive
 13 SCATS control system running. The link traffic counts obtained from the SCATS detectors
 14 are aggregated in 15-min time-intervals. Most of the SCATS signals are located throughout
 15 the main corridor and near the Sydney CBD. The simulation is conducted for 4-h morning
 16 peak hours from 6:00 to 10:00 a.m. using an AIMSUN microscopic model. AIMSUN is a
 17 discrete-event simulation tool established based on car-following and lane-changing models
 18 (31). Therefore, detailed traffic phenomena such as congestion propagation and dissipation
 19 of queues are simulated over time. We used a modified multinomial logit model as an
 20 advanced stochastic route choice model (31). Maximum five shortest paths are calculated
 21 using Dijkstra's label-setting algorithm. The probability of choosing a path k is then
 22 calculated according to a utility function of each path.

23 In Sydney, the signal controls are working with SCATS to reduce delay and make the
 24 transport system more efficient. Signal configurations such as signal group, phases and
 25 detector IDs are set in the model based on the SCATS configuration. Since the SCATS
 26 signals are adaptive and the adjacent signals are synchronized, it is very challenging to model
 27 such a complex system. To deal with this issue, we integrate our traffic simulator with
 28 SCATS using SCATSIM plug-in architecture (32). As a result, the real-life adaptive SCATS
 29 control logic is applied to the simulated vehicles in our AIMSUN microsimulation model.



1
 2 Figure 2. Victoria corridor sub-network. Green points show signals equipped with SCATS
 3 count detectors (measured traffic data). Red line demonstrates the main Victoria corridor.

4 *1.5.Demand estimation and prediction*

5 The initial demand used in our study was obtained from the Sydney strategic model received
 6 from Transport for NSW, Australia. The extracted demand for the subnetwork contains 1,262
 7 non-zero origin and destination pairs and around 150,000 travelers who are commuting in
 8 the area during 4-h morning peak hours working days. The total number of travelers suffers
 9 daily changes and declines to less than 100,000 on weekends. We select October 2017
 10 because the traffic count data and incident data are available for almost every day of the
 11 month. To compare day-to-day traffic changes, we plotted the overall traffic counts pattern
 12 for all days in October in Figure 3. We observe that during morning peak hours, the traffic
 13 flow can reach almost 40,000 vehicles per every 15-min time interval compared to weekend
 14 when this number can be counted in the 20,000s. This indicated almost twice motorists
 15 travelling daily during working week, increasing the traffic congestion along the Victoria
 16 Road Corridor. From Figure 3, we selected Thursday 12th October as a typical weekday.
 17

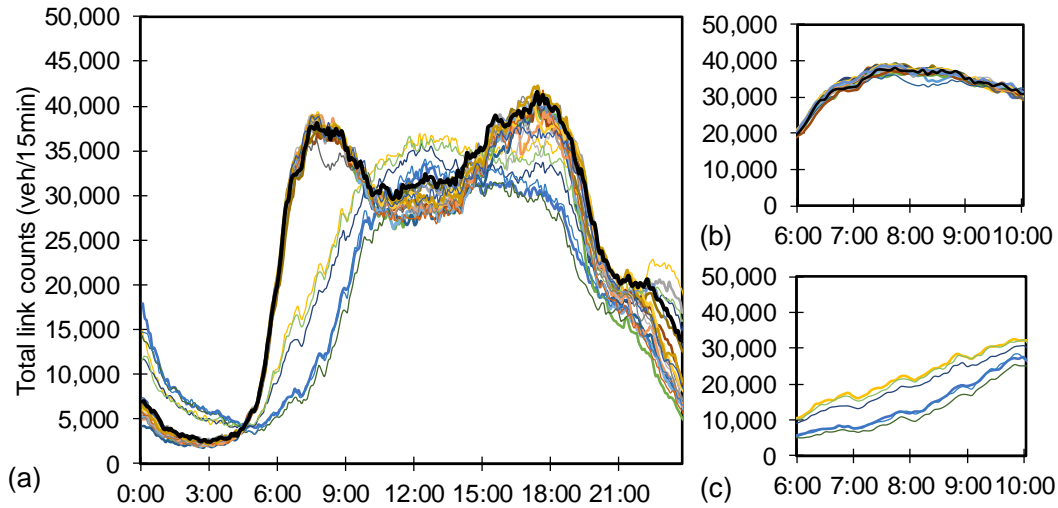


Figure 3. (a) Total 24-hour link counts obtained from loop detectors in the Victoria area in different days within a month, morning peak hours in (b) weekdays and (c) weekends.

We conduct our OD estimation process in two stages. At the first stage, we estimate time-dependent OD demand matrices based on the selected typical weekday link count and a-priori demand data. A priori static OD demand obtained from the strategic model is time-sliced into sixteen 15-minute OD demand matrices for a 4-hour simulation during peak period. Then, the bilevel optimization problem formulated in Eq.(1 is iteratively solved for the whole 4-hour morning peak period. This stage is done once in an offline manner and demand flows at different time intervals are estimated. The only parameter in Eq.(1 that must be set before executing the OD estimation problem is the demand reliability weight, which influences the accuracy of results. Previous studies proposed ranges based on the accuracy of the initial demand, the size of the network, and the simulation time window(33, 34). After various tests, we set this parameter to 0.95 for this case study.

We next execute our proposed OD estimation in a 15-min rolling-horizon procedure. In other words, the time-dependent OD demand matrices estimated from the first stage are adjusted every 15-min time interval based on the most recent observed traffic counts. Note that the input OD matrices for the second stage are more reliable than the inputs to the previous stage since they have already been adjusted. We increase the reliability weight (ω) value from 0.95 to 0.99. Adding higher weight for demand deviation also helps us to avoid overfitting the simulation model based on possible noisy count data. The microsimulation is executed for four hours morning peak with a 15-min network warm-up (5:45- 6:00 AM). We used the coefficient of determination (R^2), mean absolute error (MAE) and GEH (35) as the common goodness of fit criteria to evaluate the simulation results based on link traffic volumes.

$$R^2 = 1 - \frac{\sum_{a=1}^A (\hat{y}_a^r - y_a^r)^2}{\sum_{a=1}^A (\hat{y}_a^r - (\frac{1}{A} \sum_{a=1}^A y_a^r))^2}$$

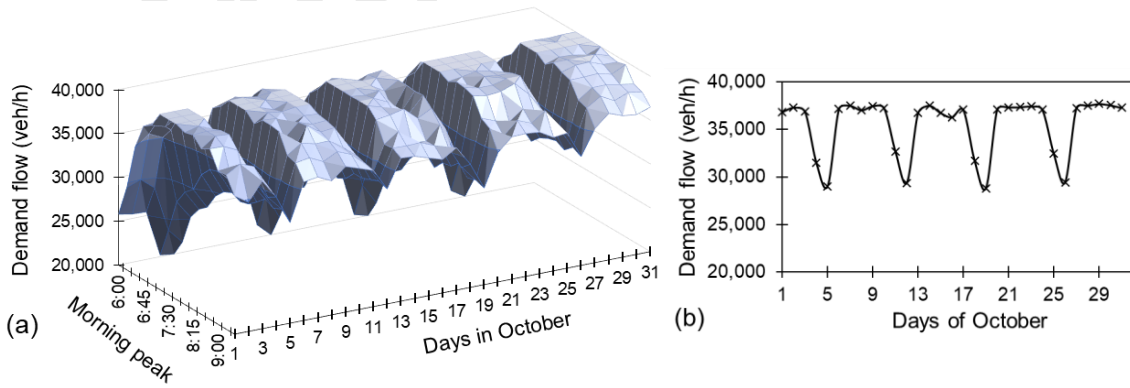
$$MAE = \frac{1}{A} \sum_{a=1}^A |\hat{y}_a^r - y_a^r| \quad (12)$$

$$GEH_a = \sqrt{\frac{2(\hat{y}_a^r - y_a^r)^2}{(\hat{y}_a^r + y_a^r)}}$$

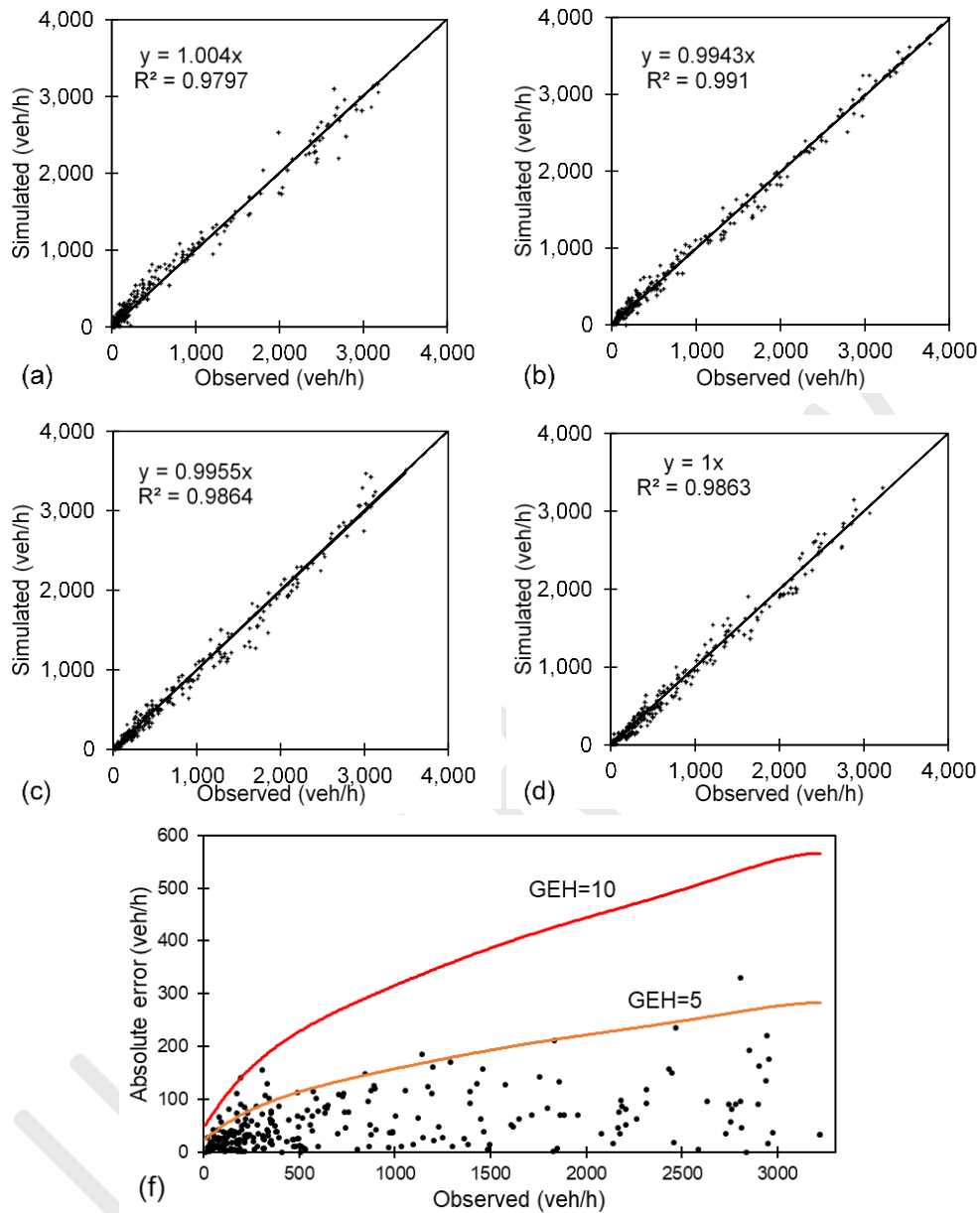
1 Table 1 presents how the accuracy of the simulated traffic volumes increases through the
2 two-stage OD estimation applications. Results show that MAE improves about 42% and 27%
3 respectively after implementing OD demand estimation process at first and second stages. In
4 general, a GEH value under 5 is regarded as a good fit, between 5 and 10 implies the
5 measurement site needs further investigation, and a value greater than 10 implies a significant
6 error (35). As can be seen, at the end of the OD estimation process, all links among 252
7 observed links have GEH less than 10 and almost 90% of links have GEH<5. Similar work
8 is conducted for other days of October 2017 to archive day-to-day OD demand matrices.
9 Figure 4 displays day-to-day variation in the estimated demand. The scatter plots in Figure 5
10 show the simulated and observed traffic flows after OD estimation applications.

11 Table 1. The goodness of fit before and after the OD estimation.

OD matrices	No. links GEH<5	No. links GEH<10	MAE (veh/h)	R2	Regression line
Before OD estimation	189	243	97	0.97	Y=0.98X
After OD estimation stage 1	228	251	56	0.99	Y=1.00X
After OD estimation stage 2	231	252	41	0.99	Y=1.00X



13 Figure 4. Day-to-day total estimated demand flow profiles: (a) in a 3D, (b) in 2D plotting.



1 Figure 5. Simulated versus observed traffic flows after the rolling horizon OD estimation
 2 (a) 6:00-7:00 am, (b) 7:00-8:00 am, (c) 8:00-9:00 am and (d) 9:00-10:00 am (f) Absolute
 3 flow errors vs observed flows.
 4

5 The estimated OD demand matrices were archived and used for the demand prediction
 6 model. As mentioned earlier, there are 1,262 OD pairs with various demand profiles in the
 7 study network. The OD flows vary from few trips between local OD pairs to hundreds of
 8 trips between two ends of the main corridor. Therefore, it is necessary to consider an ML
 9 model for each OD pair trained on previous historical OD pairs. We consider the
 10 corresponding OD flow values from the 5 previous working days. There is a tradeoff between

1 the size of the database and the accuracy of the prediction. More historical data may be useful,
2 but it increases the computation time, especially for real-time forecasting.

3 The features we consider for our models are: three time-lagged demand data (x_i^{t-2} , x_i^{t-1} , x_i^t),
4 the time interval of the prediction (t) and the flow direction (inbound and outbound). We
5 adopt DT, SVR, and the traditional ARMA models for predicting the OD flows for the next
6 15, 30, 45 and 60min. The experiments were conducted in Scikit tool and Stat Python
7 libraries (30). The results of each approach are presented in
8 Table 2 and evaluated against the total error and MAE.

9 As a baseline approach, we assume that we do not have any model to predict the demand.
10 Therefore, the latest demand flow is considered for the next time intervals. As can be seen,
11 by extending the prediction time intervals (from 15 min to 60 min), the prediction error grows
12 quickly (from 1.37 to 1.85). First, we investigate the performance of the decision tree model.
13 The maximum depth of the decision tree is one of the most important parameters that affect
14 the prediction accuracy. Therefore, we chose three different values for this parameter to
15 investigate the sensitivity of the model (maximum depth of 2, 5 or unconstrained). When the
16 constraint is too strict (e.g., max depth=2), the predictor is too simplistic to predict the traffic
17 demand accurately. In contrast, with no constraint (no max depth), the prediction error
18 increases showing the predictor overfitted to the training data. This result demonstrates that
19 the optimum depth of the tree is a critical parameter, which can be optimized. Next, the
20 performance of the SVM model is explored by using different kernel functions. We tried
21 several combinations (the radial basis function (RBF), the sigmoid function, and the linear
22 function) and compared the results through a cross-validation approach. As can be seen, the
23 first two models fail to predict the demand flows successfully and the error is higher than the
24 baseline (e.g. 1.47 and 1.71 to 1.37). The best result for SVM prediction was obtained when
25 using the Linear kernel (with critical parameter of $C=0.1$), for a 45min prediction in the
26 future. This seems to perform similarly to predictions for the next 15 or 60min time-interval.
27 However, overall, the accuracy results for SVM are significantly worse than those of DT
28 prediction. Lastly, we present the results of the ARMA model, for which we need to
29 determine the p and q parameters. Defining various parameters for each OD pair requires a
30 vast amount of modelling effort. This process would be extremely computationally intensive
31 if we need to execute the demand forecasting for any incidents that may arrive in the road
32 network. As a result, we consider the specifications of a unique model for all OD demands
33 and estimate the factors of each OD pair. To identify p and q , we test various combinations
34 of these parameters on all OD demand series ((1,0,0), (2,0,0) and (0,0,1)). Overall, the
35 performance of the traditional AR and MA models show a medium level of accuracy
36 compared to the others and the MAE errors are similar to those of SVM only for a 45min
37 prediction.

38 Overall, we can conclude that DTs are outperforming all other models and represent our final
39 choice for conducting the rest of the experiments presented in this paper.

1

Table 2. Predicted demand using different predictors.

Predictor	Prediction window							
	15 min		30 min		45 min		60 min	
	Total error	MAE	Total error	MAE	Total error	MAE	Total error	MAE
Baseline	1283	1.37	2785	1.49	4519	1.61	6953	1.85
DTs								
Max=2	762	0.81	2785	0.79	2278	0.81	3077	0.82
Max=5	606	0.65	1152	0.61	1743	0.62	2533	0.68
unconstraint	660	0.70	1216	0.65	1816	0.65	2645	0.70
SVM								
RBF (C=0.1)	1381	1.47	2613	1.40	3738	1.33	4797	1.28
Sigmoid (C=0.1)	1592	1.71	3017	1.67	4519	1.54	5545	1.48
Linear (C=0.1)	832	0.89	1676	0.89	2462	0.87	3327	0.89
Linear (C=1.0)	852	0.91	1693	0.90	2490	0.89	3376	0.90
ARMA								
(1,0,0)	869	0.93	1652	0.88	2459	0.87	3377	0.90
(2,0,0)	883	0.94	1678	0.90	2517	0.89	3509	0.93
(0,0,1)	1009	1.08	1876	1.00	2762	0.98	3864	1.03

2

1.6. Incident impact analysis:

3

For evaluating the potential of our proposed framework, we consider a real reported incident along the Victoria Rd with characteristics showcased in Table 3 (as received from the real-life incident stream in the Traffic Management Centre - TMC). The incident took place at 7:58 AM on the 11th of October 2017 and affected the traffic in both directions.

7

8

Table 3. CMCS incident data example

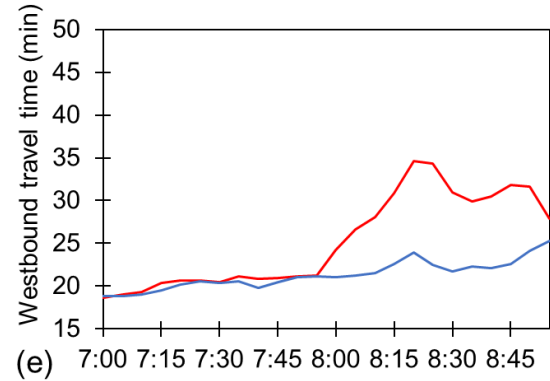
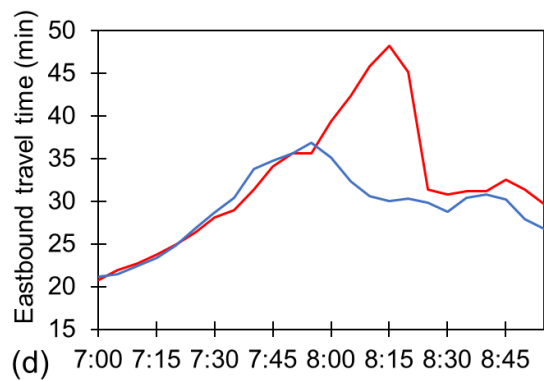
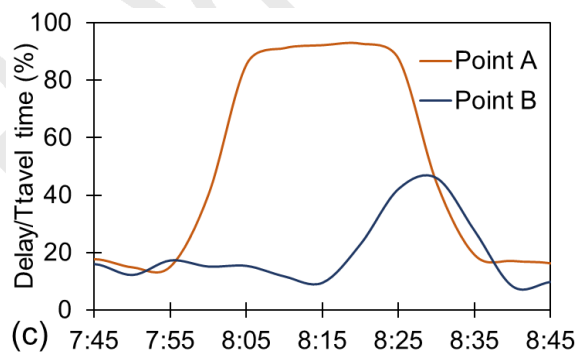
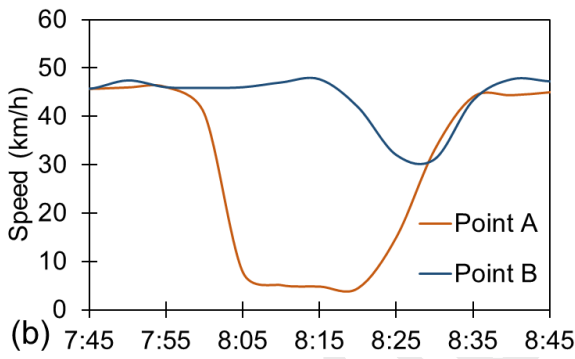
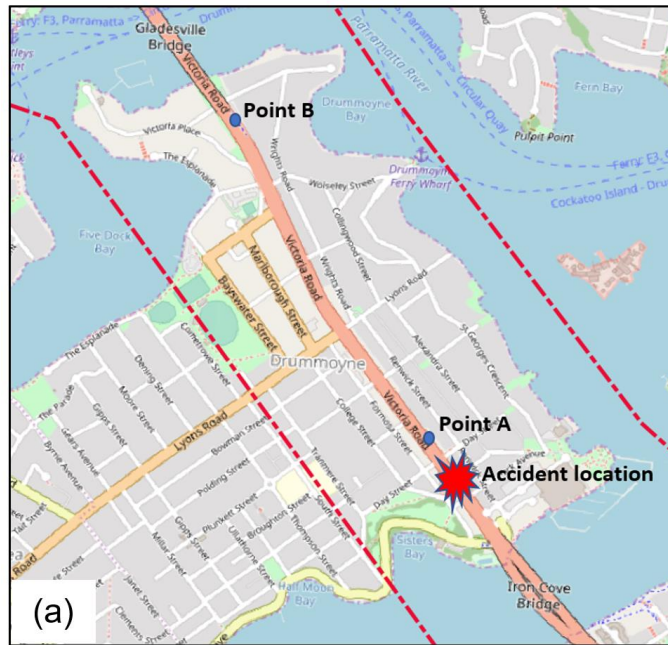
(X, Y)	(9684462, 4425168)
Date	11/10/2017
Start Time Plain	7:58:19 AM
End Time Plain	8:23:00 AM
Incident Description	Accident: Accident
Location Description	VICTORIA RD PARK AVE DRUMMOYNE 2047 CANADA BAY (LGA) NSW
Direction	BOTH DIRECTIONS
Affected Lanes	ALL LANES
Sector ID	ICMT
Inc Source	ICEMS INCIDENT AND ISENTRY
Operator	----
ICEMS Street	VICTORIA RD
ICEMS Suburb	DRUMMOYNE
UBD Ref	235 A/4
ed duration	25
rowid	A6C4B8F8-5617-4E12-B170-973234EA31B0

9

1 First, the accident information is imported into the simulation platform. The corresponding
2 affected link IDs from the traffic simulation are determined based on the accident location.
3 For example, according to the presented data, the accident impacts both travel directions, and
4 thus, two affected sections are selected. Then, an incident scenario containing the number of
5 blocked lanes, start time and incident duration is generated. Next, the Decision-Tree demand
6 prediction module is triggered to forecast the travel demand starting from 8:00 AM for the
7 next hour. Subsequently, the simulation model is executed with consideration of the
8 developed incident scenario. Since the incident is located in a crucial link, we explore the
9 impact of the incident duration by analyzing the total travel time in the network and the extra
10 delay it caused in next hour.

11 Figure 6 (a) shows the location of the car accident. The accident took place in the main road
12 and according to the reported data it impacted all lanes in both directions. No further details
13 about how the accident affected the area exist in the database. Therefore, different
14 interpretations of affected lanes can be considered. For example, the accident may have
15 physically blocked all the lanes or it caused some speed reduction for crossing vehicles. Since
16 it is unlikely that for half an hour all lanes are fully blocked in two directions, we assume
17 only two lanes were blocked and vehicles could slowly cross the accident area with some
18 lane changing near the accident. We executed the simulation based on the above assumption
19 and the simulated speed and delay ratio are plotted for two different location points along the
20 corridor: point A taken near the accident location and point B towards west, 1,600 meters
21 away from the accident. Figure 6 (b) and (c) show the severe drop in the speed near the
22 incident location (Point A) and consequently, the delay/travel time ratio increases
23 significantly at this point. The impact of the accident can be observed upstream with a time
24 lag and less severity. Next, we compare the simulated travel time obtained for the
25 eastbound/westbound directions along the entire Victoria Rd corridor in two scenarios: with
26 the reported incident and without the incident (this would be regular travel times in normal
27 conditions) in Figure 6 (d) and (e). One can observe that the reported incident at 07: 58AM
28 induces an increase of almost 12 min on the eastbound direction (from 36-48 min) and 13
29 minutes in the westbound direction (from 22 to 35 minutes).

30
31



1 Figure 6. (a) Accident location, (b) speed (c) delay ratio profiles for Point A and B. Journey
 2 times with (red) and without (blue) the incident: (d) Eastbound, (e) Westbound.

1 CONCLUSION

2 Managing an incident situation effectively is one of the critical challenges that TMCs deal
3 with on a daily basis. Methodological advances in both data-driven and computer-based
4 simulation modeling provide a unique opportunity to predict traffic conditions accurately in
5 real-time. This paper presented a generic framework for incident management proposed for
6 use in the TMC of Sydney, Australia, by using integrated data-driven and traffic simulation
7 models. We first introduced a generic demand estimation and prediction model which
8 provides the essential input for the traffic simulation model to forecast the traffic features
9 under non-recurrent incident conditions.

10 The proposed approach initially calibrates the traffic model based on the most recent
11 observed link traffic count and then uses them for demand prediction for the next time-
12 interval. A bi-level dynamic OD demand estimation problem was formulated and solved
13 iteratively. Thereafter, we showcased that Decision Trees outperformed the baseline, SVM
14 and ARMA models in terms of prediction accuracy. Finally, we investigated an incident's
15 impact by making use of the proposed framework outputting the predicted travel time/delay
16 along the affected corridor. Several limitations exist for this study that will be addressed in
17 our future work:

- 18 • We assumed that travellers respond to the bad traffic conditions by changing routes
19 in peak hours. However, for critical traffic disruptions, we should consider mode
20 shifting and trip cancelation in short-term traffic forecasting.
- 21 • Although the current simulation network provides the commuters with some re-
22 routing options, the selected area has limited major parallel routes to consider
23 strategic re-route choices of travellers under severe incident conditions. We plan to
24 expand our simulation modelling to larger subnetwork areas.
- 25 • For the real-time incident impact application, incident time duration should be
26 predicted based on the incident features. Another AI-engine will be added to the
27 incident management platform to provide an incident duration estimation for the
28 traffic simulator when an incident occurs. This estimation can be updated with more
29 incident data.
- 30 • In order for our proposed modelling framework to be used for real-life traffic
31 management operations, it requires exact details of the incident location (inside
32 intersection or not, beginning and ending of road link), the length of the affected
33 incident area and exact number of blocked lanes. This can be challenging for
34 operational centres to provide in real-time.
- 35 • The performance of the simulation results should be evaluated based on
36 complementary measured traffic data including travel time, flow and queue length.

- The traffic model includes private cars and buses. The other types of traffic modes such as taxi, freight and active modes can be exclusively considered in the model. This will help us to replicate the simulated congestion more accurately.

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AUTHOR CONTRIBUTIONS

S. S. designed and performed the research, A-S. M. contributed to direction, and A-S. M., H. N., C. B. and C. C. reviewed and contributed to the manuscript.

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