# Three Applications of Time-Varying Parameter Models to Macroeconomics

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This dissertation is submitted for the degree of Doctor of Philosophy

## **Declaration**

I would like to dedicate this thesis to my loving parents.

Bowen Fu

December 2019

**Certificate of Original Authorship** 

I, Bowen Fu, declare that this thesis, submitted in fulfilment of the requirements for the

award of Doctor of Philosophy, in the Economics Discipline Group, Business School, at

the University of Technology Sydney. This thesis is wholly my own work unless otherwise

reference or acknowledged. In addition, I certify that all information sources and literature

used are indicated in the thesis. This document has not been submitted for qualifications at

any other academic institution.

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## **List of Abbreviations**

**AUROC** Area under the receiver operating characteristic

**CC-SV** Constant coefficient model with stochastic volatility

**CPI** Consumer price index

**EU** European Union

**GDP** Gross domestic product

**HPD** Highest Posterior Density

LASSO Least absolute shrinkage and selection operator

MCMC Markov Chain Monte Carlo

**NFE** Non-financial enterprise

**SPF** Survey of Professional Forecasters

TVC Time-varying coefficient model with constant volatility

**TVP** Time-varying parameter

**TVC-SV** Time-varying coefficient model with stochastic volatility

**UIP** Uncovered interest parity

UK United Kingdom

US United States

VAR Vector autoregression

#### **Abstract**

This thesis includes chapters that examine the application of time-varying parameter models to three macroeconomic topics: the Phillips curve, early warning system models, and uncovered interest rate parity.

Chapter 2 formally tests for time variation in the slope of the Phillips curve using a variety of measures of inflation expectations and real economic slack. We find that time variation in the slope of the Phillips curve depends on the measure of inflation expectations rather than the measure of real economic slack. We find strong evidence supporting the time-varying slopes of the Phillips curve with different measures of inflation expectations. Thus, we conclude that the slope of the Phillips curve is time varying.

In Chapter 3, we both narrowly and widely replicates the results of Anundsen et al. (2016). Further, we find that allowing for time-varying parameters of early warning system models can considerably improve the in-sample model fit and out-of-sample forecasting performance based on an expanding window forecasting exercise.

In Chapter 4, we consider a time-varying coefficient model with stochastic volatility for the uncovered interest parity regression. We show that jointly estimating time-varying coefficients and stochastic volatility can provide relatively reliable time-varying parameters. Using posterior samples from Bayesian estimation, we determine which United States macroeconomic variables explain the variation in time-varying coefficients and volatility based on least squares with shrinkage. Our empirical study shows that the null hypothesis of uncovered interest parity cannot be unconditionally rejected in the cases of several de-

veloped economies. Further, we show that local breaches of uncovered interest parity are mainly associated with variables from the labour market variables and the output variables in the United States, among other variables.