MATHEMATICAL AND STOCHASTIC MODELLING OF MOLECULAR COMMUNICATION SYSTEMS FOR Advanced Drug Delivery Applications

by

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Certificate of Original Authorship

I, Muneer Al-Zubi declare that this thesis, is submitted in fulfilment of the requirements for the award of Doctor of Philosophy, in the School of Biomedical Engineering at Faculty of Engineering and Information Technology at the University of Technology Sydney.

This thesis is wholly my own work unless otherwise reference or acknowledged. In addition, I certify that all information sources and literature used are indicated in the thesis.

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Abstract

Molecular communication (MC) is an emerging nanoscale communication paradigm, biologically inspired by the cellular communications via biochemical molecules in the living organisms. The MC paradigm is highly suitable for modelling and abstraction of the underlying complex processes in the drug delivery systems (DDSs) over wide spatiotemporal scales. Targeted and implantable DDSs are advanced and engineered technologies for effective delivery of anticancer drugs to the cancerous tumors without affecting other healthy parts in the body. This approach offers an efficient alternative or adjunctive therapy to other treatment techniques, such as conventional chemotherapy, thermal ablation, and surgical resection. In-Silico (mathematical and stochastic) models are key tools to understand and quantify the various parameters and processes in the DDSs, including drug transport, release processes, reaction, and other physicochemical interaction processes in the biological microenvironments inside the body. These models play an essential role in the design and development of the DDSs which in order can reduce the animal experiments and can save time and reduce cost.

The focus of my Ph.D. research is to develop novel mathematical and stochastic simulation models using MC paradigm for localized targeted and implantable DDSs over nano- and micrometer scales in complex biological microenvironments. Using the MC paradigm, the drug delivery process is abstracted as a communication mechanism where the drug source acts as a transmitter while the target site (e.g., cancer cell) acts as a receiver and the biological environment through which the molecules get transported acts as a propagation channel. The anticancer drug molecules represent the information carriers that contain the physicochemical properties of the drug. We use system analysis approach using the channel impulse response (CIR) coupled with the signal processing technique (convolution) for modelling the targeted and implantable DDSs in tumor microenvironments (TME). This approach provides more general and flexible models compared to other modelling approaches.

The thesis made original contributions in the following four major aspects:

(1) Generalized mathematical and stochastic simulation models are developed for diffusionbased molecular communications (MC) in complex fluidic microenvironments that include multilayered physical structures, ligand-receptor reaction, anisotropic diffusion, and the effect of reactive obstacles. These generalized models are developed for modelling and design of both the targeted drug delivery systems (TDDS) as well as the molecular communication systems between bio-nanomachines or cells in such complex environments over microscopic scale. (2) The proposed multilayer MC models have been extended for modelling the intravascular TDDS including anticancer drug release from the nanocarriers (NCs) and drug transport across the endothelial barrier of the tumor vasculature in tumor microenvironments. (3) Novel mathematical and stochastic simulation models are developed for modelling the implantable drug delivery system (IDDS) in tumor by predicting and characterizing the release process and drug distribution in the surrounding tumor tissue. (4) Pharmacokinetic /Pharmacodynamics models are developed for modelling the combination therapy using local implantable drug delivery systems in solid tumors following thermal ablation therapy.

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Dedication

To **my parents and my family** for their love, endless support and encouragement. I am forever indebted to my parents, who have always kept me in their prayers and taught me the meaning of life. Moreover, this thesis is dedicated to my beloved wife, **Duaa**, who has been a constant source of support and encouragement. Without them, the completion of this work would not have been possible.

Abbreviations

- AUC Area Under the Curve
- CIR Channel Impulse Response
- CT Computed Tomography
- DDD Drug Delivery Device
- DDS Drug Delivery System
- DOX Doxorubicin
- DTI Diffusion Tensor Imaging
- ECS Extracellular Space
- ECM Extracellular Matrix
- EPR Enhanced Permeability and Retention
- FDA Food and Drug Administration
- HT Hyperthermia
- IBP Intervascular Blood Pressure
- IDDS Implantable Drug Delivery System
- IFF Interstitial Fluid Flow
- IFP Interstitial Fluid Pressure
- ISFI In-Situ Forming Implant
- IVF Interstitial Velocity Field
- IVIVC In Vitro In Vivo Correlation
- MC Molecular Communication

- MCvD Molecular Communication via Diffusion
- MEC Minimum Effective Concentration
- MRI Magnetic Resonance Imaging
- MSD Mean-Square Displacement
- MW Molecular Weight
- NC Nanocarrier
- PTX3 Pentraxin-3
- PD Pharmacodynamic
- PK Pharmacokinetic
- PLGA Poly (Lactic-co-Glycolic Acid)
- QS Quorum Sensing
- RDME Reaction-Diffusion Master Equation
- RF Radio Frequency
- RFA Radiofrequency Ablation
- RMSE Root-Mean Square Error
- RN Receiving Nanomachine
- TDDS Targeted Drug Delivery System
- TME Tumor Microenvironment
- TN Transmitting Nanomachine
- TSL Thermosensitive Liposome

List of Publications

Journals:

- M. Al-Zubi and A. Sanagavarapu, "Modelling of Implantable Drug Delivery System in Tumor Microenvironment using Molecular Communication Paradigm", *IEEE Access*, vol. 7, pp. 141929-141940, 2019.
- 2. M. Al-Zubi and A. Sanagavarapu, "Modeling a composite molecular communication channel", *IEEE Transactions on Communications*", vol. 66, pp. 3420-3433, 2018.
- M. Al-Zubi and A. Sanagavarapu, "Modeling of Ligand-Receptor Protein Interaction in Biodegradable Spherical Bounded Biological Micro-Environments", *IEEE Access*, vol. 6, pp. 25007-25018, 2018.
- 4. M. Al-Zubi and A. Sanagavarapu, "Implantable Biosensor Interface Platform for Monitoring of Atherosclerosis", *IEEE Sensors Letters*, vol. 4, p. 5500204, 2020.

Conferences:

- M. Al-Zubi, A. Sanagavarapu, and S. Ling, "Influence of Tissue Anisotropy on Molecular Communication", *IEEE International Engineering in Medicine and Biology Conference (EMBC)*, Germany, pp. 2921-2924, 2019.
- M. Al-Zubi, A. Sanagavarapu, and S. Ling, "Impact of Reactive Obstacle on Molecular Communication between Nanomachines", *IEEE International Engineering in Medicine and Biology Conference (EMBC)*, USA, pp. 4468-4471, 2018.
- M. Al-Zubi, A. Sanagavarapu, and S. Ling, "Comparison of Reception Mechanisms for Molecular Communication via Diffusion", *International Conference on Information and Communication Systems (ICICS)*, Jordan, pp. 203-207, 2018.
- M. Al-Zubi and A. Sanagavarapu, "Modelling of multilayer biological medium under molecular communication paradigm", *IEEE Life Sciences Conference (LSC)*, Australia, pp. 31-34, 2017.

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