

© 2020. This manuscript version is made available under the CC-BY-NC-ND 4.0 license <http://creativecommons.org/licenses/by-nc-nd/4.0/>
The definitive publisher version is available online at <https://doi.org/10.1016/j.trgeo.2020.100490>

Experimental insights into the stiffness degradation of subgrade soils prone to mud pumping

Authors:

Mandeep Singh¹, Ph.D., Senior Technical Support Officer (GeoTech)

Buddhima Indraratna^{2*}, Distinguished Professor

Thanh Trung Nguyen³, Research Fellow

¹University of Technology Sydney, Tech Lab, Botany NSW 2019, Australia.

²School of Civil and Environmental Engineering and Director, Transport Research Centre (TRC), University of Technology Sydney, NSW 2007, Australia

Formerly: Founding Director, Centre for Geomechanics and Railway Engineering; Director, Australian Research Council (ARC) Industrial Transformation Training Centre, ITTC-Rail University of Wollongong, NSW 2522, Australia.

³Transport Research Centre (TRC), University of Technology Sydney, NSW 2007, Australia.

Word count: 2637 (excluding references, tables and figures)

Figures: 6

Submitted to: Transportation Geotechnics

*Corresponding author: Buddhima Indraratna (e-mail: Buddhima.Indraratna@uts.edu.au)

1 **Abstract**

2 Recent laboratory investigations conducted on soils prone to mud pumping have shown that
3 the subgrade soil experiences softening associated with an internal redistribution of moisture
4 when the cyclic stress ratio (CSR) exceeds a certain critical level. This article aims to
5 evaluate the stiffness degradation of these problematic subgrade soils subjected to a wide
6 range of loading conditions. The test results revealed that the instability of the specimens is
7 caused by the early softening behaviour, and this is accompanied by a sharp reduction in the
8 specimen stiffness. As high as 70-80% reduction in the initial small-strain stiffness was
9 observed even for densely compacted specimens ($\rho_d = 1790 \text{ kg/m}^3$). In this regard, a new
10 method for predicting the threshold number of cycles, N_{thr} and residual axial strains required
11 for the onset of subgrade instability is proposed. As a useful practical guide, a quasi-linear
12 relationship between the threshold strain and N_{thr} is also determined.

13

14 *Keywords:* Mud pumping; fluidization; subgrade instability; stiffness degradation.

15 **1. Introduction**

16 In recent times there has been a considerable interest within the railway geotechnical
17 community to investigate the underlying mechanisms and to propose appropriate remediation
18 measures for ballasted tracks affected by mud pumping (Kuo et al., 2017; Hasnayn et al.,
19 2017; Nguyen et al., 2019; Singh et al., 2019; Indraratna et al. 2020a and 2020b). In short,
20 mud pumping is the upward migration of soft subgrade fines to the coarser ballast layer.
21 Indraratna et al. (2020b) reported that low plastic soils can experience fluidization where soil
22 turns into a fluid-like state under the ballast at high applied cyclic stresses and termed it as
23 subgrade fluidization. Few researchers (Nguyen and Indraratna, 2020) have explained the
24 micro-mechanism behind the fluidisation of subgrade soils using advanced CFD-DEM
25 coupling. Indraratna et al. 2020a observed early softening of fluidized specimens at high
26 applied cyclic stresses. Hasnayn et al. 2020 performed full-scale experimental investigations
27 on submerged rail track system and reported that flooding caused a continual reduction in soil
28 stiffness. As the fluidized specimens were unable to sustain the amount of applied cyclic
29 stress and therefore, it is essential to quantify the stiffness of the subgrade specimens under
30 cyclic loading to provide further insight to the degradation aspect of these unstable
31 specimens.

32 Clay soils in general, when subjected to cyclic loading experience a reduction in the
33 stiffness with the number of loading cycles. On the other hand, coarse-grained soils when
34 subjected to lower cyclic stresses experience an increase in the stiffness due to densification
35 (Leng et al., 2017). Zhou and Gong (2001) proposed a relationship for the strain degradation
36 in terms of the applied cyclic load, the frequency and the over-consolidation ratio. Kallioglou
37 et al. (2008) reported a comprehensive summary of the factors effecting the small-strain shear
38 modulus and studied the role of plasticity index in governing the degradation of the shear
39 modulus.

40 Although there is an abundance of literature on the degradation of soft soils, majority
41 of them have been carried out for strain-controlled cyclic triaxial tests (Zhou and Gong, 2001;
42 Mortezaie and Vucetic, 2013). Also, it is widely accepted that when fully saturated soils are
43 subjected to large cyclic strain amplitudes under undrained conditions, they experience a
44 permanent change in the soil structure leading to a decrease in the stiffness as well as the
45 strength and a permanent increase in the pore water pressure. The stress path adopted while
46 loading the specimens also plays a crucial role in the stiffness degradation of the specimens.
47 When the specimens are subjected to principal stress rotation, the specimens experience
48 larger strains and thereby severe stiffness degradation (Cai et al. 2018, Mamou et al. 2019).
49 As will be shown later, there exists a correlation between the generation of excess pore
50 pressure and stiffness degradation for fluidized soil specimens, and there are limited studies
51 addressing this phenomenon (Hsu and Vucetic, 2006; Soralump and Prasomsri, 2016). This
52 paper aims to establish the threshold residual axial strains for fluidized specimens by
53 considering in tandem the stiffness degradation index and the mean excess pore pressure
54 ratio(u_m/σ'_{3c}).

55 **2. Experimental investigation**

56 **2.1. Undrained cyclic triaxial testing**

57 The response of two subgrade soils prone to mud pumping was studied by conducting a series
58 of undrained cyclic triaxial tests on remoulded soil specimens, at various initial dry densities
59 (detailed experimental procedures are described elsewhere by Indraratna et al., 2020a;
60 2020b). The particle size distribution (PSD) of the two soils indicates that these two samples
61 have a high percentage of fines ($< 75 \mu\text{m}$) of about 30% and 54% for soils - MP1 and MP2,
62 respectively (Fig. 1). The basic geotechnical properties of the soils MP1 and MP2 are detailed
63 in Table 1. The ratio of the initial dry density (ρ_d) to that of the maximum dry density as

64 obtained by Standard Proctor test (ASTM D698-07 Standard, 2012) is defined as relative
65 compaction (RC). The cyclic stress ratio (CSR) is defined as the ratio of the amplitude of the
66 applied cyclic stress ($\sigma_d/2$) to that of the effective confining pressure after consolidation
67 (σ'_{3c}).

$$\text{CSR} = \frac{\sigma_d}{2\sigma'_{3c}} \quad (1)$$

68 The pore pressure transducer installed at the base of the standard triaxial cell was calibrated
69 prior to each test. The specimens were fully saturated to achieve a Skempton's B-value
70 exceeding 0.95 prior to the anisotropic consolidation phase (ratio of effective horizontal
71 stress to the vertical stress, $k_0 = 0.6$). A low effective confining pressure ($\sigma'_{3c} = 15$ kPa) was
72 chosen to represent the shallow regions of the rail subgrade thereby, the initial deviatoric
73 stress, q_0 , for the tested specimens was set to 10 kPa. For the tested frequency range (1.0 –
74 5.0 Hz), the time lag in the peak and trough of the excess pore pressure response
75 corresponding to the applied cyclic load was insignificant. The anticipated stresses on the top
76 of the subgrade were considered to be within the range of 15 to 30 kPa for various axle loads
77 (14-23 t) (Liu and Xiao, 2010). Therefore, the testing was carried out for a wide range of
78 CSR (0.2 to 1.0). It is noteworthy that Powrie et al. (2007) have noted a frequency of 4.0 Hz
79 acting at 1.0 m below the sleeper base for train speed at 50 m/s (180 km/h), implying that the
80 authors' tested frequency range of 1.0 to 5.0 Hz would correspond to train speeds of 45- 225
81 km/h on standard gauge tracks. The influence of the CSR and loading frequency on the
82 stiffness degradation is highlighted in the following sections and the details of soil properties
83 and loading parameters used in the current study are summarized in Table 2.

84 **2.2. Cyclic response of the soil specimens**

85 Two distinct stress-strain responses, viz., stable and unstable response were recorded as the
86 cyclic stress ratio is increased. As can be seen from Fig. 2a, when the specimen ($\rho_d = 1790$

87 kg/m³) was subjected to a CSR = 0.4 at a loading frequency of $f = 1.0$ Hz, the stress-strain
 88 loops stabilized after about 1000 cycles. The maximum cyclic axial strain (ϵ_{ac}) after 50000
 89 cycles is shown to be only 0.45%. Further, when the CSR is increased to 1.0, the test
 90 specimen shows signs of early softening due to which the specimens were unable to
 91 withstand the applied cyclic stress (Fig. 2b). These observations clarify that the reduction in
 92 the stiffness as observed from the stress-strain loops is more prominent at higher CSR due to
 93 the formation of slurry at the top of the fluidized specimen. At CSR greater than the critical
 94 cyclic stress ratio (CSR_c), the specimen experiences a rapid increase in the mean excess pore
 95 pressure ratio along with a sudden decrease in the stiffness.

96 3. Stiffness Degradation Index

97 When soils experience larger strains, there is a significant reduction in the soil stiffness.
 98 While some past studies (Zhou and Gong, 2001; Lei et al., 2016) have computed the stiffness
 99 degradation by assuming constant level of stress, this may not be applicable for the fluidized
 100 specimens as they experience early softening (as indicated in Fig. 2). Therefore, the approach
 101 suggested by Cai et al. (2018) was adopted for the current analysis by evaluating the axial
 102 dynamic modulus of each loading-unloading cycle.

103 The generalised behaviour of a soil subjected to one-way stress controlled cyclic loading
 104 is depicted in Fig. 3. The axial dynamic stiffness is defined as the ratio of the difference of
 105 maximum and minimum deviatoric stress to the difference of the maximum and minimum
 106 axial strain at N number of cycles (note that the data logger records 10 data points per cycle):

$$107 \quad E_{d,N} = \left[\frac{\sigma_{d,max} - \sigma_{d,min}}{\epsilon_{d,max} - \epsilon_{d,min}} \right]_N \quad (2)$$

108 As the axial strains are readily measured in the triaxial setup and have been used to determine
 109 the specimen stiffness, the corresponding modulus is termed as the axial dynamic stiffness.
 110 The stiffness degradation index, δ , is computed by comparing the axial dynamic stiffness of a

111 given cycle to that of the first cycle, thus:

$$112 \quad \delta = \frac{E_{d,N}}{E_{d,1}} \quad (3)$$

113 **4. Relationship between the stiffness degradation index and mean excess** 114 **pore pressure ratio**

115 **4.1. Predicting threshold number of cycles, N_{thr}**

116 Konstadinou and Georgiannou (2014) estimated the critical number of cycles for the
117 liquefaction of sands based on the variation in the excess pore water pressure data. The
118 critical number of cycles was estimated by plotting the incremental normalized excess pore
119 pressure for every cycle, and they observed the characteristic concave downward followed by
120 concave upward shape for the generation of excess pore pressure. However, in this study, an
121 attempt is made to predict the threshold number of cycles by incorporating the stiffness
122 degradation and the mean excess pore pressure.

123 To estimate the critical number of cycles, the degradation index curves are plotted
124 along with the mean excess pore pressure curves. The specimens which fluidize show a rapid
125 reduction in the stiffness (Fig. 4a) that is accompanied by a sharp rise in the mean excess pore
126 pressures. The point of intersection of the two curves can be defined as the threshold number
127 of cycles, N_{thr} , initiating the onset of fluidization. It is important to note that N_{thr} differs from
128 the critical number of cycles, N_c as defined by Indraratna et al. 2020b, as it considers stiffness
129 degradation and pore pressure response of the fluidized specimens as opposed to mere axial
130 strain response. As shown in Fig. 4, when the specimen compacted at $\rho_d = 1790 \text{ kg/m}^3$ is
131 subjected to a CSR of 0.5 and frequency of 1.0 Hz, the degradation index at 5% cyclic axial
132 strain (ε_{ac}) is about 0.46, and the mean excess pore pressure accumulated at the end of the
133 test (i.e. at $\varepsilon_{ac} = 5\%$) is 0.63. The threshold number of cycles, N_{thr} , can be estimated as $N_{thr} =$

134 50. Similarly, the values of the threshold number of cycles required for the onset of subgrade
135 fluidization at various loading conditions are summarised in Table 2.

136 **4.2. Evaluating threshold residual axial strain, $\epsilon_{ar,thr}$**

137 The residual axial strain corresponding to the threshold critical number of cycles is denoted
138 as $\epsilon_{ar,thr}$. Referring to Fig. 4b, it is noted that the present methodology of estimating N_{thr}
139 overestimates the critical number of cycles N_c , as obtained from the inflexion point on the
140 concave axial strains plots (Indraratna et al. 2020b). It could be attributed to the fact that the
141 determination of N_c , did not take into account the stiffness degradation of the specimen and
142 captured only the point of rapid axial strain accumulation. Also, one can observe that there is
143 a quasi-linear relationship between $\epsilon_{ar,thr}$ and $\log(N_{thr})$ at a given cyclic stress ratio. The
144 threshold residual axial strain corresponding to different CSR, loading frequency and RC is
145 shown in a single plot (Fig. 4c). The specimen compacted at an RC = 93% has a lower value
146 of the threshold axial strain at CSR = 0.5 (i.e., 1.2%) compared to the specimen compacted at
147 RC = 99% (i.e., 1.6%) when subjected to a loading frequency of 1.0 Hz. However, it is
148 interesting to note that the loose specimen (i.e., RC = 93%) fails quicker than the relatively
149 dense specimen (RC = 99%) attributed to the rapid generation of excess pore pressure in the
150 loose specimen. Moreover, as the smaller loading frequency imparts higher residual axial
151 strains for the fluidized specimens (discussed in above section 3.2.), the threshold residual
152 axial strains follow the same trend (Fig. 4c). In order to compare the variation of the
153 threshold axial strains for fluidized specimens, the above procedure was repeated for soil-
154 MP2 which fluidized under undrained cyclic loading (Indraratna et al. 2020a). In particular,
155 $\epsilon_{ar,thr}$ decreases faster with N given the same frequency $f = 5.0$ Hz. The difference in the
156 relative compaction of the two soils (both having very different fines content) could be the
157 reason for the relatively flatter behaviour for the current soil (Fig. 5a).

158 The threshold axial strains were also evaluated for the undrained cyclic triaxial tests on

159 the ultrasoft and medium plastic soil ($w_{LL} = 54.9\%$; $PI = 27.5$; cohesion, $c = 7.58$ kPa)
160 reported by Lei et al. (2016). The CSR reported by them was computed using the ratio of the
161 applied dynamic stress to the effective confining pressure. Therefore, the soil that exhibited
162 instability at a CSR of 0.35 by Lei et al., (2016) could be re-evaluated to a CSR of 0.175
163 based on the definition consistent with Eq. (1) of the current paper. It is noted that Lei et al.
164 (2016) have observed an inflection point in the behaviour of the soft soil with respect to
165 frequency by subjecting the soil specimens to a frequency range of 1.0 to 10.0 Hz. However,
166 no such inflection point can be observed in the present study for the tested loading frequency
167 range of 1.0-5.0 Hz, but the variation in the threshold residual axial strain matches well with
168 the trend reported by Lei et al. (2016) as shown in Fig. 5b.

169 **5. Discussion and practical implications**

170 By carrying out undrained cyclic triaxial testing, the critical cyclic stress ratio (CSR_c) at
171 which the specimen fluidise can be determined. Based on the test results, it is evident that the
172 subgrade soil specimens undergo severe stiffness degradation when the applied CSR exceeds
173 the CSR_c which was also reported by other researchers (Zhou and Gong 2001; Leng et al.
174 2017). The threshold number of cycles, N_{thr} , corresponds to the point where the increasing
175 mean excess pore pressure ratio and the decreasing stiffness degradation index meet. It
176 provides an estimate to the minimum number of cycles required to initiate rapid axial strain
177 accumulation in the specimen. The threshold residual axial strain corresponding to the N_{thr} ,
178 marks the onset of fluidisation for the test specimens. The methodology adopted above is
179 highlighted in Fig. 6.

180 It is noted that the above method is yet to be applied for a wide range of soils to further
181 strengthen the correlation between the generation of mean excess pore pressure and stiffness
182 degradation. However, the current analysis shows promising results for low to medium

183 plastic clays (Indraratna et al. 2020a and 2020b). Further, the role of principal stress rotation
184 on the stiffness degradation is yet to be investigated. It is believed that the principal stress
185 rotation would aggravate the stiffness degradation and increase the cyclic axial strains (Cai et
186 al. 2018). Moreover, the thresholds would be higher for drained or partially drained than in
187 undrained conditions (Mamou et al. 2019).

188 **6. Conclusions**

189 The present study was focussed on analysing the stiffness degradation of fluidized soil
190 specimens. Based on the present study, the following salient conclusions can be drawn:

- 191 • There is a steep decrease in the axial dynamic stiffness of the specimens that are
192 subjected to a higher CSR. For example, when the specimen compacted at an initial
193 density of $\rho_d = 1790 \text{ kg/m}^3$ was subjected to a CSR = 0.5 at $f = 1.0 \text{ Hz}$, the stiffness
194 reduced to 30% of the initial value in about 100 cycles.
- 195 • There exists a near linear relationship between $\varepsilon_{ar,thr}$ and $\log(N_{thr})$ for the tested
196 frequency range (1.0 to 5.0 Hz) and CSR (0.4 to 1.0). However, further experimental
197 data for different soil types is required to establish a more reliable governing
198 relationship that can encompass a wider range of soils that are vulnerable for mud
199 pumping.
- 200 • The threshold number of cycles required to initiate fluidization could be evaluated by
201 knowing the stiffness degradation index (δ) and the evolution of the mean excess pore
202 pressure in the specimen. This value of N_{thr} depends on the soil type, gradation, CSR,
203 loading frequency and relative compaction. N_{thr} predicted from the above
204 methodology seems to overestimate the critical number of cycles N_c , obtained from
205 the inflexion point of the concave axial strain plots.

206 **Acknowledgements**

207 This research was supported by the Australian Government through the Australian
208 Research Council's Linkage Projects funding scheme (project **LP160101254**) and the
209 Industrial Transformation Training Centre for Advanced Technologies in Rail Track
210 Infrastructure (ITTC), University of Wollongong. The authors also acknowledge the support
211 from Transport Research Centre, University of Technology Sydney, Australia.

212 **List of Notations:**

CSR	Cyclic stress ratio
CSR _c	Critical cyclic stress ratio
$E_{d,N}$	Axial dynamic modulus
f	Loading frequency
G_s	Specific gravity
k_0	Ratio of effective horizontal stress to the vertical stress
N_c	Critical number of cycles
N_{thr}	Threshold number of cycles
PI	Plasticity index
q_0	Initial deviatoric stress
RC	Relative compaction
u_m/σ'_{3c}	Mean excess pore pressure ratio
w_{LL}	Liquid limit
δ	Stiffness degradation index
ε_{ac}	Cyclic axial strain
$\varepsilon_{ar,thr}$	Threshold residual axial strain
ρ_d	Initial dry density
σ'_{3c}	Effective confining pressure after consolidation
σ_d	Applied cyclic stress

Tables

Table 1 Basic geotechnical properties of the soils analysed in this study

Characteristics of sub-soil	Soil – MP1 (present study)	Soil – MP2 (Indraratna et al., 2020a)
Liquid limit, w_{LL}	26%	25%
Plasticity index, PI	11%	10%
Initial moisture content	15%	20%
Specific Gravity, G_s	2.63	2.65
USCS Classification	CL	CL
Maximum dry density, $\rho_{d,max}$ (kg/m^3)	1814	1820
Finer fraction (< 75 μm)	30%	54%

Table 2 Summary of the threshold number of cycles N_{thr} and threshold residual axial strains

$\epsilon_{ar,thr}$ for different loading conditions

Soil	Initial Density	Relative Compaction	CSR	f (Hz)	N_{thr}	$\epsilon_{ar,thr}$ (%)
Soil - MP1 (Present study)	1790	99%	0.5	1.0	50	1.6
				2.0	240	1.4
				5.0	3300	0.95
			1.0	1.0	10	1.75
				2.0	22	1.5
				5.0	40	1.3
	1680	93%	0.4	1.0	310	1.05
			0.5	1.0	11	1.2
				2.0	100	0.7
Soil - MP2 (Indraratna et al., 2020a)	1710	94%	0.3	5.0	58	0.52
			0.4		33	0.9
			0.5		12	1.3

Figures

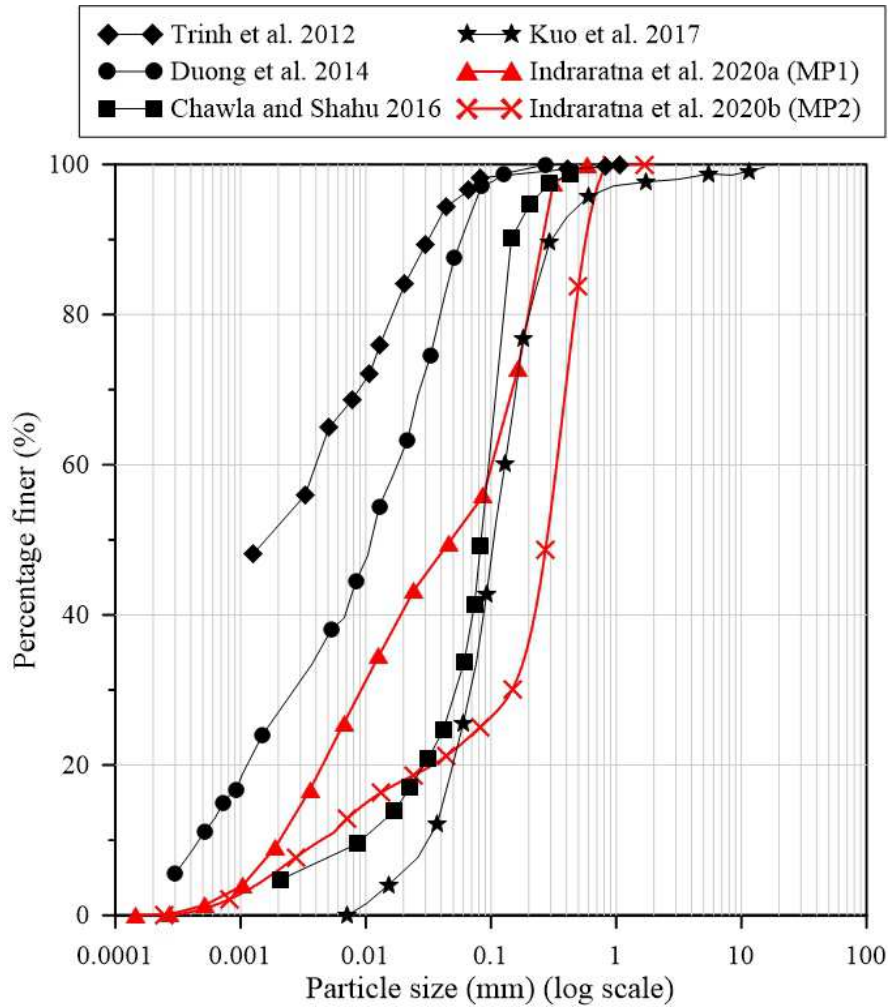


Fig. 1 Particle size distribution of subgrade soils reported to have mud pumped in the field

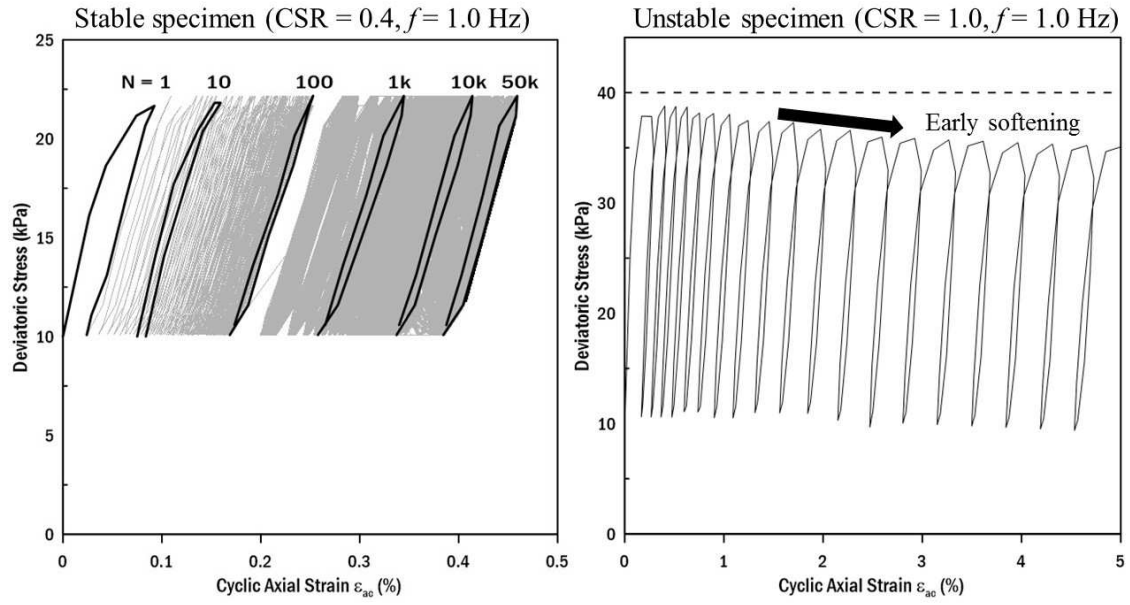


Fig. 2 Stress-strain loops for the stable (low CSR) and unstable specimen (high CSR)

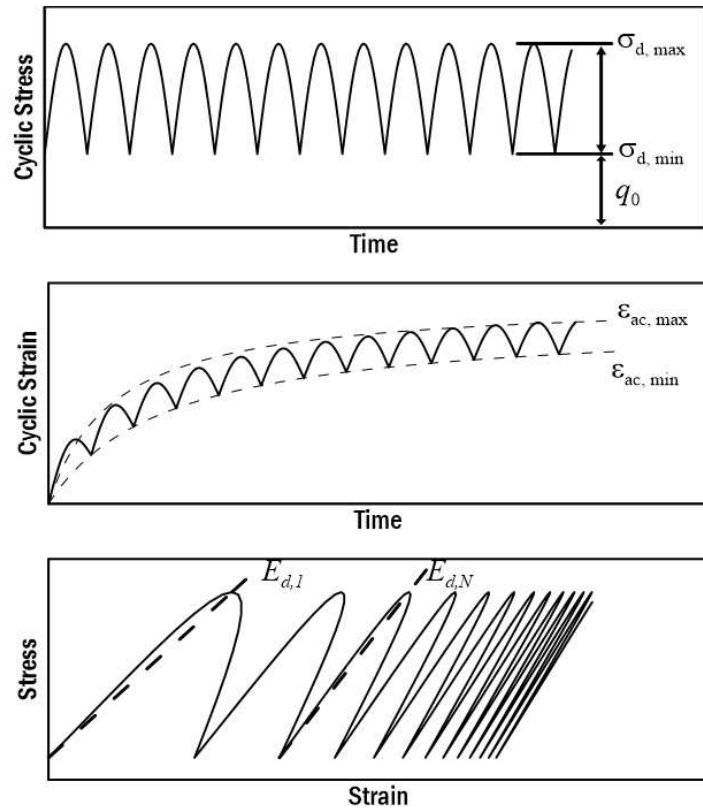


Fig. 3 Generalized stress-strain behaviour for a specimen subjected to one-way stress-controlled cyclic loading under undrained condition

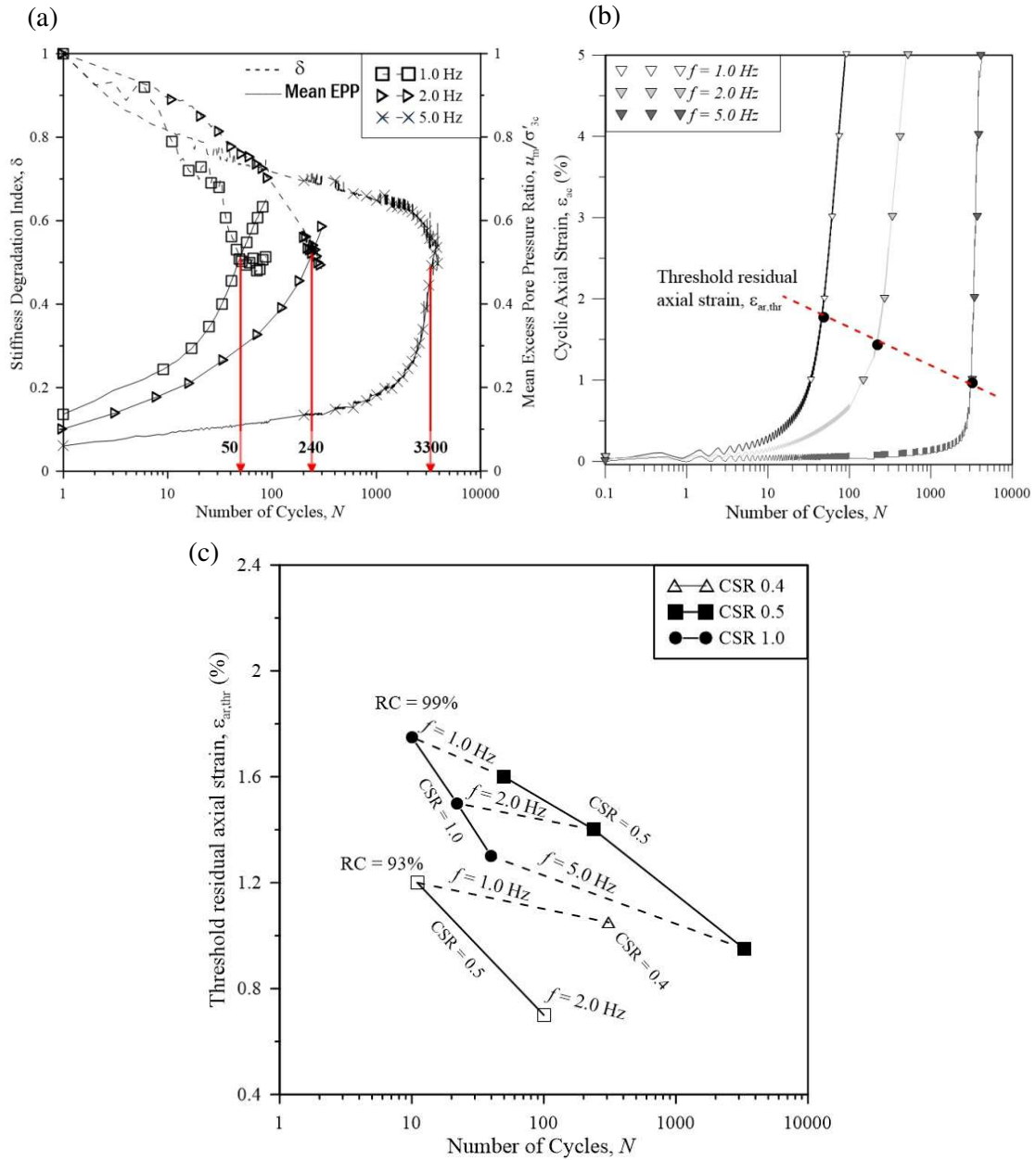
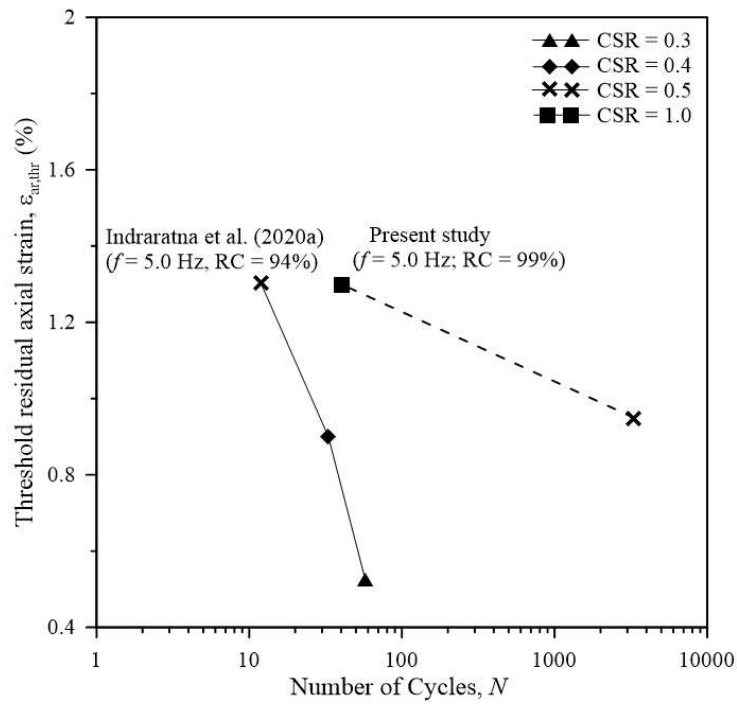


Fig. 4 (a) Predicting the threshold number of cycles N_{thr} , from the degradation index and mean EPP plots (b) Evaluating threshold residual axial strains ($\rho_d = 1790 \text{ kg/m}^3$, CSR = 0.5) (c) Threshold residual axial strain for various loading conditions for Soil – MP1

(a)



(b)

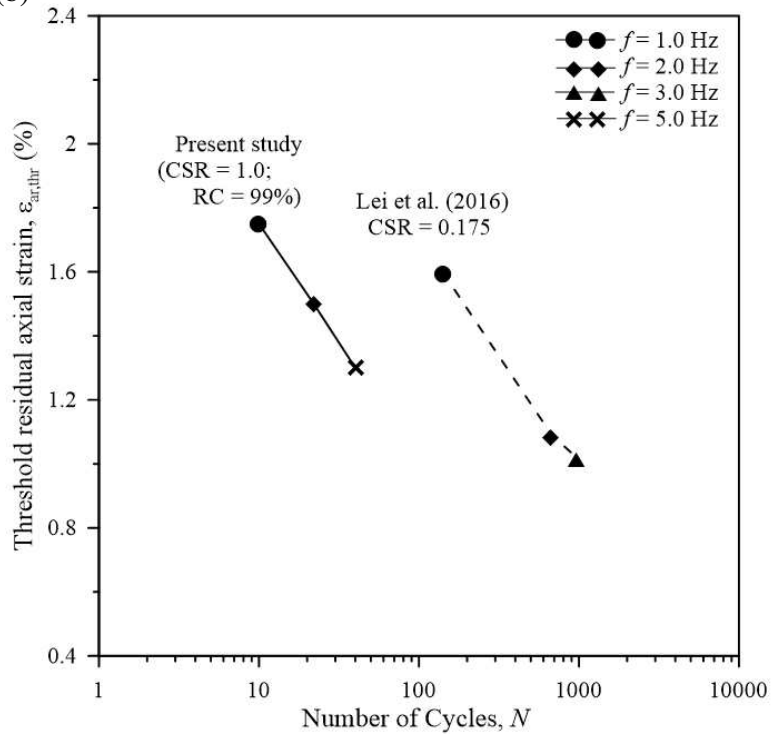


Fig. 5 Comparison of the threshold axial strains (a) for the two soils (Soil-MP1 and Soil-MP2) at $f = 5.0$ Hz (b) with respect to different loading frequency

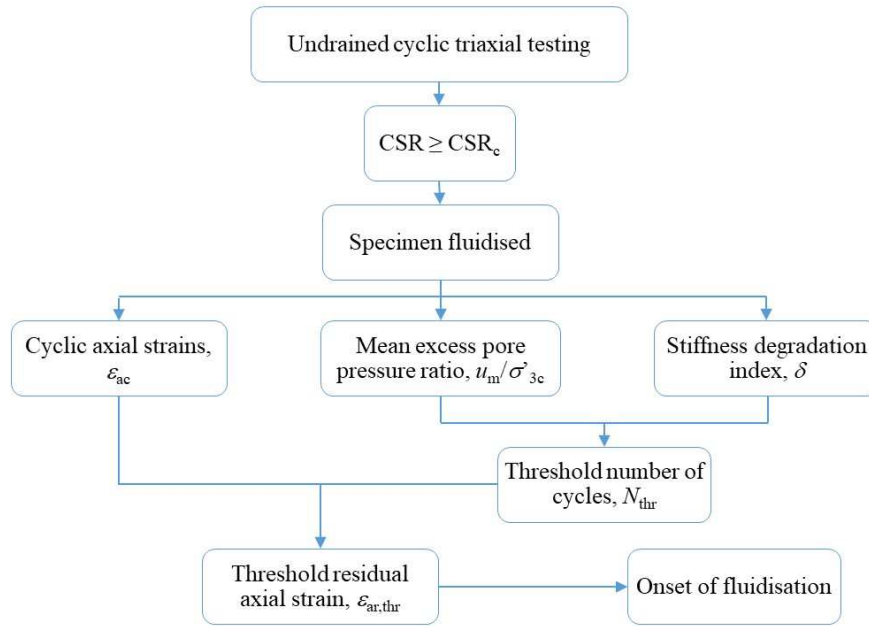


Fig. 6 Flowchart for predicting the onset of fluidisation for mud pumping prone soils using stiffness degradation index

References:

- ASTM D698-07 Standard. 2012. Standard Test Methods for Laboratory Compaction Characteristics of Soil Using Standard Effort.
- Cai, Y., Wu, T., Guo, L. and Wang, J. 2018. Stiffness degradation and plastic strain accumulation of clay under cyclic load with principal stress rotation and deviatoric stress variation. *Journal of Geotechnical and Geoenvironmental Engineering*, **144**(5): 04018021.
- Chawla, S. and Shahu, J.T. 2016. Reinforcement and mud-pumping benefits of geosynthetics in railway tracks: Model tests. *Geotextiles and Geomembranes*, 44: pp. 366-380.
- Duong, T.V., Cui, Y.-J., Tang, A.M., Dupla, J.-C., Canou, J., Calon, N., Robinet, A., Chabot, B. and De Laure, E. 2014. Physical Model for Studying the Migration of Fine Particles in the Railway Substructure. *Geotechnical Testing Journal*, 37(5): pp. 1-12.
- Hasnain, M.M., McCarter, W.J., Woodward, P.K. and Connolly, D.P. 2020. Railway Subgrade Performance after Repeated Flooding Large-scale Laboratory Testing. *Transportation Geotechnics*. doi: 10.1016/j.trgeo.2020.100329
- Hasnain, M.M., McCarter, W.J., Woodward, P.K., Connolly, D.P. and Starrs, G. 2017. Railway subgrade performance during flooding and the post-flooding (recovery) period. *Transportation Geotechnics*, **11**: 57-68. doi: 10.1016/j.trgeo.2017.02.002
- Hsu, C.-C. and Vucetic, M. 2006. Threshold shear strain for cyclic pore-water pressure in cohesive soils. *Journal of Geotechnical and Geoenvironmental Engineering*, **132**(10): 1325-1335.
- Indraratna, B., Korkitsuntornsan, W. and Nguyen, T.T. 2020a. Influence of kaolin content on the cyclic loading response of railway subgrade. *Transportation Geotechnics*, **22**: 100319. doi: <https://doi.org/10.1016/j.trgeo.2020.100319>.
- Indraratna, B., Singh, M., Nguyen, T.T., Leroueil, S., Abeywickrama, A., Kelly, R. and Neville, T. 2020b. Laboratory study on subgrade fluidization under undrained cyclic triaxial loading. *Canadian Geotechnical Journal*. doi: <https://doi.org/10.1139/cgj-2019-0350>.
- Kallioglou, P., Tika, T. and Pitilakis, K. 2008. Shear modulus and damping ratio of cohesive soils. *Journal of Earthquake Engineering*, **12**(6): 879-913.
- Konstadinou, M. and Georgiannou, V.N. 2014. Prediction of pore water pressure generation leading to liquefaction under torsional cyclic loading. *Soils and Foundations*, **54**(5): 993-1005. doi: <https://doi.org/10.1016/j.sandf.2014.09.010>.
- Kuo, C., Hsu, C., Wu, C., Liu, P. and Chen, D. 2017. Study on the Piping Path and Mechanism of Mud-pumping in Railway Subgrade. 19th International Conference on Soil Mechanics and Geotechnical Engineering. Seoul, South Korea.
- Lei, H., Li, B., Lu, H. and Ren, Q. 2016. Dynamic Deformation Behavior and Cyclic Degradation of Ultrasoft Soil under Cyclic Loading. *Journal of Materials in Civil Engineering*, ASCE, **28**(11): 04016135. doi: doi:10.1061/(ASCE)MT.1943-5533.0001641.
- Leng, W., Xiao, Y., Nie, R., Zhou, W. and Liu, W. 2017. Investigating strength and

- deformation characteristics of heavy-haul railway embankment materials using large-scale undrained cyclic triaxial tests. *International Journal of Geomechanics*, **17**(9): 04017074.
- Liu, J. and Xiao, J. 2010. Experimental study on the stability of railroad silt subgrade with increasing train speed. *Journal of Geotechnical and Geoenvironmental Engineering*, **136**(6): 833-841.
- Mamou, A., Clayton, C., Powrie, W. and Priest, J. 2019. The role of clay content on the response of railway track foundations during free-to-drain cyclic changes in principal stress rotation. *Transportation Geotechnics*. **20**: (100246). doi.org/10.1016/j.trgeo.2019.100246
- Mortezaie, A.R. and Vucetic, M. 2013. Effect of Frequency and Vertical Stress on Cyclic Degradation and Pore Water Pressure in Clay in the NGI Simple Shear Device. **139**(10): 1727-1737. doi:10.1061/(ASCE)GT.1943-5606.0000922.
- Nguyen, T.T. and Indraratna, B. 2020. A coupled CFD-DEM approach to examine the hydraulic critical state of soil under increasing hydraulic gradient. *ASCE International Journal of Geomechanics*, **20**(9): 04020138-1:15. doi: https://doi.org/10.1061/(ASCE)GM.1943-5622.0001782.
- Nguyen, T.T., Indraratna, B., Kelly, R., Phan, N.M. and Haryono, F. 2019. Mud pumping under railtracks: mechanisms, assessments and solutions. *Australian Geomechanics Journal*, **54**(4): 59-80.
- Powrie, W., Yang, L. and Clayton, C.R. 2007. Stress changes in the ground below ballasted railway track during train passage. *Proceedings of the Institution of Mechanical Engineers, Part F: Journal of Rail Rapid Transit*, **221**(2): 247-262.
- Singh, M., Indraratna, B. and Rujikiatkamjorn, C. 2019. Use of geosynthetics in mitigating the effects of mud pumping: a railway perspective. *In Geotechnics for transportation infrastructure. Edited by R. Sundaram, Shahu, J. & Havangi, V. Springer, Singapore.*
- Soralump, S. and Prasomsri, J. 2016. Cyclic pore water pressure generation and stiffness degradation in compacted clays. *Journal of Geotechnical and Geoenvironmental Engineering*, **142**(1): 04015060.
- Trinh, V.N., Tang, A.M., Cui, Y.-J., Dupla, J.-C., Canou, J., Calon, N., Lambert, L., Robinet, A. and Schoen, O. 2012. Mechanical characterisation of the fouled ballast in ancient railway track substructure by large-scale triaxial tests. *Soil and Foundations, The Japanese Geotechnical Society*, **52**(3): pp. 511-523.
- Zhou, J. and Gong, X. 2001. Strain degradation of saturated clay under cyclic loading. *Canadian Geotechnical Journal*, **38**: 208-212.