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Missing Value Imputation for Multi-view Urban Statistical Data via Spatial Correlation Learning

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Abstract—As a developing trend of urbanization, massive amounts of urban statistical data with multiple views (e.g., views of Population and Economy) are increasingly collected and benefited to diverse domains, including transportation service, regional analysis, etc. Unfortunately, these statistical data that are divided into fine-grained regions usually suffer from missing value problem during the acquisition and storage processes. It is mianly caused by some inevitable circumstances, e.g., the document defacement, statistical difficulty in remote districts, and inaccurate information cleaning, etc. Those missing entries which make valuable information invisible may distort the further urban analysis. To improve the quality of missing data imputation, we propose an improved spatial multi-kernel learning method to guide the imputation process incorporating with the adaptive-weight non-negative matrix factorization strategy. Our model takes into account the regional latent similarities and the real geographical positions as well as the correlations among various views that are able to complete missing values precisely. We conduct intensive experiments to evaluate our method and compare with other state-of-the-art approaches on real-world datasets. All the empirical results show that the proposed model outperforms all the other state-of-the-art methods. Additionally, our model represents a strong generalization ability across multiple cities.

Index Terms-Missing data imputation, Spatial data, Statistic data, Multi-view

1 INTRODUCTION

RBANIZATION'S rapid progress has currently modernized many people's lives. The generated statistic 3 data play an irreplaceable role in a large number of city development and social services, e.g., regional planning, 5 urban computing, failure detection, and transportation man-6 agement [1]–[5]. These statistical data record various types 7 of information that usually contain multi-fold views (e.g., 8 views of Family, Income, Population and Business). Such statistics reveal the growth gaps among different adminis-10 trative regions from various perspectives. Fig. 1 gives an 11 example of the regional statistics. The Business area r_2 con-12 tains four views. Among them, the economy view records 13 the key economic indicators for fine-grained regions¹, such 14 as employee statistics and the number of industries; and the 15 family view consists of detailed family information of all 16 living sizes. 17

The statistic data provide key statistics to governments, business and the community on social science, for the benefit of many aspects of human life². However, in some places, statistical data are hard to be entirely acquired due to document defacement, error recordings, and statistician misplay, resulting in data-missing and sparsity problem.

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1. The fine-grained area partition is based on the Australian Bureau of Statistics (ABS) standard. https://www.abs.gov.au/

2. https://www.abs.gov.au/about?OpenDocument&ref=topBar

Such missing values hide useful information which may 24 cause distorted results for further analysis. For example, in 25 the point of interest recommendation problem [6], economy 26 and population are two of the most important influence fac-27 tors of determining area functions. A business area should 28 have a high-quality economy and a larger population. If 29 the economy attributes were missing, this area would be 30 grouped into the residential district because the solely con-31 sideration of population. To the best of our knowledge, 32 to present, it is an under-studied field concerning on this 33 specific problem. Yet it is a real-world demand from the 34 national government. Accordingly, an effective missing-data 35 imputation method for urban statistical data should be de-36 vised, which is important for the reliable urban computing 37 and government services. 38

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In this paper, we explore the missing-data imputation problem in urban statistical datasets collected from the Australian Bureau of Statistics (ABS) and the New Zealand Stats (NZS)³. Such a missing value imputation task for the multi-view urban statistical data is much more difficult than completing missing values for other datasets as this type of problem has some unique challenges:

Spatial Correlation Mining. The statistical data focusing on 46 fine-grained regions may change over locations significantly 47 and non-linearly. Even though the First Law of Geography 48 emphasizes that everything is related to everything else, 49 but near things are more related than distant ones [7], the 50 potential similarities need to be considered when analyzing 51 the spatially related data [8], [9]. Therefore, to properly 52 recover the missing information of statistical data, we need 53 to consider the regional similarities. As illustrated in Fig. 1, 54

3. https://www.stats.govt.nz/

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Fig. 1: Urban statistical data illustration and the regional similarity. *First, the tabular data give an example of the property of statistics; second, to properly recover the missing information of statistical data, we need to consider the regional similarities, as represented in the map figure.*

the properties of business area b_1 are similar to the 'Sydney center' because they are neighboring each other. However, although the business area r_2 is closer to the park area in terms of the physical distance, the statistical data of r_2 are more analogous to the 'Sydney center' than the 'Park' because they have a similar functional property (business centre).

Multi-view Problem. The complicated underlying interac-62 tions suggest that simply recovering the missing informa-63 tion without considering the correlations among attributes 64 and multi-modes will end up with a poor performance [10]. 65 For example, the economy view has strong correlations with 66 the income and population views, so that a high-quality 67 economy in a region usually goes along with a better income 68 and a larger population; and a low-level economy in a 69 region has a high probability of being connected with a 70 lower income and a smaller population. In this case, only 71 considering per view separately does not utilize the rela-72 tionships between attributes and multi-modes. Therefore, 73 how to integrate the whole views into a unified model is 74 a principal challenge need to be solved. 75

Missing Temporal Information. In this specific problem, 76 almost all the missing statistic values in the current year 77 were also missing in the past years, which may be caused by 78 the region restriction and complicated human-made errors. 79 Based on the real phenomenon, the temporal dimension 80 is unavailable. Besides, this violates the basic assumption 81 of matrix completion [11] that the unobserved entries are 82 sampled uniformly at random. Thus matrix completion-83 based approaches may not work in this case. Note that, 84 this challenge is not solely a matter for statistical data but 85 86 appears in other fine-grained spatio-temporal data mining problems [12], [13], where the temporal information in some 87 fine-grained areas cannot be collected at any time. 88

⁸⁹ In the current literature, the existing missing data impu-

tation approaches, while yielding good estimations for miss-90 ing values in the single view, are poor in terms of completing 91 missing data on multiviews, especially when associated 92 with the spatial characteristic. For example, numerous ap-93 proaches can be applied in urban statistical data, e.g., mean-94 filling (MF), k-nearest-neighbor (KNN) filling [14], and 95 collaborative filtering based methods [15]. Most of them, 96 however, have been proposed to focus on the single view 97 problem. Besides, although several spatiotemporal methods 98 can infer the missing information based on the knowledge 90 from both spatial and temporal domains [8], [16], [17], they 100 do not perform well when the missing temporal information 101 challenge appears. To handle all challenges well, we devise 102 a model via the spatial correlation learning. In detail, the 103 method integrates a spatial multi-kernel clustering method 104 and an adaptive-weight non-negative matrix factorization⁴ 105 (NMF) method for solving the multi-view spatially related 106 tasks. We summarize the main contributions and innova-107 tions of this paper as follows: 108

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• To address the multi-view problem with spatial characteristics, we design a Spatially related Multi-Kernel K-Means (S-MKKM) approach to identify the underlying relationships among multi-fold views and capture the regional similarities.

• We propose an adaptive-weight non-negative matrix factorization method to leverage the information learned above to tackle the multi-view missing data imputation problem. Besides, the proposed method also takes guidance from the single-view and the real geographic information with *KNN* strategy into consideration.

• A multi-view missing data imputation method for urban statistical data via spatial correlation learning named SMV-NMF is proposed. SMV-NMF does not rely on the temporal information but achieves a great performance by only using the spatial information.

• We perform a collection of experiments on six realworld datasets to prove the effectiveness of our method compared with other state-of-the-art models. All the evaluation results show that the proposed method SMV-NMF yields the best performance. Furthermore, SMV-NMF shows the strong generalization ability that can transfer the constructed model from one urban dataset to another well.

This paper is an extended version of [18], the nov-132 elty and improvements of this paper are: we leverage an 133 improved adaptive-weight matrix factorization strategy to 134 control the knowledge extraction, provide more detailed 135 theoretical analyses and conduct intensive experiments for 136 the comprehensively evaluation from many perspectives. 137 The remainder of this paper is organized as follows: Section 138 2 includes a literature review. Section 3 formally defines the 139 problem and shows the preliminary methods. Our model is 140 proposed in Section 4. All experimental results are shown in 141 Section 5. Finally, conclusions are drawn in Section 6. 142

2 RELATED WORK

In this section, we review the current studies on the spatiotemporal missing data imputation. Then provide the multiview model discussions.

4. We add the non-negativity constraint since almost all the urban statistic data are non-negative.

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147 2.1 Missing Data Imputation for Spatio-temporal Data

Missing data imputation is a significant task for data anal-148 vsis [19]. It aims at filling out the data with estimation 149 value. In the spatially related problem, neighborhood and 150 151 collaborative filtering [8], [20] based methods are two kinds of dominant approaches in missing data filling. Although 152 some classical methods (e.g., zero-filling, mean value filling, 153 regression models) can be applied to the spatial missing data 154 imputation, they have disadvantages in nature, i.e, they are 155 not designed for this spatial problem. [21] used the inverse 156 distance weighting (IDW) method to interpolate the spatial 157 rainfall distribution. [22] utilized the spatial information as 158 inputs in a residual kriging method to estimate the aver-159 age monthly temperature. Unlike the spatial model, some 160 successful spatio-temporal models were proposed for use 161 with time stream data [8], [9], [16], [17]. For example, [8] de-162 velops a spatio-temporal multi-view approach (ST-MVL) to 163 collectively complete missing values in a collection of geo-164 sensory time series data. It considers that 1) the temporal 165 correlations between readings at various time spans in the 166 167 same series and 2) the spatial correlations between different time series. However, they focused on filling missing entries 168 by considering both spatial and temporal properties, and 169 would not perform well on the static spatial data with-170 out the temporal information. Furthermore, these discussed 171 methods leveraged the spatial guidance but did not consider 172 the problem on multi-view datasets. 173

Here we also discuss other spatio-temporal missing data
imputation methods used in the real-time applications. For
a large city network, we are faced with a truth that data
is not everywhere, especially in the real-time system, there
may be not enough time to collect complete data.

A naive way is to average the values near missing data.
Research by [23] used the simple average method to impute
the missing data. As they said, this was mainly because the
missing ratios for the selected sensors are sufficiently low.
However, when faced with large-scale traffic network, the
number of missing data is probably huge, and the average
method cannot be adopted.

Many traffic prediction methods incorporate missing 186 data completion into prediction steps. [24] dealt with miss-187 ing data by 'expanded Bayesian network'. They made use 188 of the causal relations in traffic network, and constructed 189 the network by replacing the missing data with its causal 190 variables. The main shortage for this method is that once 191 the structures and parameters of the Bayesian network is 192 193 trained, the relative position and time for missing data is also fixed. This is usually unreal, because data is likely to 194 be missed at different time and sites. In other words, one 195 model can only handle with one case of missing data. If we 196 are facing a real traffic network, it is impossible for us to 197 enumerate every condition and train for each condition a 198 model. 199

[25] proposed a data completion method by matrix factorization. The Traffic data were structured as matrix with each entry X_{ij} denotes traffic speed between node *i* and node *j*. Based on the non-negative matrix tri-factorization framework, they got the latent attribute matrix of nodes and the attribute interaction matrix. By minimising the known error together with constraint using Laplacian matrix [26], missing data completion was accomplished by reconstructing data matrix with factor matrices. 200

Tensor decomposition [27] was used by [28] to com-209 plete missing computer network traffic data. They used 210 a weighted optimization version of CP decomposition to 211 impute the missing data. [29] improve this method through 212 Tucker decomposition. They got a comparatively accurate 213 result even when the missing ratio of data was quite high 214 (up to 75%). These methods organised data as a three-215 way tensor, with day mode, hour mode and interval mode. 216 [30] used this method to floating car data and get a better 217 coverage of traffic state. In this paper, data is organised as 218 a three-way tensor of link mode, interval mode and day 219 mode. Similar method was used in research of [31]. They 220 treated data to be predicted as missing data, and trained 221 the decomposition model with historical data as rough 222 prediction. There are two main problems of these tensor-223 based methods. First, they can only deal with one road or 224 several road segments at a time, which is not enough for 225 a citywide traffic network. Second, they did not define a 226 rule for choosing the ranks for tensor decompositions, but 227 the rank is one of the most crucial parameters for tensor 228 decompositions. 229

2.2 Multi-view Learning

We discuss the multi-view studies because the missing-data 231 usually contain the multiply views. Multi-view learning 232 methods involved the diversity of different views that can 233 jointly optimize functions based on various feature subsets 234 [32], [33]. [34] proposed a matrix co-factorization based 235 method (MVL-IV) to embed different views into a shared 236 subspace, such that the incomplete views can be estimated 237 by the information on observed views. To connect multiple 238 views, MVL-IV assumes that different views have distinct 230 'feature' matrices (i.e., $\{H_i\}_{i=1}^d$), but correspond to the same 240 coefficient matrix (i.e., W). However, it does not exploit 241 the spatial correlations and may suffer from the imbalance 242 problem, i.e., if there is a substantial missing ratio gap 243 between views, the coefficient matrix W is mostly learned 244 from the dense view. The proposed method has addressed 245 this weakness by introducing guidance matrices. Another 246 widely used strategy for solving the multi-view problem 247 is tensor factorization [35], [36], but this restricts a regular 248 tensor that requires the number of dimensions per view 249 to be the same. Moreover, multiple kernel learning with 250 incomplete views [37], [38] only focuses on completing 251 missing kernels instead of filling missing values. To the best 252 of our knowledge, none of the above studies considered 253 both spatial and multi-view problems. Hence, this paper 254 proposes an effective missing value imputation model for 255 multi-view urban statistical data. 256

3 PROBLEM DESCRIPTION AND PRELIMINARIES

Before clarifying our model, we firstly introduce some basic notations, operations and algorithms used in this paper. The main symbols used in this paper are summarized in Table 1. 260

3.1 Problem Description

Focusing on the multi-view missing-value problem, each 262 set of urban statistical data includes multi-fold views, e.g., 263

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Fig. 2: The flowchart of our proposed method. In the learning process, given a set of multi-view urban statistical data, we first use the muti-view NMF as a basic imputation method, then we propose a multi-view spatial similarity guidance with adaptive-weight strategy to build guidance X_p^{mv} . Next, SMV-NMF also considers single-view and real geographic locations. Finally, the target missing value can be inferred by Algorithm 1.

Symbols	Descriptions		
$X = [X_1 X_2 \dots X_d]$	original data matrix contains d views		
W ; H_p	latent space matrices, p indicates the p -th view		
$V\cdotar{V}$	indication matrices for all complete		
<i>Ip</i> , <i>Ip</i>	entries and missing entries of <i>p</i> -th view		
le: 1	the number of dimensions of		
κ, ι	latent space; and the number of clusters		
	the number of regions;		
$n;d;m_p$	and the number of views;		
	the dimension of attributes in the p -th view		
$Z_p; Z'_p$	weight matrices of the <i>p</i> -th view		
L	graph Laplacian matrix		
V	the clustering matrix		
$X^{mv}; X^{sv}; X^{knn}$	three guidance matrices		
<i>K</i> _β ; β	the kernel matrix; the coefficients of kernels		
$\lambda_1;\lambda_2;\lambda_3;lpha$	regularization parameters		

TABLE 1: Symbol description.

Income, Population, Economy views, etc. As shown in Fig. 3, given the incomplete statistic dataset with *n* regions $(r_1,...,r_n)$ and *d* views, where the dimension of attributes in the *p*-th view is m_p ($1 \le p \le d$), this paper aims to find the interactions among views and fill missing entries precisely.

269 3.2 Non-negative Matrix Factorization (NMF)

In the missing data imputation problem, the non-negative 270 matrix factorization method decomposes the original matrix 271 $X \in \mathbb{R}^{n \times m}_+$ into two matrices $W \in \mathbb{R}^{k \times n}_+$ and $H \in \mathbb{R}^{k \times m}_+$, 272 where W and H represent the latent spaces. In our problem, 273 W indicates the latent features of the regions; H indi-274 cates the latent features of the data view. Each column 275 in these matrices represents k attributes of corresponding 276 regions and statistical fields. The interaction between these 277 attributes determines the statistical value between the re-278 gions and statistic fields. Therefore, the basic missing data 279 imputation model based on NMF can be described as the 280 following optimization objective: 28

$$\min_{V \ge 0, H \ge 0} ||Y \odot (X - W^{\top} H)||_F^2 \tag{1}$$

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3.3 Multiple Kernel K-means (MKKM)

The original data X is combined by d data views (X =288 $[X_1...X_d]$) as shown in Fig. 3. Let $\{\mathbf{x}_i\}_{i=1}^n$ be a collection 289 of *n* samples (region), \mathbf{x}_i represents the statistical features of 290 the *i*-th region, and $\phi_p(\cdot)$ be the *p*-th view mapping that 291 maps x onto the *p*-th reproducing kernel Hilbert space. 292 In this case, each sample has multiple feature representa-293 tions defined by a group of feature mappings $\phi_{\beta}(\mathbf{x}_i) =$ 294 $[\beta_1 \phi_1(\mathbf{x}_i)^{\top}, \cdots, \beta_d \phi_d(\mathbf{x}_i)^{\top}]'$, where $\boldsymbol{\beta} = [\beta_1, \cdots, \beta_d]'$ 295 consists of the coefficients of the d base kernels. These 296 coefficients will be optimized during learning. Based on the 297 definition of $\phi_{\beta}(\mathbf{x})$, a kernel function can be expressed as 298 $\kappa_{\beta}(\mathbf{x}_i, \mathbf{x}_j) = \phi_{\beta}(\mathbf{x}_i)^{\top} \phi_{\beta}(\mathbf{x}_j) = \sum_{p=1}^d \beta_p^2 \kappa_p(\mathbf{x}_i, \mathbf{x}_j)$. And a kernel matrix K_{β} is then calculated by applying the kernel 299 300 function $\kappa_{\beta}(\cdot, \cdot)$ to $\{\mathbf{x}_i\}_{i=1}^n$. Based on the kernel matrix K_{β} , 301 the objective of MKKM can be written as: 302

$$\min_{V,\beta} \operatorname{Tr}(K_{\beta}(\mathbf{I}_{n} - VV^{\top}))$$

$$t. \ V \in \mathbb{R}^{n \times l}, V^{\top}V = \mathbf{I}_{l}, \beta^{\top}\mathbf{1}_{d} = 1, \beta_{p} \ge 0, \forall p,$$
(2)

where *V* is the clustering matrix; $\mathbf{1}_d \in \mathbb{R}^d$ is a column vector with all 1 elements; \mathbf{I}_n and \mathbf{I}_l are identity matrices with size *n* and *l*; *l* is the number of clusters. 303

4 THE PROPOSED METHOD

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In this section, we propose our missing data imputation model SMV-NMF. We will describe how to address the multi-view problem, and how to capture the spatial correlation via the multiple kernel learning. Fig. 2 shows the flowchart of our model.

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 \boldsymbol{x}

 x_2

x

 x_4

s

5.3

2 9.4

View 1: X

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Fig. 3: Problem description. For an urban dataset containing *n* regions $(r_1,...,r_n)$, our method aims to impute the missing values with a high accuracy. For example, the imputation process for $x_{2(1,3)}$ will both consider the internal (feature similarities) and external knowledge (view interactions) to fill the target entry.

312 4.1 Multi-view NMF

The multi-view NMF is an effective method to handle the multi-view problem. In our problem, we aim to learn a latent subspace $W \in \mathbb{R}^{n \times k}_+$ by multiple views $\{X_1...X_d\}$ through the multi-view generation matrices $H_p \in \mathbb{R}^{k \times m_p}_+$. In this case, the basic missing data imputation model can be described as the following optimization objective:

$$\min_{V \ge 0, H_p \ge 0} \mathcal{N} = \sum_{p=1}^{d} ||Y_p \odot (X_p - WH_p)||_F^2, \qquad (3)$$

where Y_p are indicator matrices for the *p*-th view whose entry $Y_p(i,j)$ is one if $X_p(i,j)$ has been recorded (for observed values).

We utilize the multi-view NMF method to find the potential connections among views. One of the advantages of non-negative constraint is the reasonable assumptions of latent characters and interpretability of the results [39]–[41]. Furthermore, due to the fact of urban statistical data, the missing values must be non-negative, thus *W* and *H* should be constrained into non-negative field.

329 4.2 Multi-view Spatial Similarity Guidance

In general, the multi-view matrix factorization based meth-330 ods usually suffer from the imbalance problem as discussed 331 in Section 2.2. To address this problem, we propose the 332 similarity guidance X_p^{mv} for the *p*-th view X_p in this 333 paper. To extract associations among different views of 334 spatially related data, we devise a method to capture re-335 gional similarities via the spatial multiple kernel learning, 336 named S-MKKM. The basic idea is that the development 337 of a city gradually fosters different functional groups, such 338 as educational and business districts, where the regions 339 belonging to the same group would have strong connections 340 with each other [3]. S-MKKM leverages the multi-kernel 341 k-means (MKKM) clustering algorithm combined with a 342 343 graph Laplacian dynamics strategy (an effective smoothing approach for finding spatial structure similarity [25], [41]-344 [43]) to cluster regions into the functional groups. Specifi-345 cally, we construct a graph Laplacian matrix L, defined as 346



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View d: X_d^{mv}

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0.7 0.1

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L = D - M, where M is a graph proximity matrix that is constructed from the regional physical topology, i.e., $M_{(i,j)}$ and D is = 1 if and only if the region \mathbf{x}_i is contiguous to \mathbf{x}_j , and D is a diagonal matrix $D_{(i,i)} = \sum_j (M_{(i,j)})$. With this constraint, the S-MKKM model can be formulated as follows: 351

$$\min_{V,\boldsymbol{\beta}} \operatorname{Tr}(K_{\boldsymbol{\beta}}(\mathbf{I}_n - VV^{\top})) + \alpha \operatorname{Tr}(V^{\top}LV)$$

$$t. \ V \in \mathbb{R}^{n \times l}, V^{\top}V = \mathbf{I}_l, \boldsymbol{\beta}^{\top}\mathbf{1}_d = 1, \beta_p \ge 0, \forall p,$$
(4)

where α is the regularization parameter; *V* is the consensus clustering matrix.

To get the complete kernels, we initially impute the missing data for each view by a simple method, such as KNN or MF (the effects of different initializations are illustrated in Section 5.7). Therefore, this problem can be solved by alternately updating V and β [38]: 358

i) Optimizing V with fixed β . With the kernel coefficients β fixed, V can be obtained by the following strategy: 360

$$V \leftarrow choose \ the \ l \ smallest \ eigenvectors \ of \ (-K_{\beta} + \alpha L)$$
(5)

ii) Optimizing β with fixed V. With V fixed, β can be optimized via solving the quadratic programming with linear constraints:

$$\beta_p = \frac{tr(K_p(\mathbf{I} - VV^{\top}))^{-1}}{\sum_{p=1}^d (tr(K_p(\mathbf{I} - VV^{\top}))^{-1})}$$
(6)

The objective of the S-MKKM method is to discover 364 the regions with similar properties and build the guidance 365 matrices X_p^{mv} . We employ the clustering result to build a 366 matrix X_p^{mv} , that is after having gotten V, X_p^{mv} can be built. 367 Fig. 4 illustrates an example of this process. The construction 368 process of X_n^{mv} is that i) for the unknown entry x_{ij} , and 369 the region $\mathbf{x}_i \in c$ -th cluster, we use its corresponding value 370 $x_{c(i),j}$ from the centroid region to impute x_{ij} ; ii) if the 371 corresponding value of centroid region is also missed, a 372

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greedy strategy will be used to find the nearest observedvalue for imputation.

375 4.3 Adaptive-Weight NMF

To learn the knowledge from X_p^{mv} more reliably, we propose an adaptive weighting strategy in the NMF imputation process. The adaptive-weight matrix of the *p*-th view is denoted as $Z_p \in \mathbb{R}^{n \times m_p}_+$, which is built by an exponential function as shown in Equation (7) and (8).

$$z_{p(i)} = e^{-Dist(\mathbf{v}_i, \mathbf{v}_{c(i)})},\tag{7}$$

$$Z_p = z_p \mathbf{1}_{m_p}^{\top}, \tag{8}$$

where $Dist(\cdot, \cdot)$ is the Euclidean distance calculating from 38 the geo-location (\mathbf{v}_i) and its corresponding centroid region 382 $(\mathbf{v}_{c(i)})$, here we use the latent embedding \mathbf{v}_i to represent the 383 geo-location of region *i*, and $\mathbf{v}_{c(i)}$ represents the centroid 384 of the *c*-th cluster which contains region \mathbf{v}_i ; $z_p \in \mathbb{R}^n_+$ is 385 a column vector and $\mathbf{1}_{m_p}$ is all-ones vector with size m_p . 386 It is not a straight way for imputation, but the adaptive-387 weight matrix Z_p controls how much information can be 388 extracted. Z_p adjusts the penalty of each estimated entry. 389 As emphasised in the First Law of Geography [7], the near 390 things have more spatial correlations than distant things. If 391 the distance between \mathbf{x}_i and $\mathbf{x}_{c(i)}$ is small, we want a high 392 penalty to guide the imputation process. 393

To this stage, the adaptive-weight NMF can be described as the following optimization function:

$$\min_{W \ge 0, H_p \ge 0} \mathcal{M} = \sum_{p=1}^d ||\bar{Y_p} \odot Z_p \odot (X_p^{mv} - WH_p)||_F^2, \quad (9)$$

where $\bar{Y}_p = \mathbf{1} - Y_p$, **1** is an all one matrix that has the same size as Y_p ; X_p^{mv} is a homomorphic matrix of X_p .

We consider the adaptive-weight NMF jointly, then we can get:

$$\min_{W \ge 0, H_p \ge 0} \mathcal{J}_1 = \mathcal{N} + \lambda_1 \mathcal{M}, \tag{10}$$

where λ_1 is the regularization parameter to control the learning rate of X_p^{mv} .

402 4.4 Improved by Single-view and KNN Guidances

S-MKKM aims to find the regional groups by consider-403 ing multiple views simultaneously. However, it is obvious 404 that each view has its characteristics, and the relationships 405 between regions in one specific view are also critical for 406 imputing missing entries. To consider the above knowledge, 407 we apply the spatially related kernel k-means (S-KKM) to 408 capture the similarities among regions of each view. It is 409 essentially analogous to the learning process of S-MKKM as 410 discussed in Section 4.2, but considering each view, respec-411 tively. For one view X_p , the S-KKM model is expressed as 412 follows: 413

$$\min_{V_p} \quad \operatorname{Tr}(K_p(\mathbf{I}_n - V_p V_p^{\top})) + \alpha \operatorname{Tr}(V_p^{\top} L V_p)$$

s.t. $V_p \in \mathbb{R}^{n \times l}, V_p^{\top} V_p = \mathbf{I}_l,$ (11)

where K_p is one separate kernel and V_p represents the *p*-th dustering matrix based on X_p .

In fact, to reduce the complexity of our model, we 416 assume that the physical location affects the clustering per-417 formance with the same degree and the number of clusters 418 is the same as that in S-MKKM, i.e., l and α are the same 419 as used in Equation (4). The reason behind this assumption 420 is that most cities have the same functional regions, such 421 as the residential region and business region. Thus, it is 422 reasonable that we choose the same α and l in this practical 423 task. Besides, α and l are very stable due to the intrinsic 424 property of the urban statistical data, and we fixed them in 425 the experiments. The single view guidance matrix X_p^{sv} and 426 adaptive-weight matrix Z'_p can be constructed by the same strategy of building X^{mv}_p and Z_p . 427 428

Furthermore, for each region, its *k*-nearest spatial neigh-429 bors imply rich information that should be considered in 430 our model. Even though the regional physical topology is 431 already involved in multi-view and single-view learning 432 processes, the KNN is a more flexible method. After struc-433 turing X_n^{knn} which is an imputed matrix with the average 434 value of k-nearest neighbors, our optimization functions of 435 single view and KNN are expressed as: 436

$$\min_{W \ge 0, H_p \ge 0} \ \mathcal{S} = \sum_{p=1}^d ||\bar{Y}_p \odot Z'_p \odot (X_p^{sv} - WH_p)||_F^2, \quad (12)$$

$$\min_{W \ge 0, H_p \ge 0} \mathcal{K} = \sum_{p=1}^{a} ||\bar{Y_p} \odot (X_p^{knn} - WH_p)||_F^2, \quad (13)$$

Taking all the above techniques into consideration, our437final jointly loss function is shown as follows:438

$$\min_{\geq 0, H_p \geq 0} \mathcal{J} = \mathcal{N} + \lambda_1 \mathcal{M} + \lambda_2 \mathcal{S} + \lambda_3 \mathcal{K}, \qquad (14)$$

where λ_2 and λ_3 are the regularization parameters to control the learning rate of X_p^{sv} and X_p^{knn} , respectively.

After solving Equation 14, the learned matrices W and441 H_p can be used to do the missing data imputation. The filled442data are estimated by:443

$$\hat{X}_p = Y_p \odot X_p + \bar{Y}_p \odot (WH_p) \tag{15}$$

4.5 Learning Process

W

As Equation (14) is a non-convex problem, we use the multiplicative update strategy [44] to discover the local optimization. Additionally, to generate the complete kernels, we need to initialize the missing values in data matrices $\{X_1...X_d\}$, shown in the Section 5.7. The update rules for W and H_p are presented in Equation (16) - (17).

Theorem 1. \mathcal{J} is non-increasing under the following update rules in Equation 16-17 by optimizing W and H_p alternatively:

$$W = W \odot$$

$$\sum_{p=1}^{d} (Y_p \odot X_p + \bar{Y_p} \odot (\lambda_1 Z_p \odot X_p^{mv} + \lambda_2 Z_p' \odot X_p^{sv} + \lambda_3 X_p^{knn})) H_p^\top$$

$$\sum_{p=1}^{d} ((Y_p + \bar{Y_p} \odot (\lambda_1 Z_p + \lambda_2 Z_p' + \lambda_3 \mathbf{1})) \odot (W^\top H_p) H_p^\top)$$
(16)

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$$H_{p} = H_{p} \odot$$

$$\frac{W(Y_{p} \odot X_{p} + \bar{Y_{p}} \odot (\lambda_{1}Z_{p} \odot X_{p}^{mv} + \lambda_{2}Z_{p}^{'} \odot X_{p}^{sv} + \lambda_{3}X_{p}^{knn}))}{W(Y_{p} + \bar{Y_{p}} \odot (\lambda_{1}Z_{p} + \lambda_{2}Z_{p}^{'} + \lambda_{3}\mathbf{1})) \odot (W^{\top}H_{p})}$$
(17)

The prove of Theorem 1 is given in Section 4.6.1. The 453 above two multiplicative update rules guarantee to be non-454 negative if the initialization is positive. Without this con-455 straint, the matrices W and H_p could be negative, thus 456 the imputation results could be negative too, which is a 457 contradiction to the facts. We now derive the update rule 458 of W as an example, other variables can be solved with a 459 similar process. The objective of \mathcal{J} could be rewritten as 460 follows: 461

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$$\mathcal{J}=L_0+L_1+L_2+L_3$$
 , where:

$$L_{0} = \sum_{p=1}^{d} ||Y_{p} \odot (X_{p} - WH_{p})||_{F}^{2},$$

$$L_{1} = \lambda_{1} \sum_{p=1}^{d} ||\bar{Y}_{p} \odot Z_{p} \odot (X_{p}^{mv} - WH_{p})||_{F}^{2},$$

$$L_{2} = \lambda_{2} \sum_{p=1}^{d} ||\bar{Y}_{p} \odot Z_{p}^{'} \odot (X_{p}^{sv} - WH_{p})||_{F}^{2},$$

$$L_{3} = \lambda_{3} \sum_{p=1}^{d} ||\bar{Y}_{p} \odot (X_{p}^{knn} - WH_{p})||_{F}^{2}$$
(18)

We provide the derivative of L_0 respect to W as an 463 example, the other components can be derived in the same way. L_0 could also be rewritten as follows: 465

$$L_0 = \langle Y_p \odot (X_p - WH_p), Y_p \odot (X_p - WH_p) \rangle$$
(19)

where \langle , \rangle presents the inner product of matrix. Then:

$$dL_{0}(W) = -2\sum_{p=1}^{d} \langle dWH_{p}, Y_{p} \odot (X_{p} - WH_{p}) \rangle$$

$$= -2\sum_{p=1}^{d} \langle dW, Y_{p} \odot (X_{p} - WH_{p})H_{p}^{\top} \rangle \qquad (20)$$

$$\Rightarrow \frac{\partial L_{0}}{\partial W} = -2\sum_{p=1}^{d} Y_{p} \odot (X_{p} - WH_{p})H_{p}^{\top}$$

Analogously, we can get:

$$\frac{\partial L_1}{\partial W} = -2\lambda_1 \sum_{p=1}^d \bar{Y_p} \odot Z_p \odot (X_p^{mv} - WH_p) H_p^{\top} \qquad (21)$$

$$\frac{\partial L_2}{\partial W} = -2\lambda_2 \sum_{p=1}^{d} \bar{Y_p} \odot Z'_p \odot (X_p^{sv} - WH_p) H_p^{\top} \qquad (22)$$

$$\frac{\partial L_3}{\partial W} = -2\lambda_3 \sum_{p=1}^d \bar{Y_p} \odot (X_p^{knn} - WH_p) H_p^\top$$
(23)

As discussed in [44], the traditional gradient descent 468
method is expressed as:
$$W_t = W_t - \gamma g(W_t) = W_t - 469$$

 $\gamma(P_{item} + N_{item})$, where P_{item} and N_{item} denote all positive 470
and negative items in $g(W_t)$, respectively (e.g., $P_{item} = 471$
 $\sum_{p=1}^{d} ((Y_p + \bar{Y_p} \odot (\lambda_1 Z_p + \lambda_2 Z'_p + \lambda_3 \mathbf{1})) \odot (W^{\top} H_p) H_p^{\top}))$. We 472
can set the step γ to: 473

$$\gamma = \frac{W_t}{P_{item}} \tag{24}$$

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then, we got the update rule of W as shown in Equation 16. 474 Algorithm 1 summarizes our learning and estimation 475 process of SMV-NMF.

Algorithm 1: SMV-NMF

	Input: original data $\{X_p\}$; graph Laplacian matrix
	L.
	Output: complete data $\{\hat{X}_p\}$.
1	Impute X_p by KNN for an initialization.
2	Initialize W and H_p by decomposing X_p .
3	Construct X_n^{mv} , X_n^{sv} and X_n^{knn} by S-MKKM,
	S-KKM, and KNN respectively.
4	for $Epoch = 1$ to T do
5	$ \mathbf{if} \mathcal{J}_t - \mathcal{J}_{t+1} / \mathcal{J}_t \geq \varepsilon$ then
6	update W By Equation (16)
7	update H By Equation (17)
8	else
9	Break
10	Return \hat{X} By Equation (15)

4.6 Time complexity and convergence

We discuss the time complexity and convergence of SMV-478 NMF here. The time complexity of guidance matrices X_n^{mv} 479 and X_p^{sv} is mainly affected by MKKM. Even though MKKM 480 has a high computational complexity $(O(n^3))$, it is not in-481 volved in updating loop of variables (W and H_p). Equation 482 (16) and Equation (17) present that the time complexity 483 of our final function is governed by matrix multiplication 484 operations in each iteration. Therefore, the time complexity 485 per iteration is dominated by $O(nk^2)$. Due to the pursuing 486 of pinpoint accuracy, we sacrifice efficiency to some degree 487 in this real-world problem. In terms of convergence, we give 488 the strict convergence proof of W because other variables 489 can similarly be proofed. 490

4.6.1 Proof of Theorem 1

To prove **Theorem 1**, we need to find an auxiliary function 492 for SMV-NMF objective function as expressed in Equation 493 (14).494

Definition 1. G(h, h') is an auxiliary function for our final 495 function $\mathcal{J}(h)$ if the following conditions are satisfied: 496

$$G(h',h) \ge \mathcal{J}(h)$$
 and $G(h,h) = \mathcal{J}(h)$. (25)

Lemma 1 If G is an auxiliary function, then \mathcal{J} is non-497 *increasing under the update:* 498

$$h^{t+1} = \arg\min_{h} G\left(h, h^{t}\right), \tag{26}$$

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consequently, we have: 499

$$\mathcal{J}\left(h^{t+1}\right) \le G\left(h^{t+1}, h^{t}\right) \le G\left(h^{t}, h^{t}\right) = \mathcal{J}\left(h^{t}\right).$$
(27)

The proof of Lemma 1 is given by [44]. Lemma 1 illus-500 trates that $\mathcal{J}(h^{t+1}) \leq \mathcal{J}(h^t)$ when exits $\mathcal{Q}(h, h^t)$. 501

Lemma 2. If $K(h^t)$ is a diagonal matrix under the following 502 definition, 503

$$K(h^t) = diag(W diag(v) W^T h./h),$$
(28)

where v is a column vector of $V = Y_p + \overline{Y}_p$. 504 $(\lambda_1 Z_p + \lambda_2 Z'_p + \lambda_3 \mathbf{1})$ then, 505

$$G(h, h^{t}) = J(h^{t}) + (h - h^{t})^{T} \nabla \mathcal{J}(h^{t}) + \frac{1}{2} (h - h^{t})^{T} K(h^{t}) (h - h^{t}),$$
(29)

is an auxiliary function for $\mathcal{J}(h)$. 506

Proof: Since $G(h, h) = \mathcal{J}(h)$ is obvious, we need only 507 show that $G(h, h^t) \geq \mathcal{J}(h)$. To do this, we compare 508

$$\mathcal{J}(h) = \mathcal{J}(h^{t}) + (h - h^{t})^{T} \nabla \mathcal{J}(h^{t}) + \frac{1}{2} (h - h^{t})^{T} \left(W diag(v) W^{T} \right) (h - h^{t})$$
(30)

with Equation (29) to find that $G(h, h^t) \geq \mathcal{J}(h)$ is equivalent to 510

$$0 \le \left(h - h^t\right)^T \left[K\left(h^t\right) - Wdiag(v)W^T\right]\left(h - h^t\right) \quad (31)$$

The next step is to prove $[K(h^t) - W \operatorname{diag}(v)W^T]$ 511 positive semi-definite. Let $Q = W diag(v) W^T$ 512 is then $|K(h^t) - W \operatorname{diag}(v) W^T|$ can be expressed as 513 [diag(Qh./h) - Q]. As the Lemma 1 provided in [45], if 514 Q is a symmetric non-negative matrix and h be a positive 515 vector, then the matrix $\hat{Q} = diag(Qh./h) - Q \succeq 0$. 516

Replacing $G(h, h^t)$ in Equation (26) by Equation (29) 517 results in the update rule: 518

$$h^{t+1} = h^t - K \left(h^t\right)^{-1} \nabla \mathcal{J} \left(h^t\right)$$
(32)

Since Equation (29) is an auxiliary function, \mathcal{J} is non-519 increasing under this update rule, according to Lemma 520 1. Writing the components of this equation explicitly, we 52 obtain 522

$$h_{a}^{t+1} = h_{a}^{t} \frac{(Wx)_{a}}{(W(v \odot W^{T}h))_{a}}$$
(33)

x is the column vector of 523 where X $(Y \odot X + \overline{Y} \odot (\lambda_1 Z \odot X^{mv} + \lambda_2 Z' \odot X^{sv} + \lambda_3 X^{knn})).$ 524

By reversing the roles of W and H in Lemma 1 and 525 **Lemma 2**, \mathcal{J} can similarly be shown to be nonincreasing 526 under the update rules for W. 527

EXPERIMENTS 5 528

In this chapter, we have conducted comprehensive experiments to demonstrate the effectiveness of our method. The 530 source code has been released at https://github.com/SMV-531 532 NMF.

5.1 Datasets

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We use eight real-world urban statistical datasets collected 534 from the Australian Bureau of Statistics 2017 (ABS) and the 535 New Zealand Stats 2018 (NZS), i.e., Sydney, Melbourne, 536 Brisbane, Perth, SYD-large and MEL-large are collected 537 from the ABS, and Auckland and Northland are collected 538 from NZS. -large datasets contains much more fine-grained 539 regions. In ABS datasets, each one contains four views, 540 i.e., Economy, Family, Income, and Population; the size 541 (number of fine-grained areas) of the first six datasets are 542 174, 284, 220, 130, 2230, 1985 respectively, and the numbers 543 of attributes of the four views are 43, 44, 50, 97. The last 544 two datasets are provided by NZS, which includes 563 areas 545 with eleven views, and the average number of the view's 546 dimension is six. Notably, due to the fact that the NZS 547 geography map is inaccessible to us, we tested our method 548 without any geography guidance on these datasets. And 549 for the ABS data, the designation of regions is based on 550 the Statistical Geography Standard⁵ for the best practical 551 value. The scales of different views are normalized into 552 the same range [0,10] so that we can evaluate the results 553 together. Besides, to guarantee the diversity of testing, for 554 each missing ratio, we randomly select the test columns and 555 repeat the experiment 20 times and report average results. 556

Baselines & Measures 5.2

5.2.1 Baselines

We compare the proposed method SMV-NMF with the following 13 baselines. All parameters of the proposed method and baselines are optimized by the grid search method.

sKNN: A classical method that uses the average values 562 of its k nearest spatial neighbors as an estimate (k=5).

MKKMIK^a: A MKKM based method to handle the incomplete views [38]. We modified it to adapt to the spatially related data, then interpolated a missing value by its knearest spatial neighbors (k=5);

MKKMIK^b: Similar to MKKMIK^a but utilize the mean value of each cluster to fill the missing data.

NMF: Fill the missing data by NMF.

IDW: A global spatial learning method compared in many works [16], [21].

UCF: The Local spatial learning method based on collaborative filtering [8], [20].

IDW+UCF: Fill missing entries by the average result of IDW and UCF.

MVL-IV: A state-of-the-art multi-view learning method based on matrix co-factorization, which learns a same coefficient matrix to connect multiple views [34].

ST-MVL: A state-of-the-art method to impute spatiotemporal missing data [8]. We only use its spatial part due to the problem of missing temporal information.

SMV-MF: We remove the non-negativity constraint in SMV-NMF to test the effects of this constraint.

MV-NMF^a: Remove the graph Laplacian dynamics strategy in SMV-NMF when building the X_p^{mv} and X_p^{sv} ;

MV-NMF^b: Remove the KNN guidance in SMV-NMF.

MV-NMF^c: Remove all the geography guidance that can 588 be used in the NZS datasets. 589

5. https://www.abs.gov.au/geography

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Fig. 5: Average RMSE with the variation of missing ratios.

Measures. We utilized the most widely used evaluation
 metrics in this chapter, namely Mean Relative Error (MRE)
 and Root Mean Square Error (RMSE).

$$MRE = \frac{\sum_{i=1}^{Q} |u_i - \hat{u}_i|}{\sum_{i=1}^{Q} u_i}, \quad RMSE = \sqrt{\frac{\sum_{i=1}^{Q} (u_i - \hat{u}_i)^2}{Q}},$$

where \hat{u}_i is a prediction for missing value, and u_i is the ground truth; *Q* is the number of prediction values.

595 5.3 Performance Results and Analysis

The first set of experiments is designed to assess per-596 formance on each dataset. We pick up 1/3 of statistical 597 fields (properties) in each urban dataset randomly as the 598 validation set, and the other set as the test set. In the test 599 set, we randomly select missing ratios from 10% to 70% to 600 evaluate the imputation accuracy. As mentioned in Section 601 5.1, NZS data do not provide geography knowledge that 602 some methods and baselines cannot be used. 603

Because of the page width limitation, we partition our 604 main results into two tables, i.e., Table 2 and Table 3. 605 These two tables report the average errors of all missing 606 ratios across different compared algorithms. In this test, it 607 is apparent that the series of proposed approaches (SMV-608 MF, MV-NMF^{*a*}, MV-NMF^{*b*}, MV-NMF^{*c*}, SMV-NMF) achieve 609 the better results on eight real-world datasets. The SMV-610 NMF method which corporates both geography and latent 611 spatial guidances that performs almost most through all 612 experiments. MVL-IV yields better results than ST-MVL, 613 MKKMIK^a, IDW+UCF, and NMF becuase it considers the 614 multi-view problem. Compared with the best baseline MVL-615 IV, our method learned the similarities from latent spaces 616 instead of clustering in the original data; second, we have 617 added prior knowledge (adaptive weights) to each missing 618 entries and observed entries. Such prior knowledge also 619 considered the spatial correlation which is significant for 620 the spatially correlated data [2], [21]. Although ST-MVL 621 is a great method of filling spatio-temporal missing data, 622 it would not perform well when the missing temporal 623 information challenge appears. 624

To represent the error change with the varying missing ratios, we draw the top eight methods with different missing ratios on the Sydney and Melbourne datasets, which is shown in Fig. 5. The results drawn in Fig. 5 demonstrate the results of Table 2-3 and the discussions aforementioned. For the methods NMF, MV-NMF^a, they are sensitive to the missing ratios, which could get good results under the lower level missing ratios, but performs worse when the missing ratio increases. To evaluate the improvement of our model, we also report the T-test results (p-value 1) compared with the best baseline MVL-IV, the result is significant at p < 0.05. Our methods, (SMV-MF, MV-NMF^a, MV-NMF^b, SMV-NMF) have significant improvements compared with current baselines.

Ablation Study. To analyses the contribution of each 639 component of the final method SMV-NMF, we analyze the 640 ablation study here. All the results are shown in Tables 2 641 and 3. Table 4 illustrates the different strategies used in pro-642 posed models. n-constraint represents the non-negativity 643 constraint; Laplacian means whether the model considers 644 the graph Laplacian dynamics when building X_n^{mv} and 645 X_p^{sv} ; knn indicates the KNN guidance is used or not. 646

As the results shown in Tables 2 and 3, we can see that 647 without the non-negativity constraint, SMV-MF performs 648 worse than SMV-NMF, which demonstrates the effective-649 ness of this constraint. Two models (MV-NMF^a and MV-650 NMF^b) will perform worse when casting off the graph 651 Laplacian dynamics strategy. If we only consider the non-652 negativity constraint but without any geography guidance, 653 our model, MV-NMF^c cannot achieve a good result. But it is 654 still better than other baselines. We have provided the T-test 655 (p-value 2) between the best model MV-NMF and the second 656 best MV-NMF^b to present the improvements, the result is 657 significant at p < 0.05. 658

Overall, SMV-NMF outperforms the other baselines because it integrates both multi-view and spatial problems to address the specified missing data imputation task. MV-NMF^{*a*} MV-NMF^{*b*} and MV-NMF^{*c*} remove a part of the spatial guidance which results in slightly worse performances than SMV-NMF.

5.4 Experiments on Generalization Ability

In this section, we try to explore the generalization ability of our method. The test process is that the dataset Sydney is chosen as the validation set and two urban datasets (Melbourne and Brisbane) are chosenas the test sets. Fig. 6 reports the performances among eight outstanding approaches. We clearly see that the SMV-NMF achieves the best performance.

Our method represents strong generalization ability 673 which can transfer the constructed model from one urban 674 dataset to another. This is because there are high correlations 675 among cities. For example, the number of functional regions 676 of each city is mostly the same, resulting in the same 677 amount of clusters. The gap between SMV-NMF and MVL-678 IV narrows as the missing ratio increases, but the former 679 is more robust than the latter because SMV-NMF achieves 680 the best results across all missing ratios. Table 5 reveals the 681 average errors using two evaluation metrics. The generality 682 test demonstrates that our model SMV-NMF is a universal 683 model that performs well crossing different urban statistical 684 datasets. 685

5.5 View Correlation Analysis

To evaluate the correlations between views, we represent the view weight changes with varying missing ratios. Fig. 7 shows the results on the Sydney dataset. As we can see that the view of Economy occupies the highest priority in

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Mathada	Sydney		Melbourne		Brisbane		Perth	
Methous	MRE	RMSE	MRE	RMSE	MRE	RMSE	MRE	RMSE
sKNN	0.332 ± 0.011	1.530 ± 0.097	0.310 ± 0.014	1.372 ± 0.079	0.355 ± 0.006	1.518 ± 0.065	0.381 ± 0.010	1.575 ± 0.083
$MKKMIK^{b}$	0.329 ± 0.015	1.550 ± 0.089	0.346 ± 0.011	1.462 ± 0.076	0.377 ± 0.009	1.593 ± 0.070	0.398 ± 0.018	1.699 ± 0.064
IDW	0.332 ± 0.009	1.518 ± 0.077	0.318 ± 0.010	1.318 ± 0.089	0.351 ± 0.008	1.466 ± 0.090	0.372 ± 0.009	1.557 ± 0.081
UCF	0.356 ± 0.008	1.663 ± 0.083	0.338 ± 0.009	1.463 ± 0.079	0.362 ± 0.007	1.592 ± 0.072	0.375 ± 0.008	1.655 ± 0.080
IDW+UCF	0.330 ± 0.007	1.460 ± 0.056	0.314 ± 0.006	1.304 ± 0.064	0.340 ± 0.008	1.397 ± 0.070	0.361 ± 0.007	1.495 ± 0.069
$MKKMIK^{a}$	0.308 ± 0.011	1.439 ± 0.105	0.288 ± 0.009	1.226 ± 0.092	0.316 ± 0.010	1.347 ± 0.097	0.354 ± 0.008	1.506 ± 0.083
NMF	0.221 ± 0.014	1.384 ± 0.111	0.199 ± 0.009	1.155 ± 0.093	0.225 ± 0.010	1.304 ± 0.108	0.248 ± 0.013	1.288 ± 0.127
ST-MVL	0.294 ± 0.007	1.313 ± 0.069	0.283 ± 0.007	1.179 ± 0.077	0.311 ± 0.006	1.295 ± 0.067	0.332 ± 0.006	1.394 ± 0.077
MVL-IV	0.198 ± 0.005	1.063 ± 0.032	0.174 ± 0.004	0.818 ± 0.029	0.197 ± 0.004	0.969 ± 0.041	0.225 ± 0.005	1.067 ± 0.044
SMV-MF	0.191 ± 0.004	0.960 ± 0.031	0.181 ± 0.004	0.800 ± 0.027	0.183 ± 0.005	0.854 ± 0.021	0.219 ± 0.004	1.002 ± 0.029
$MV-NMF^{a}$	0.185 ± 0.005	0.925 ± 0.020	0.177 ± 0.004	0.815 ± 0.022	0.163 ± 0.003	0.757 ± 0.015	0.223 ± 0.004	0.976 ± 0.022
$MV-NMF^b$	0.180 ± 0.003	0.927 ± 0.013	0.173 ± 0.002	0.804 ± 0.015	0.164 ± 0.003	0.770 ± 0.014	0.217 ± 0.004	0.972 ± 0.021
$MV-NMF^{c}$	0.195 ± 0.005	0.957 ± 0.033	0.182 ± 0.004	0.853 ± 0.030	0.190 ± 0.005	0.860 ± 0.035	0.228 ± 0.005	1.064 ± 0.042
MV-NMF	$\textbf{0.175} \pm \textbf{0.002}$	$\textbf{0.901} \pm \textbf{0.012}$	$\textbf{0.168} \pm \textbf{0.002}$	$\textbf{0.747} \pm \textbf{0.011}$	0.157 ± 0.002	$\textbf{0.705} \pm \textbf{0.009}$	$\textbf{0.208} \pm \textbf{0.003}$	$\textbf{0.933} \pm \textbf{0.014}$
<i>p</i> -value 1	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01
<i>p</i> -value 2	= 0.14	< 0.01	= 0.02	< 0.01	< 0.01	< 0.01	< 0.02	< 0.03

TABLE 2: The average MRE, RMSE, std and p-value on real-world urban statistical datasets (Part I). Best results are bold.

Mathada	SYD-large		MEL-large		Auckland		Northland	
Wethous	MRE	RMSE	MRE	RMSE	MRE	RMSE	MRE	RMSE
sKNN	0.297 ± 0.010	1.256 ± 0.088	0.310 ± 0.012	1.313 ± 0.070	-	-	-	-
$MKKMIK^{b}$	0.348 ± 0.013	1.611 ± 0.094	0.306 ± 0.011	1.456 ± 0.068	0.527 ± 0.027	2.139 ± 0.156	0.570 ± 0.034	2.575 ± 0.201
IDW	0.327 ± 0.008	1.499 ± 0.065	0.308 ± 0.009	1.258 ± 0.072	-	-	-	-
UCF	0.332 ± 0.009	1.423 ± 0.068	0.332 ± 0.009	1.509 ± 0.070	-	-	-	_
IDW+UCF	0.304 ± 0.006	1.223 ± 0.047	0.297 ± 0.007	1.211 ± 0.055	-	-	-	_
$MKKMIK^{a}$	0.291 ± 0.012	1.288 ± 0.080	0.301 ± 0.014	1.230 ± 0.101	0.496 ± 0.022	1.957 ± 0.123	0.512 ± 0.028	2.200 ± 0.104
NMF	0.238 ± 0.009	1.199 ± 0.092	0.203 ± 0.011	1.066 ± 0.073	0.406 ± 0.017	1.580 ± 0.092	0.444 ± 0.016	1.787 ± 0.099
ST-MVL	0.294 ± 0.006	1.077 ± 0.077	0.282 ± 0.008	1.145 ± 0.071	-	-	-	-
MVL-IV	0.179 ± 0.004	0.895 ± 0.059	0.184 ± 0.003	0.922 ± 0.046	0.327 ± 0.012	1.226 ± 0.066	$\textbf{0.322} \pm \textbf{0.010}$	1.467 ± 0.039
SMV-MF	0.177 ± 0.003	0.835 ± 0.024	0.192 ± 0.004	0.901 ± 0.031	-	-	-	-
$MV-NMF^{a}$	0.171 ± 0.005	0.822 ± 0.017	0.185 ± 0.003	0.861 ± 0.020	-	-	-	_
$MV-NMF^b$	0.168 ± 0.002	0.804 ± 0.014	0.176 ± 0.004	0.812 ± 0.017	-	-	-	_
$MV-NMF^{c}$	0.182 ± 0.005	0.960 ± 0.034	0.193 ± 0.004	0.915 ± 0.035	$\textbf{0.317} \pm \textbf{0.009}$	$\textbf{1.208} \pm \textbf{0.061}$	0.341 ± 0.009	$\textbf{1.405} \pm \textbf{0.032}$
SMV-NMF	$\textbf{0.166} \pm \textbf{0.001}$	$\textbf{0.774} \pm \textbf{0.007}$	$\textbf{0.169} \pm \textbf{0.002}$	$\textbf{0.791} \pm \textbf{0.008}$	-	-	-	-
p-value 1	< 0.01	< 0.01	< 0.01	< 0.01	=0.09	= 0.35	< 0.01	< 0.01
p-value 2	= 0.34	< 0.05	< 0.04	< 0.03	-	-	-	-

TABLE 3: The average MRE, RMSE, std and p-value on real-world urban statistical datasets (Part II). Best results are bold.

TABLE 4:	Ablation	Studies.	The	strategies	used	in	different
models.							

n-constraint	Laplacian	knn	Method
\checkmark		\checkmark	MV-NMF ^a
\checkmark	\checkmark		$MV-NMF^b$
\checkmark			$MV-NMF^{c}$
	\checkmark	\checkmark	SMV-MF
\checkmark	\checkmark	\checkmark	SMV-NMF



Fig. 6: The average RMSE in generalization ability tests.

the similarity learning process when the missing ratio is below (or equal to) 50%. When data is relatively adequate,

Mathada	Dataset N	ſelbourne	Dataset Brisbane		
Methous	MRE	RMSE	MRE	RMSE	
UCF	0.331 ± 0.009	1.405 ± 0.096	0.368 ± 0.008	1.560 ± 0.089	
IDW	0.333 ± 0.010	1.339 ± 0.070	0.369 ± 0.006	1.496 ± 0.071	
IDW+UCF	0.320 ± 0.007	1.306 ± 0.047	0.351 ± 0.005	1.455 ± 0.072	
$MKKMIK^{a}$	0.282 ± 0.010	1.201 ± 0.103	0.313 ± 0.009	1.302 ± 0.086	
ST-MVL	0.279 ± 0.006	1.139 ± 0.077	0.312 ± 0.006	1.269 ± 0.038	
NMF	0.183 ± 0.017	0.955 ± 0.126	0.199 ± 0.015	0.989 ± 0.093	
MVL-IV	0.152 ± 0.003	0.787 ± 0.022	0.163 ± 0.004	0.808 ± 0.029	
SMV-NMF	$\textbf{0.148} \pm \textbf{0.002}$	$\textbf{0.720} \pm \textbf{0.006}$	$\textbf{0.149} \pm \textbf{0.001}$	$\textbf{0.671} \pm \textbf{0.010}$	

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TABLE 5: Generalizability test. We report the average MRE and RMSE of all missing ratios and best results are bold.

the attributes of economy are the most important factor that influences the imputation method. With increasing missing ratio, the weight of Economy view decreases significantly because the data from other views are more considered to utilize the observed data comprehensively.

5.6 The Sensitivity of Parameters

This section evaluates the performances of SMV-NMF by varying the critical parameters (k, λ_1 , λ_2 , and λ_3). We here 700

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Fig. 7: View correlation analysis on the Sydney dataset.



Fig. 8: Effect of Parameters.

show the experimental results for the Sydney validation
dataset. We discuss them separately but pick them up by
the grid search method because four parameters have high
dimensional correlations that are hard to visualize. Our
illustration approach that discusses parameters separately
has been widely used in many other research papers [25],
[43].

Fig. 8 (a) shows the different performances with a vary-708 ing setting for k. When we increase k from 5 to 15, the 709 results improve significantly. However, the performance 710 tends to stay stable at $15 \le k \le 35$. In particular, SMV-711 NMF achieves the best result when k = 30, while it can 712 get good performance if the k is set between 15 and 35. 713 This indicates that a low-rank latent space representation 714 715 can already capture the attributes of the urban statistical data. 716

Fig. 8 (b) reveals the effect of varying λ_1 , λ_2 , and λ_3 . These three parameters determine the strength of the three guidance matrices X^{mv} , X^{sv} , and X^{knn} , respectively. $\lambda_1=2^{-7}$, $\lambda_2=2^{-8}$ and $\lambda_3=2^{-6}$ yield the best results for SMV-NMF. We observe that the performance is stable when these three parameters are ranged between 2^{-8} and 2^{-6} .

In summary, both parameters used in this chapter bring
benefits to the improvement of our models. Furthermore,
our model is stable and easy fine-tuning because it is insensitive to these parameters.

727 5.7 Initialization and Convergence

To get the complete kernels, we first impute the missing datafor each view by an efficient method, such as KNN and MF.



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dataset.

Fig. 9: Convergence rate.

TABLE 6: Effects of different initialization methods.

	Zero-init	Random-init	Mean-init	KNN-init
RMSE	1.173	1.134	0.949	0.908

The effects of different initializations are reported in Table 730 6. Based on the results, we easily find that the initialization 731 method KNN could achieve the great performance for SMV-NMF. Accordingly, we choose the KNN method for a good 733 balance between time-consuming and accuracy. 734

Figs. 9 (a) and (b) show the convergence trends of iter-
ative model SMV-NMF on both the Melbourne and Perth
datasets. It illustrates that our algorithm can converge into
a local solution in terms of the objective value in a small
number of iterations.735736737

6 CONCLUSION

Due to some inevitable issues, urban statistical data usually 741 suffer from the missing data problem. To overcome it, we 742 propose a missing data imputation model for multi-view 743 urban statistical data via the spatial correlation learning, 744 which called SMV-NMF in this paper. To handle the multi-745 view problem, we develop an improved spatial multi-kernel 746 method to guide the imputation process based on the NMF 747 strategy. Furthermore, the spatial correlations among differ-748 ent regions are taken into consideration from two aspects. 749 First, the latent similarities are discovered by S-MKKN and 750 S-KKM based on the idea of finding functional regions, and 751 secondly, KNN is used for capturing the information of real 752 geographical positions. We conduct intensive experiments 753 on eight real-world datasets to compare the performance 754 of our model and other state-of-the-art approaches. The 755 results not only show that our approach outperforms all 756 other methods, but also represent strong generalizabilities 757 crossing different urban datasets. 758

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