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# Error-Related Potential-Based Shared Autonomy via Deep Recurrent Reinforcement Learning

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 *Abstract*—*Objective.* Error-related potential (ErrP)-based brain-computer interfaces (BCIs) have received a considerable amount of attention in the human-robot interaction community. In contrast to traditional BCI, which requires continuous and explicit commands from an operator, ErrP-based BCI leverages the ErrP, which is evoked when an operator observes unexpected behaviours from the robot counterpart. This paper proposes a novel shared autonomy model for ErrP-based human-robot inter- action. *Approach.* We incorporate ErrP information provided by a BCI as useful observations for an agent and formulate the shared autonomy problem as a partially observable Markov decision process (POMDP). A recurrent neural network-based actor-critic model is used to address the uncertainty in the ErrP signal. We evaluate the proposed framework in a simulated human-in-the- loop robot navigation task with both simulated users and real users. *Main results.* The results show that the proposed ErrP- based shared autonomy model enables an autonomous robot to complete navigation tasks more efficiently. In a simulation with 70% ErrP accuracy, agents completed the task 14.1% faster than in the no ErrP condition, while with real users, agents completed the navigation task 14.9% faster. *Significance.* The evaluation results confirmed that the shared autonomy via deep recurrent 23 reinforcement learning is an effective way to deal with uncertain 24 human feedback in a complex human-robot-interaction task.

#### <sup>25</sup> I. INTRODUCTION

 Error-related potential (ErrP)-based brain-computer inter- faces (BCIs) have been widely used in human-robot inter-28 actions in recent works  $[1, 2]$  $[1, 2]$  $[1, 2]$ . The ErrP is an event-related potential (ERP) that are involuntarily evoked when a human perceives unexpected errors in an environment [\[3,](#page-11-2) [4\]](#page-12-0). The ErrP 31 phenomenon was first reported in choice-reaction tasks [\[5\]](#page-12-1). After the participant was aware of an erroneous response made by herself, a negative potential approximately 80 ms and a sustained positivity in the time interval between 200 and 500 ms were observed  $\left[3, 6\right]$  $\left[3, 6\right]$  $\left[3, 6\right]$ . It was later found that ErrP was also evoked 250 ms after the user observed an unexpected event in the external environment [\[4\]](#page-12-0). Due to the nature of ErrP signals, this type of brain activity is particularly useful as supervision or feedback signals during human-robot interactions tasks. ErrP signals can enhance the scalability of a system in cases in which a user can assess a device's actions as correct or incorrect. The agent takes advantage of the implicit brain

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signals acquired from the human user when determining the 43 appropriate agent action. Thus, the human user does not need 44 to explicitly send action commands, significantly reducing the  $45$ burden on the human user  $[7, 8]$  $[7, 8]$  $[7, 8]$  46

The shared autonomy in human-robot interaction leverage 47 the strengths of both human and robots, where robots can no 48 longer act solitarily, but must share part of their autonomy 49 space with human. In most traditional shared control tasks, 50 the user needs to provide explicit input, such as keyboard or  $\frac{51}{10}$ mouse commands  $[9-11]$  $[9-11]$ , during interactions. BCI systems  $52$ offer new channels that allow shared autonomy by integrating 53 user intent directly according to the ongoing brain activity, 54 thus eliminating the need to exploit muscular control [\[12,](#page-12-7) <sup>55</sup> [13\]](#page-12-8). The use of shared-autonomy schemes may allow error- <sup>56</sup> related potentials to be used as complementary signals in BCI  $_{57}$ systems. Due to the natural uniqueness of ErrPs, ErrP-based 58 shared autonomy can leverage the advantages of human-robot <sub>59</sub> collaboration without interrupting the user's main workflow.  $60$ However, due to the uncertainty of EEG signals, a direct  $61$ mapping of ErrPs to robot actions is not sufficient for optimal  $\epsilon$ <sub>82</sub> behavior. For example, a misclassification of EEG signal will  $\epsilon$ <sub>63</sub> lead wrong robot action. On the other hand, to train a shared  $\overline{64}$ autonomy model via deep neural network need a large data set. 65 But real ErrPs data collections can be very time-consuming 66 [\[14\]](#page-12-9) and have other drawbacks, such as overfitting if there is  $67$ not enough data.

In this paper, we propose a shared autonomy framework that 69 incorporates ErrP-based BCI via deep recurrent reinforcement  $\frac{70}{20}$ learning. Considering the uncertainty of ErrP, we formulate  $71$ the shared autonomy as a Partially Observed Markov Deci-<br>  $72$ sion Process (POMDP). Unlike the Markov Decision Process 73 (MDP), where the agent decides actions based on the direct  $_{74}$ observation of the full underlying state, POMDP allows the <sup>75</sup> agent to make optimal decisions based on a history of partial  $\frac{76}{6}$ observations or uncertain inputs  $[15, 16]$  $[15, 16]$  $[15, 16]$ . We consider the  $77$ uncertainty of the ErrP signal similar to an agent's imperfect  $\frac{78}{6}$ sensing of the environment. A BCI module might incorrectly  $\frac{79}{2}$ infer the user's intention because of a noisy ErrP signal; 80 similarly, a robot might wrongly identify the direction of an  $81$ arrow sign due to the noisy image captured from an imperfect  $\frac{82}{2}$ camera module. In other words, observations of the actual 83 environmental state could differ and be represented using 84 probabilistic models  $[17, 18]$  $[17, 18]$  $[17, 18]$ . Thus in our experiment, instead  $85$ of real EEG data, we simulate ErrP as a binary input of 0 or  $86$ 1 and represent its uncertainty as a Bernoulli distribution with  $87$ a probability  $\overline{P}$  of observing the true state.

Similar with previous works  $[12, 19-21]$  $[12, 19-21]$  $[12, 19-21]$ , an agent accu- 89 mulatively changes the decision probability over time, in this 90

<span id="page-2-0"></span>



Figure 1: An overview of our method for ErrP-based real-time shared autonomy and deep reinforcement learning, where the user's ErrP and robot observation of the environment were concatenated as the neural network input(a). We evaluated our method in a navigation task with real human participants (b). The red arrow with an arrow indicates the agent, and the green dot indicates the target (c).

91 paper, we use recurrent neural networks (RNN) to approach the POMDP. The RNN is an approach that involves stacking the memory history and is robust to partial observations [\[22\]](#page-12-16). 94 To solve the neural network training issue with a large data set, we use binary value (0 or 1) to simulate the decoded results of the ErrP classifier, instead using real EEG data to train the 97 model. This simulation enables us to train our model without real users. Our approach builds upon the shared autonomy framework [\[9\]](#page-12-5) As shown in Figure [1,](#page-2-0) we apply our method in a navigation task. Our studies with both simulated users and real human participants suggest that ErrP-based shared autonomy can successfully improve task performance.

- <sup>103</sup> Our contributions in this work can be summarized as <sup>104</sup> follows:
- <sup>105</sup> A novel ErrP-based reinforcement learning for shared <sup>106</sup> autonomy.
- <sup>107</sup> Demonstration the feasibility of the proposed shared <sup>108</sup> control paradigm with simulated ErrP.
- <sup>109</sup> Evaluation the ErrP-based shared autonomy with real <sup>110</sup> human participants in a navigation task with a pretrained 111 shared autonomy model.
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# 112 **II. RELATED WORKS**

# <sup>113</sup> *A. ErrP-based BCI for Human-Robot Interaction*

<sup>114</sup> Recently, the ErrP-based BCI has been widely used in <sup>115</sup> Human-Robot Interaction tasks[\[1,](#page-11-0) [23,](#page-12-17) [24\]](#page-12-18). Salazar et al. [\[1\]](#page-11-0) <sup>116</sup> proposed a closed-loop system that used the ErrP as an implicit 2

input to guide a robotic arm in a binary bin-sorting task. Kim 117 et al.  $[2]$  used the ErrP as an implicit reward of a robot to learn  $_{118}$ the mapping between human gestures and actions. Stefan K. 119 Ehrlich et al.  $[23]$  demonstrated the applicability of ErrPs as  $120$ human feedback signals for real-time mediating coadaptation 121 in human-robot interactions. Lopes-Dias et al.  $[24]$  showed the 122 feasibility of online asynchronous decoding of ErrP signals <sup>123</sup> and used the resulting decoded signals as feedback to guide  $a_{124}$ robotic arm towards a target after the robot was halted at an 125 unexpected moment. These works show that ErrPs can be used  $_{126}$ to decode human intention during human-robot interactions. 127

#### *B. Shared autonomy using BCI* 128

Shared control is a widely used technology in human-robot 129 interactions. BCI systems provide new channels that allow <sup>130</sup> shared control by integrating the user intent directly according 131 to the ongoing brain activity, eliminating the need to exploit 132 muscular control  $[12, 13, 25]$  $[12, 13, 25]$  $[12, 13, 25]$  $[12, 13, 25]$  $[12, 13, 25]$ . Various methods have been 133 used in BCI-based shared autonomy systems. Previous studies 134  $[26–28]$  $[26–28]$  have proposed flexible self-paced BCI systems that 135 switch between automatic and subject control methods. While 136 the switch model is efficient, only one control command can 137 be executed at a time. Thus, this kind of method cannot 138 take advantage of both human inputs and robot autonomy. <sup>139</sup> Some research [\[29,](#page-12-22) [30\]](#page-12-23) has used shared control in hierarchical 140 systems, with the brain signal providing high-level commands 141 via BCIs as the robot performs low-level tasks, such as <sup>142</sup> grasping, navigation, and manipulation. In  $[30]$ , steady-state 143 visually evoked potentials (SSVEPs) were used to select a <sup>144</sup> target while a robot arm performed a specific grasping action. <sup>145</sup> However, this shared control method subdivides tasks into <sup>146</sup> separate modules for the human user and the robot. Recently, 147 deep reinforcement learning (RL) frameworks incorporate user 148 inputs and agent observations to achieve shared autonomy <sup>149</sup> [\[9\]](#page-12-5). This shared control scheme opens the door to the use 150 of ErrP signals as an alternative or complementary signal in <sup>151</sup> BCI systems.

#### *C. ErrP-based Human-in-the-loop reinforcement learning* <sup>153</sup>

ErrP has been widely used in human-in-the-loop RL sys- <sup>154</sup> tems. In these systems, the ErrP signal is used as a positive <sup>155</sup> or negative reward to accelerate the training of autonomous 156 agents  $[31-33]$  $[31-33]$ . In  $[19]$ , ErrPs was used as negative reinforcers  $157$ of the actions to infer the optimal control strategies. In  $[20]$ , 158 ErrP was used to learn the reward function in an inverse 159 reinforcement learning control to the robot to avoid obstacles. 160 In  $[12]$ , inverse RL based on ErrP signals was used to infer  $_{161}$ the goal position in a virtual grid. In  $[31]$ , ErrP-based RL was 162 used to update the reward to determine a policy in a route 163 learning strategy. ErrP has also been used in RL to choose the <sup>164</sup> correct target among several possible targets. In [\[34\]](#page-13-1), ErrPs 165 served as the reward in a reinforcement learning approach to 166 train an intelligent neuroprosthesis controller. The objective <sup>167</sup> in this work was to improve the control policy. In  $[2]$ , ErrP 168 was used to train a robot to learn human gestures through 169 a reinforcement learning strategy based on the leap motion 170 and ErrP features. However, when the ErrP signal was used 171  as a reward, while the ErrPs accelerated learning, the signals operated independently of the system during testing [\[31](#page-12-24)[–33\]](#page-13-0). Unlike others works where human-in-the-loop reinforce- ment learning frameworks leverage human feedback to train autonomous agents that operate independently of the user at test time  $\left[31-33\right]$ , In our paper, We combine user input (ErrP) and robot observation as inputs of the deep model for mapping optimal actions. The shared autonomy will always need to leverage user input to accomplish the task both at training and test time.

#### <sup>182</sup> *D. Formulating Human-Robot Interaction as POMDP*

 A POMDP can handle sequential decisions with various uncertainties arising from human feedback errors and sensing noise. The POMDP formulates a problem in which the state measurements are partial observations in sequential decisions. Recently, the POMDP has emerged as a popular approach in human-robot collaboration tasks [\[35–](#page-13-2)[38\]](#page-13-3).

 In [\[35\]](#page-13-2), human-robot collaboration was formulated as a POMDP by characterizing the robot's information and hu-191 man's intention as the state space. In  $[36]$ , human-robot collab- oration was formulated as a POMDP to learn the human model via Bayesian nonparametric learning to determine the human state. Moreover, in [\[37\]](#page-13-5), the observation model, dynamic machine model, and human model were combined in one framework and formulated as a POMDP model for the human- in-the-loop system. In [\[38\]](#page-13-3), human-computer interactions were formulated as a consequence of a POMDP and used to model human perception during interactions. In summary, the POMDP does not assume that the system state is fully observable, and the POMDP's ability to represent uncertainties arising from different sources makes it a suitable model in human-robot collaboration applications. In our paper, ErrP uncertainty is represented by a Bernoulli distribution with a 205 probability  $\overline{P}$  of observing the truth. As a result, our system can be considered a partially observable Markov decision process with uncertain observations. The POMDP allows for optimal decision-making under uncertain input conditions.

<sup>210</sup> *A. Overview*

## <sup>209</sup> III. METHOD

 In this section, we first introduce background knowledge on the POMDP. We then introduce the ErrP-based shared framework, neural network architecture and reinforcement learning, task environment, and input feature to the neural <sup>215</sup> network.

#### <sup>216</sup> *B. POMDP background*

 A Markov decision process (MDP) assumes that an agent can fully observe an environment. Otherwise, the agent senses the environment with limited or uncertain observations. If the observations are uncertain, the state signal is no longer Markovian, violating a key assumption of most reinforcement learning techniques [\[39\]](#page-13-6). A POMDP allows for optimal de- cision making even when the agent's observation is partially [\[16\]](#page-12-11). A partially observable Markov decision process is a tuple

 $\langle S, A, \Omega, T, O, R \rangle$  in which S is a finite set of states, A is a 225 finite set of actions,  $\Omega$  is a finite set of observations, T is a 226 transition function defined as T:  $S \times A \times S \rightarrow [0, 1]$ , O is an 227 observation function defined as  $O: S \times A \times \Omega \rightarrow [0, 1]$ , and R 228 is a reward function defined as R:  $S \times A \times S \rightarrow R$ .

The discrete set of observations  $\Omega = \{o^1, \dots, o^M\}$ 230 represents the agent's observation, which depends on the <sup>231</sup> next state  $s'$  and is sometimes conditioned on its action a. 232 This set can be determined with the observation function 233 O:  $S \times A \times \Omega \rightarrow [0, 1]$ . The probability of observing o 234 in state s' after an action is  $O(s', a, o)$ . This requires that 235  $O(s', a, o) \ge 0$  and  $\sum_{o \in \Omega} O(s', a, o) = 1$ . In our paper, the 236 discrete partial observation is  $\Omega = \{0, 1\}$ , which represents 237 the decoded ErrP result. The probability follows the Bernoulli 238 distribution. If  $P = 0.7$ , the probability can be modelled 239 as follows:  $O(s', a, o^1) = 0.7, O(s', a, o^2) = 0.3,$  or 240  $O(s', a, o^2) = 0.7, O(s', a, o^1) = 0.3$ . In this case, the 241 agent has a 70% chance to observe the true environment state. 242 Thus, an agent with uncertain ErrP feedback conforms to 243 Partially Observable Markov Decision Processes.

#### *C. ErrP-based framework* <sup>245</sup>

The classification of ErrP signals collected from humans <sup>246</sup> is not perfect due to misclassification. ErrP uncertainty can <sup>247</sup> be regarded as an agent's imperfect sensing of the true state 248 of the environment. We use a deep reinforcement learning <sup>249</sup> agent that maps observations from sensors (including ErrP) 250 to actions. We incorporate the ErrP information provided by a 251 BCI as useful observations for the agent. Our method jointly 252 embeds the ErrP information  $e_t$  acquired from the user and the 253 agent's observations of the environment  $s_t$  by concatenating  $254$ the values.  $\frac{1}{2}$   $\frac{1}{255}$ 

 $\tilde{s}_t = \begin{bmatrix} e_t \\ e_t \end{bmatrix}$ st 1

# *D. Network architecture and reinforcement learning* <sup>256</sup>

Our network architecture builds on the one proposed by Sut- <sup>257</sup> ton et al.  $[40]$ . The actor consists of 64-bit gated recurrent units  $_{258}$ (GRUs) that use fully connected layers to process the input and <sup>259</sup> produce the output values of the hidden states,  $h_t^a$ . The action  $_{260}$ probabilities are produced by the final layers,  $z$ , via a bounded  $261$ softmax distribution:  $P(u) = (1 - \varepsilon)$ soft max $(z)_u + \varepsilon / |U|$ , 262 where  $\varepsilon/|U|$  lower-bounds the probability of any given action. 263 We anneal  $\varepsilon$  linearly from 0.5 to 0.05 across 5500 training 264 episodes and set it to 0 during the test. The critic is a <sup>265</sup> feedforward network with multiple ReLU layers and fully <sup>266</sup> connected layers.

We choose the widely used advantage actor-critic (A2C) 268 algorithm  $[41, 42]$  $[41, 42]$  $[41, 42]$  to stabilize the training by reducing the vari-<br>269 ance. We train the critic with this policy to estimate the Q value  $_{270}$ using TD( $\lambda$ ) [\[41\]](#page-13-8), which is adapted for use in deep neural networks. We train the actor with advantage function  $A(\tau^a, u^a) =$  272  $Q(\tau^a, u^a) - V(\tau^a)$ , where  $Q(\tau^a, u^a)$  is action value function 273 and  $V(\tau^a)$  is value function. The update direction is defined 274 by the gradient  $g = E_T \left[ \sum_{n=1}^{T-1} \right]$  $\sum_{t=0}^{T-1} \nabla_{\theta \pi} \log \pi (u_t | s_t) G_t \bigg]$ , where 275

<span id="page-4-0"></span>

Figure 2: The environment without obstacles (a) and obstacles (b).

  $G_t$  is empirical returns. At each time step, the policy architec- ture is fed the ErrP, agent's local observation and step number and is tasked with estimating the Q-value function and policy at each point.

#### <sup>280</sup> *E. Task statement*

 We test our method in two environments. As shown in Figure [2,](#page-4-0) the navigation environment is described by a grid map. The first environment is a grid map without obstacles, and the second environment is a grid map that includes several obstacles. The layout of the map and the positions of the obstacles were fixed during training and testing. The second environment simulates a real-world environment where an agent's observation is blocked by obstacles. The use of two environments demonstrates the generalizability of the proposed shared autonomy framework.

291 The size of the grid was  $11 \times 11$ . The locations of the robot and the target were simplified as grid coordinates. The horizons of the robot were limited to the four corners of its neighbourhood. The robot can move north, south, west, or east during each time step. The robot cannot move towards the barriers or out of the grid. The robot is surrounded by a  $297 \text{ } 1 \times 1$  horizon in which it can detect the target. The agent's task is to identify the goal location within the map. The agent has a limited sensing range that is assumed to be substantially <sub>300</sub> smaller than the size of the maze. The target will be detected 301 when the target is in the sensing range. The goal location and agent start position are randomized (spawned) in a constant static map in each episode during training and testing. After the goal is achieved, a new episode begins. To encourage short trajectories, each time step has a step cost (penalty) of 0.01. A typical sparse terminal reward (20) and the step cost are provided to encourage the agent to reach the target position in the minimal number of steps.

# <sup>309</sup> *F. Input features of the neural network*

310 The input features include ErrP feedback from the human user and the agent's observations of the environment. The agent's observations of whether the target is in its current position and four adjacent positions. The step number and most recent agent action are also included as features. All features are normalized by their maximum values. Information about the target position was not included in the input.

# *1)* Last action: The coupled action is a useful input feature 317 because the ErrP signal is cued by the agent's last action. 318

2) *Mark of visited grads:* For a stationary target, an optimal 319 search strategy is trivially represented by a path that attempts 320 to cover the entire environment without revisiting any location. 321 The marker was often used as a reward in learning a policy 322 to encourage the agent to explore unvisited locations  $[43, 44]$  $[43, 44]$  $[43, 44]$ . 323 However, the uncertainty of ErrP feedbacks could cause the 324 agent to make incorrect decision. In such case, revisiting an 325 explored location might allow a correction. Indeed, we found 326 that the use of the visited marker as a reward limited the 327 optimal policy and thus yielded slightly suboptimal policies. <sup>328</sup> We found that using visited marker as an input allows the 329 model to learn an optimal strategy. 330

3) ErrP information: To eliminate the gap between the 331 simulated EEG data and the real EEG data collected from 332 a human user, we simplified the EEG data as a binary 333 variable, which corresponds to the decoding output of the ErrP 334 classifier. During model training, we use the binary values 335 0 and 1 to simulate the output of the ErrP binary classifier. <sup>336</sup> To generate the ErrP values, we calculated the shortest path 337 towards the target position at each step. The shortest path  $[45]$  338 was computed according to the full map environment. This 339 approach follows a environment in which the human user has  $340$ a global view of the environment. If the current shortest path 341 is larger than the previous shortest path, we considered the <sup>342</sup> current step to be bad action and assigned an ErrP label of 1; <sup>343</sup> otherwise, we assigned an ErrP label of 0. <sup>344</sup>

#### IV. EXPERIMENT 1: SIMULATED USERS 345

We begin our experiments with simulated users. Then, we  $_{346}$ evaluate the shared autonomy with real human participants. 347 We use a binary value  $(0 \text{ or } 1)$  to simulate the decoded results  $348$ of the ErrP classifier. 349

## *A. Experiment Design* 350

We first consider the ErrP as a full observation with  $100\%$  351 accuracy and then consider ErrP as a partial observation with 352 different accuracy levels. We use an autonomous agent without 353 ErrP feedback as our baseline. Our central hypothesis is that 354 our method can improve the agent's performance despite the <sup>355</sup> partial ErrP observations. We use simulated pilots, which <sup>356</sup> enables us to more thoroughly consider different aspects of 357 our method (such as the effects of the ErrP accuracy level <sup>358</sup> on training an effective shared control model and gradient <sup>359</sup> analyses with different ErrP accuracies at various positions). <sup>360</sup> Moreover, we use a simulated ErrP to train the shared control 361 model that is used to test with real human users.

*1) Partially observable ErrP and without ErrP:* We first <sup>363</sup> trained an autonomous agent without ErrP feedback as the <sup>364</sup> baseline. We then trained six agents receiving ErrP feedback 365 with different levels of accuracy ranging from 65% to 100%. 366 We evaluated the agents in 20000 episodes with random 367 starting and target positions. Figure [3a](#page-7-0) shows the training 368 curve of the agents and Figure  $3b$  shows the average number  $369$ of steps used by each agents to reach the target. <sup>370</sup> <sup>371</sup> *2) Trained with full observation and evaluated with partial* <sup>372</sup> *observation:* To test the robustness of the POMDP model to 373 uncertainty, we compared two model: one was trained with 374 partial observations (75% ErrP accuracy) and another one was 375 trained with full observations (100% accuracy). We evaluated 376 the models with incrementally more complete observations 377 (ranging from 70% to 100% accuracy).

 *3) Gradient analysis on ErrP with different observation levels:* The gradient computes the derivatives of the outputs of a model with respect to the input variables and identifies which input variables are important for predicting the outputs. The gradient-based method is a natural and popular attribution 383 method [\[46\]](#page-13-13) for explaining deep neural network decisions. This method uses the learned model to determine how impor- tant the input dimension is for the output. To better understand the mechanisms that allow the POMDP model to perform well in uncertain environments, we analysed the performance and gradients of POMDP models with different accuracies. More specifically, we compared the gradient at 70%, 75%, and 80% accuracies. We found that when the ErrP accuracy is greater than 80%, the learned policy is the same as that learned when the accuracy is 100%. This result indicates that the ErrP gradients are the same when the accuracy is greater than 80%. Therefore, we compared the gradients of models trained with accuracies less than 80%.

 *4) ErrP gradient analysis at different positions:* During the test, we found that ErrP has a greater effect on the outputs in the central area than on those in the edge area. We visualized the ErrP gradient map of the model in the two environments to assess whether the ErrP has different effects on the outputs at various positions. The computation of the gradient map is extremely quick since it requires only one backpropagation pass. The gradient map encodes the effect of the ErrP signal on the agent's action at different locations. The colours represent different gradient values.

 *5) Agent performance analysis:* The performance was op- erationalized according to the step number and the success rate of the agent in reaching the target position from the start position. We compared the performance of agents with and without ErrP feedback. Even without human assistance, the agent would eventually reach the target. To evaluate the search ability of different distance ranges, we varied the initial distance between 2 and 20. Each distance was evaluated over 10000 runs. We compared the agent performance in the two 415 environments with no ErrP, 70% ErrP accuracy, and 80% ErrP accuracy.

#### <sup>417</sup> *B. Result*

 *1) Partial observation ErrP and without ErrP:* Figure [3](#page-7-0) shows that the agent with 100% accurate ErrP feedback performs better than the baseline agent without ErrP feedback. The result also suggested that higher ErrP accuracy corre-sponds to fewer steps required to reach the target position.

 *2) Trained with full observations and evaluated with partial observations:* Figure [4](#page-7-1) shows the average number of steps used during the test with models trained with full observations (100% ErrP accuracy) and partial observations (75% ErrP accuracy). The average number of steps decreased as the <sup>427</sup> correct probability increased for both conditions. However, <sup>428</sup> when the accuracy was less than  $80\%$ , the model trained with  $429$ partial observations used fewer steps than the model trained 430 with full observations. In contrast, when the accuracy was 431 greater than 80%, the model trained with partial observations 432 used more steps than the model trained with full observations. 433 The POMDP model allows the performance to scale linearly 434 as a function of the observation quality. Note that when the <sup>435</sup> accuracy was 70%, while both models exhibited a reduced <sup>436</sup> performance, the MDP model decreased to approximately 40 437 steps, while the POMDP model decreased to approximately <sup>438</sup> 27 steps. The performance of the model trained with full 439 observations declined considerably when presented with in- <sup>440</sup> complete observations. When the accuracy was 100%, the 44 POMDP model used approximately 12 steps, reaching near-<br> perfect levels (approximately ten steps). 443

*3) Gradient analysis of ErrP with different observation* <sup>444</sup> *level:* As shown in Figure [5,](#page-7-2) the ErrP gradient increases as  $445$ the ErrP accuracy increases. This result indicates that more <sup>446</sup> accurate ErrPs have more important effects on the outputs 447 than ErrPs with low accuracy. In contrast, when the ErrP has a 448 larger effect on the output, the effect of other input variables on  $449$ the output should be decreased. In other words, the gradients 450 of the agent's observations, such as the position variables, de- <sup>451</sup> crease. As shown in Figure [5,](#page-7-2) the position gradient decreased <sup>452</sup> as the ErrP accuracy increased. These results demonstrate that <sup>453</sup> human feedback gradually induces more effects, while agent 454 observations have fewer effects, as the ErrP accuracy increases <sup>455</sup> during training.  $456$ 

*4) ErrP gradient analysis at different positions:* Figure [6](#page-7-3) <sup>457</sup> shows model gradient maps of the two maze environments. 458 In general, the ErrP gradient is large in the central area and 459 small in the edge areas, which indicates that the ErrP has a 460 substantial effect on the central position. In other words, the 461 agent rely more on human feedback in central area than in <sup>462</sup> edge area. In future research, more advanced interpretation 463 methods, such as integrated gradients [\[47\]](#page-13-14) and SmoothGrad 464 [\[48\]](#page-13-15), could be used for further analysis. 465

*5) Agent performance analysis:* The average number of <sup>466</sup> steps were 51.2, 34.8, and 24.0 for the no ErrP condition, 467 70% accurate ErrP condition and 80% accurate ErrP condition <sup>468</sup> in environment 1 and 50.7, 40.8, and 25.7 in environment 2,  $469$ respectively. The average number of steps gradually increased <sup>470</sup> as the initial distance increased for both the ErrP conditions 47 and the no ErrP condition in environments 1 and 2.  $472$ 

Sixty steps was taken as the maximum number of steps; 473 that is, if the agent successfully reaches the target position <sup>474</sup> within 60 steps, it is considered a success. Otherwise, the  $475$ agent has failed. Figure  $7$  shows the success rate to reach  $476$ the target position within 60 steps for each initial distance.  $477$ The success rate gradually decreased as the initial distance 478 increased. The average success rates were  $79.74\%$ ,  $83.19\%$   $479$ and 95.86% for the no ErrP, 70% accurate ErrP and 80% <sup>480</sup> accurate ErrP conditions for environment 1 (Figure  $7a$ ) and  $481$ 69.43%, 76.70% and 94.21% for the no ErrP, 70% accurate <sup>482</sup> ErrP and 80% accurate ErrP conditions for environment 2 483 (Figure  $7b$ ). The success rate gradually decreased as the initial  $484$ 

2

 distance increased for both the ErrP conditions and the no ErrP condition in environments 1 and 2, except when the initial distance was the maximum value for the no ErrP condition in environment 2. The start and target positions were limited to the four corner positions, which allow the initial distance to be maximum value. We found that when the agent start position was (0, 0), the agent moved in the direction of the opposite corner. If the agent start position and target position were (0, 0) and (10, 10), 20 steps were used to reach the target position, which is the optimal number of steps. These results indicate that even when the ErrP signal is 70% accurate, the success rate is higher than the success rate in the no ErrP condition.

#### <sup>497</sup> *C. Discussion*

<sup>498</sup> *1) Performance of the shared control model:* The sim-499 ulation experiment indicates that the shared control model 500 can greatly improved the task efficiency compared with au-501 tonomous agent. As shown in Figure [7,](#page-9-0) even when the human 502 feedback was partially inaccurate, the success rate of 70% 503 and 80% of ErrP accuracy on the success rate to reach the <sup>504</sup> target position is larger than in the case of no ErrP. The 505 integration of the agent observations and human perception 506 help the agent gains more information about the environment <sup>507</sup> than an autonomous agent. Besides, the higher success rate <sup>508</sup> of 80% ErrP accuracy compared with 7% one demonstrated <sup>509</sup> that the agent can make better decisions with more accurate 510 **observation of the environment.** 

511 In the shared control policy with 100% accuracy, we found that if the ErrP signal is provided, the agent changes its search direction to the left in an anticlockwise search approach, as 514 shown in Figure [8a.](#page-9-1) The agent changes its trajectory in real-<sup>515</sup> time to adapt to the human feedback as previous study [\[49\]](#page-13-16). The same performance was observed when the ErrP accuracy was greater than 80%. However, when the ErrP accuracy was less than 80%, the agent learned a different accuracy. In this case, the agent did not change its search direction immediately after an ErrP signal was provided. Instead, the agent changed its direction when it was more confident. Thus, we hypothesize that the confidence level is related to the ErrPs of the previous steps and the current position. For the no ErrP condition, the agent's trajectory followed an anticlockwise search. The trajectory was fixed and depended only on the agent's starting point, as shown in Figure  $8b$ .

 *2) ErrPs with different accuracies:* We investigated the performance of agents trained with various noise levels during training. We provide the input accuracy during training. Figure [3a](#page-7-0) shows that the agent learned different policies during training with different ErrP accuracy levels, demonstrating that the ErrP accuracy could be learned by the model during 533 training. Figure [3b](#page-7-0) shows that the less uncertain the human feedback, the better decision the agent can make. In addition, we investigated the threshold of the ErrP accuracy that is sufficient for training an efficient shared control model. We found that if the ErrP accuracy is greater than 70%, the model trained with this ErrP accuracy performs better than an autonomous agent. However, if the ErrP accuracy is less than 70%, the shared control performance was not considerably different from that of a sole autonomous agent, as the sole 541 agent could learn a search policy without human feedback. <sup>542</sup> Thus, we take 70% as the threshold for training an effective 543 model. This result provided a new perspective on human <sup>544</sup> feedback accuracy in shared control critic models. Therefore, 545 we selected participants with offline accuracies greater than 546 70% for the online test.

*3) Model robustness:* As shown in Figure [4,](#page-7-1) the model <sup>548</sup> trained with high ErrP accuracy was more sensitive to ErrP 549 input than the other models. The agent is more likely to  $550$ change its search direction when the human user provides 551 negative feedback. In other words, human users have a more 552 significant effect on the agent's action in a more accurate ErrP 553 model than in a less accurate ErrP model. The performance 554 declines dramatically when using the model trained with full 555 observations and tested with partial observations. However, <sup>556</sup> the model trained with partial observations is more capable 557 of handling partial observability when the observation quality 558 changes during the evaluation. The results are consistent with 559 the results of  $[22]$ : the model trained with partial observations  $\frac{560}{2}$ is robust towards missing game screens and remains scalable, 561 improving the performance as more data become available.  $562$ Furthermore, the model trained with partial observations was 563 more robust to uncertainty during evaluation, despite the fact 564 that the two learned models used the same neural network 565 architecture. In addition, the model is scalable enough to <sup>566</sup> improve performance as the observation accuracy increases.  $567$ Therefore, during the test with real human participants, we 568 chose the shared control model trained with ErrP accuracy, <sup>569</sup> which is similar to real EEG classification accuracy with cross-  $570$ validation. 571

# V. EXPERIMENT 2: REAL-WORLD USER STUDY 572

In this section, we evaluate our method during the test phase 573 with real human participants. Our model was pretrained with  $574$ simulated EEG data. We want to validate the feasibility of  $575$ using the model trained on simulated EEG data with real  $576$ human participants in the same task environment. We validate 577 the feasibility of the learned model in two environments: <sup>578</sup> a environment without obstacles and a environment with <sup>579</sup> obstacles. 580

# *A. Experiment Design* 581

*1) Interaction environment design:* To evoke ErrP signals, <sup>582</sup> the interaction environment, especially the stimulus, needs to 583 be carefully considered  $[50]$ . The environment design was  $_{584}$ based on the design presented in  $[21]$ , which includes a grey  $\frac{585}{2}$ grid with a red agent and a green target on a black background. 586 The agent's start and target positions were generated under 587 the condition that their distance be larger than one grid (the 588 agent's observation ability). At each step, the agent moved 589 from its current position to one of the four adjacent positions. 590 A 1 s animation within the agent served as a countdown <sup>591</sup> to draw the participants' attention. The agent then jumped 592 instantaneously to the next position, with an arrow directed 593 towards the position. This arrow remained visible for 1 s. <sup>594</sup>

<span id="page-7-0"></span>

Figure 3: Training curve with different ErrP accuracies conditions as well as no ErrP condition (a). The average number of steps used to reach the target position (b).

<span id="page-7-1"></span>

Figure 4: The average number of steps used to reach the target position for different accuracy levels with models trained on partial and full observations.

<span id="page-7-2"></span>

Figure 5: ErrP and position gradients with different ErrP accuracies.

<span id="page-7-3"></span>

Figure 6: ErrP gradient distribution at different positions in the maps of the two environments. The color indicates the gradient value at different positions

Then, the highlights disappeared, and the agent remained at 595 its new position for 1 s before its next step.

Before the real-time control experiment, participants were 597 first asked to perform five blocks of 120 trials in environment 598 1, which contained no obstacles. The agent's initial and target 599 positions were randomly generated. If the agent did not reach 600 the target position after  $60$  trials, a new run was started.  $601$ The EEG data collected during these five blocks were used 602 to calibrate the classifier. If the agent's action decreased 603 the distance to the target position, the action was labelled  $604$ "correct"; if the agent's action increased the distance to the 605 target position, the action was labelled "error". During the 606 experiment, the participants were asked to mentally judge  $607$ whether the agent's action was correct or an error.

2) Participants: Sixteen participants (average age  $28.57 \pm \degree$ 3.11 years old, two females) participated in the experiment. 610 Seven participants participated in both the offline-BCI and 611 online-BCI experiments. Seven participants participated in 612 only the offline experiment, as their ErrP BCI performance  $613$ were below the 70% threshold. As described in Section IV.C, 614 the shared autonomy model performs better only when the 615 ErrP classification accuracy is greater than 70%. The remain<sup>617</sup> ing two participants were excluded from further analysis, as the participants could not complete the online experiment due to battery power issues. All participants provided informed consent for the study, which was approved by the University of 621 Technology Sydney (UTS) Human Research Ethics Committee (ETH19-3830). All participants had normal vision and did not report any known neurological or psychiatric diseases.

<sup>624</sup> *3) EEG recording and pre-processing:* EEG signals were 625 recorded from 64 locations according to the extended 10/20 626 system using a LiveAmp wireless EEG system from Brain  $627$  Vision [\[51\]](#page-13-18) with a sampling rate of 500 Hz. The reference <sup>628</sup> channel was placed at the FCz channel position, and the <sup>629</sup> ground channel was placed at the forehead position [\[51\]](#page-13-18). The <sup>630</sup> signal was resampled to 256 Hz and filtered using a finite  $631$  impulse response (FIR) bandpass filter with cut-off frequencies 1-50 Hz.. Then, the common average reference was used to 633 reduce signal contamination. Both offline training and online 634 testing used a same EEG signal pre-processing pipeline

 *4) ErrP Feature extraction:* Temporal features extracted from time-series data have been used in many ErrP activity studies  $[1, 50, 52, 53]$  $[1, 50, 52, 53]$  $[1, 50, 52, 53]$  $[1, 50, 52, 53]$  $[1, 50, 52, 53]$  $[1, 50, 52, 53]$  $[1, 50, 52, 53]$ . It has been reported that the classi- fication results of temporal features are better than those of 639 spectral features for decoding ErrP signals [\[54\]](#page-13-21). Thus, tempo-<sup>640</sup> ral features were used for classification in this study. **Similar** 641 with studies [\[21,](#page-12-15) [24\]](#page-12-18), the averaged signal amplitude within a 30-ms-long window between 150 ms and 600 ms at each trial and channel was extracted. Thus, during the time window 644 from 150 ms to 600 ms, there will be  $15 = ((600 - 150)/30)$ **samples for one channel.** The classification between correct and error feedback was performed from all 64 EEG electrodes [\[21\]](#page-12-15). Thus, the feature vector length is  $64*15=960$ .

 *5) ErrP classifier training:* To enable real-time detection of neural activity during each trial, the classifier must be calibrated to classify the EEG waveform as ErrP or non- ErrP. This ErrP classification is a binary classification task that indicates the agent's action as correct or incorrect.

 To minimize overfitting effects, we used tenfold crossvalidation to train the classifier with 90% of the data, and the remaining 10% of the data were used for testing. The extracted features include redundant features, and traditional linear discriminant analysis (LDA) has limited flexibility for complex features. Thus, it is necessary to search for a subset of the available features that can improve the classification performance. Shrinkage and selection methods are commonly used feature selection methods. We use shrinkage LDA [\[55\]](#page-13-22) as the classifier in our paper, which is widely used for decoding  $663$  ErrP signals [\[50\]](#page-13-17).

 A binary linear classifier can be characterized by a projec- tion vector **w** and a bias term b referring to the separating 666 hyperplane  $\mathbf{w} \mathbf{x} + b = 0$ . The projection vector of LDA is defined as:

$$
w = \boldsymbol{S}_w^{-1}(\boldsymbol{u}_a - \boldsymbol{u}_b) \tag{1}
$$

 $\epsilon_{668}$  Where  $S_w^{-1}$  is the covariance or within class variance,  $u_a$  $\epsilon_{69}$  and  $u_b$  is the mean value of class A and class B.

<sup>670</sup> The empirical covariance of the above is unbiased and <sup>671</sup> has good properties when the number of observations is greater than the dimensionality of variables. However, for 672 high-dimensional data with only few data trials, the estimation  $\frac{673}{2}$ covariance may become imprecise because the covariance <sup>674</sup> of matrix estimate is singular and the inverted matrix in <sup>675</sup> imprecise. This phenomenon leads to a systematic error: large 676 eigenvalues of the original covariance matrix are estimated 677 too large, and small eigenvalues are estimated too small  $[56]$ .  $678$ This estimation error makes the performance of LDA in  $679$ high-dimensional situations far from optimal. Shrinkage is a 680 common method that compensates the systematic bias in the 681 estimated covariance matrix by a regularized covariance matrix 682  $\boldsymbol{S}_b$  : 683

$$
\boldsymbol{S}_b = (1 - \lambda)\boldsymbol{S}_b + \lambda \boldsymbol{D} \tag{2}
$$

Where  $D$  is a diagonal matrix taking the diagonal elements  $\epsilon_{\text{68}}$ of  $S_b$ . Thus, the parameter  $\lambda$  forces the extreme eigenvalues 685 towards average  $[56]$ . 686

6) Online test with real participants : The participants 687 who achieved ErrP accuracy threshold of  $70\%$  further the  $688$ online test. The shared control model that best matched the 689 participant's offline accuracy was used in the online test. 690 For example, if the participant's offline ErrP classification 691 accuracy is 78%, we chose the shared control model that pre- <sup>692</sup> trained with 80% ErrP accuracy. The computational cost for 693 the training model is about 40 hours and 30 munites, which  $_{694}$ is running on a workstation with two Intel Xeon 6132 CPUs 695 and NVIDIA RTX 6000 GPUs, as well as 96GB of RAM. 696

#### *B. Results* 697

*1) Electrophysiology analysis:* Figure [9](#page-9-2) shows the correct, 698 error, and difference grand average potentials (error minus 699 correct averages) in the Fz channel averaged across all subjects  $\frac{700}{200}$ in the online sessions for both environments. The difference  $701$ grand average was characterized by three components: a neg-  $702$ ative deflection at approximately 200 ms, a positive deflection  $\frac{703}{200}$ at approximately 300 ms, and another negative component at  $_{704}$ approximately 400 ms.  $\frac{1}{205}$ 

*2) Classification analysis of ErrP:* In this section, we <sup>706</sup> analyse the real-time classification accuracy of the ErrP signals 707 with the classification model calibrated with offline data for the  $\frac{708}{208}$ two environments. As mentioned in the simulation section, if  $\tau_{09}$ the ErrP accuracy is less than  $70\%$ , the low ErrP classification  $710$ accuracy and no ErrP models perform similarly. Table [I](#page-9-3) shows  $_{711}$ the offline training accuracy using 10-fold cross-validation  $712$ and the online test accuracy for the two environments. The 713 overall offline training accuracy was 76.65%. The overall  $_{714}$ online test accuracy were  $73.22\%$ , 69.20% for environment  $715$ 1 and environment 2, respectively.

3) Agent performance analysis: In this section, we analysed  $\frac{7}{17}$ the success rate and number of steps for real human users to  $718$ evaluate the feasibility of the shared control model with real 719 human participants. To test the model's target search ability 720 for different initial distances, we chose episodes with initial  $\frac{721}{721}$ distances between 2 and 20 (maximum), resulting in a total  $722$ of 19 episodes with random sequences for each environment. <sup>723</sup> The episodes were pregenerated for all the participants.  $\frac{724}{2}$ 

During the online test, the brain signal's classification of  $\pi$ 25 the agent's last action as either correct or an error was fed 726

<span id="page-9-3"></span>

Participant	Offline training $(\%)$	Online test of environment $1 \ (\%)$	Online test of environment $2 \ (\%)$					
S <sub>2</sub>	73.33	77.68	77.73					
S4	72.83	60.88	58.02					
S <sub>5</sub>	85.17	94.75	65.02					
S <sub>6</sub>	74.67	69.01	66.54					
S8	76.17	71.91	66.11					
S <sub>10</sub>	80.17	71.81	70.25					
S <sub>15</sub>	75.33	64.28	70.11					
Average	76.65	73.22	69.20					

Table I: ErrP training accuracy with 10-fold cross-validation and test accuracy for the two environments.

<span id="page-9-0"></span>

(b)

Figure 7: Success rate of reaching the target position within 60 steps for each initial distance with the no ErrP, 70% accurate ErrP, and 80% accurate ErrP conditions for environments 1 and 2.

 into the model in real-time to generate the next action. If the agent did not reach the target position after 60 steps, the run was ended, and a new episode was started. The maximum number of steps was set to ensure that participants were not discouraged by long runs. In the experiment with real human participants, the maximum number of steps was set to 60 for each episode. Therefore, episodes with more than 60 steps were not included when calculating the average number of <sup>735</sup> steps.

<span id="page-9-1"></span>

Figure 8: The agent search policy with 100% accurate ErrP (a) and no ErrP (b).

<span id="page-9-2"></span>

Figure 9: ERP analysis for the correct and error conditions, averaged over the online trial sessions at Fz channel by removing baseline [-300 0]ms. The black line is the difference between correct and error condition. The red and blue dotted lines are the standard deviation for the error and correct conditions respectively.

As shown in Table [II,](#page-10-0) the success rate to reach the target po- $\frac{736}{2}$ sition within 60 steps was  $81.20\%$ , and this value was averaged  $737$ over all participants. The average number of steps was 24.87, 738 which was averaged over all participants by removing failed  $\frac{739}{2}$ episodes. The success rate was approximately the same as <sup>740</sup> the success rate of the 70% accurate ErrP condition  $(83.19\%)$   $_{741}$ and was larger than the success rate of the no ErrP condition 742  $(79.74%)$  in the simulations. The average number of steps was  $743$ almost the same as the number of steps in the  $70\%$  accurate  $744$ 

<span id="page-10-0"></span>

		Success rate $(\% )$	Mean and standard of number of steps								
	Env 1	Env <sub>2</sub>	Env <sub>1</sub>	Env <sub>2</sub>							
S <sub>2</sub>	94.74	89.47	$23.11 \pm 13.2$	$20.06 \pm 14.38$							
S <sub>4</sub>	78.95	84.21	$26.07 \pm 16.56$	$26.88 \pm 13.97$							
S <sub>5</sub>	94.74	84.21	$21.06 \pm 11.73$	$22.69 \pm 12.93$							
S6	63.13	63.16	$29 \pm 18.69$	$28.42 \pm 15.78$							
S8	78.95	89.47	$24.8 \pm 14.57$	$17.53 \pm 9.91$							
S <sub>10</sub>	84.21	94.74	24.94±15.74	$23.61 \pm 12.81$							
S <sub>15</sub>	73.68	89.47	$28.86 \pm 17.59$	$21 \pm 13.35$							
Ave	81.20	84.96	$24.59 \pm 14.66$	$21.92 \pm 12.97$							

Table II: Success rate and average number of steps with real human participants.

 ErrP condition (24.4) and less than the average number of steps in the no ErrP condition (28.4). With real human participants, the number of steps was 12.43% less than the number of steps in the no ErrP condition.

 As shown in Table [II,](#page-10-0) the success rate to reach the target po- sition within 60 steps was 84.96%, and this value was averaged over all participants. The average number of steps was 23.28, which was averaged over all participants by removing failed <sub>753</sub> episodes (failure rate=1-success rate). The success rate was better than that of the 70% accurate ErrP condition (76.70%) and the no ErrP condition (69.43%) in the simulations. The average number of steps was smaller than that in the 70% accurate ErrP condition (25.6) and no ErrP condition (25.4). With real human participants, the number of steps was 8.35% less than the number of steps in the no ErrP condition.

#### <sup>760</sup> *C. Discussion*

 *1) Feasibility of simulated ErrP for training:* We demon- strated the feasibility of our method, which involves training with simulated data and testing with real EEG data, with human participants in real time. The key idea is that the simulated data were binary values (0 or 1) based on the ErrP classifier, which has a binary output (0 or 1). The simulated pilot enables us to train the model without real users. Training an RL model requires a vast amount of data, which rendered the capturing of the EEG from real users infeasible. Thus, we use binary values instead of a linear scale between 0 and 1 to increase the similarity between the simulation data and the classification results of real EEG data. The simulated ErrP data can also be scaled linearly between 0 and 1 to train the model. In this case, the classifier's output should scale linearly with the real ErrP data, which is related to the goal congruency, as discussed in [\[21\]](#page-12-15).

 *2) Consider the learning as a POMDP with noisy ErrPs:* The policy learned with clean observations (100% accurate 779 ErrP) is not **robust** and vulnerable when the environment is inherently noisy during the test. The discrepancy between the clean simulated ErrP data and the real human EEG data contributes to this "reality gap". The real human ErrP feedback cannot match the simulated feedback with 100% 784 certainty. Thus, the shared policy may fail with real human participants because the ErrP signal cannot be decoded with 786 100% accuracy. We formulate the learning as a POMDP and train the model with simulated noise observations. We find that the model trained with partial observations is more 6

robust to noise during the test than the model trained with full 789 observations. <sup>790</sup>

3) Area analysis: As shown in Figure [10,](#page-11-3) the environment 791 was divided into two areas: the central area and the edge area. 792 Figure  $11$  shows the ErrPs of online sessions in the central  $793$ and edge areas. The positive and negative peaks of the ErrP  $\frac{794}{60}$ in the central area were larger than those in the edge area. 795 We hypothesize that the participant was more involved in  $\frac{796}{60}$ the experiment when the agent was in the central area than 797 when the agent was in the edge area. We also analysed the 798 accuracy in the central and edge areas during environment 2. <sup>799</sup> As shown in Figure  $12$ , the online test accuracy was higher in  $\sim$  800 the central area than in the edge area, except for participant  $\frac{801}{201}$  $S10$ , where the accuracy in the edge area was slightly higher  $802$ than that in the central area, and participant S15, where the 803 accuracy was the same in both the central and edge areas. <sup>804</sup> Both the larger ERP peak amplitude and higher ErrP accuracy 805 in central area demonstrated that the participants give more 806 correct feedback in the central area than in the edge area.  $807$ These findings indicate that human participants with better 808 performance should be assigned more authority in the critical some central area than in the edge area. The simulation result of the 810 gradient map shown in Figure [6](#page-7-3) demonstrates that the ErrP 811 acquired from the simulated users has a greater effect in the 812 central area than in the edge area.

4) *ErrP peak analysis:* As shown in Figure [9,](#page-9-2) the amplitude 814 of negative peak of error condition is bigger than correct 815 condition. However, the correct condition has positive peak 816 amplitude that error condition. Similar result was found in 817 [\[57\]](#page-13-24), where P300 amplitude following error feedback was  $818$ not larger than those following correct feedback. We also 819 analyse the difference between the positive peak and nega- <sup>820</sup> tive peak while an agent continuously performed the wrong 821 action. Figure  $13$  shows that the peak decreased in the first  $822$ four sequences. We hypothesize that the participant has less 823 expectations of the agent behaviour, as  $ErrP$  signals are evoked  $824$ by unexpected errors. Similar finding was also reported in  $[58]$ , 825 where the  $1^{st}$  and  $2^{nd}$  feedback ErrP responses exhibited slight assets differences in terms of latency and amplitude. However, we 827 could not explain the increase after the fifth sequence. This 828 increase may be related to the participant's emotional state. 829 Future research should attempt to determine how continuous 830 errors affect the ErrP peak. Note that the agent action was 831 determined by the control model and the agent observations,  $\frac{832}{2}$ including the environment information and the ErrP signal. 833 Even if the ErrP classification is correct, the agent can still 834 perform incorrect actions, especially in the edge areas, as the 835 ErrP has a smaller effect on the agent actions in this region  $836$ based on the gradient analysis.

*5) Potential and Limitation of the shared control model:* <sup>838</sup> In addition to testing the shared control model in a simulation 839 environment, one potential breakthrough of this research was 840 to test and demonstrate the shared autonomy in real environment. The ErrP classification accuracy would be a key part 842 of feasibility of the shared control used in real environment. <sup>843</sup> Unlike in previous study of ErrP-based shared control[\[12,](#page-12-7) 844 [19,](#page-12-14) [21\]](#page-12-15), we demonstrated that the model worked successfully  $845$ when the ErrP classification reached higher accuracy. One 846

<span id="page-11-3"></span>

Figure 10: The environment was divided into central areas and edge areas.

<span id="page-11-4"></span>

Figure 11: ERP of the error condition in the central and edge areas in Fc channel. Statistically significant difference  $(p < 0.05)$  was found at green area between error and correct conditions

847 major limitation of the proposed shared control model is <sup>848</sup> that the shared-controlled agent would perform better than an <sup>849</sup> autonomous one only if the ErrP classification accuracy is <sup>850</sup> above 70%. Achieving such classification accuracy in a real-<sup>851</sup> world environment where the user is subject to distractions <sup>852</sup> and noises could be challenging. Further advancements in 853 EEG hardware is required before the proposed framework can 854 be adapted outside a lab environment. The preprocessing and 855 classification could also be optimized to improve the ErrP 856 classification accuracy. The preprocessing used in this paper 857 are not considering possible confounds due to eye movements, 858 which is critical for error-related signals analysis. Moreover, 859 the feature selection and classification algorithm could be 860 **optimized to improve classification accuracy.** 

#### 861 VI. CONCLUSION

 We proposed an ErrP-based shared control paradigm with deep recurrent reinforcement learning. To address the low decodability of the ErrP signals, we formulated the learning as a POMDP and used an RNN to solve the POMDP. The shared control model was trained with a simulated ErrP with 867 a Bernoulli distribution with probability  $\overline{P}$  of observing the

<span id="page-11-5"></span>

Figure 12: ErrP accuracy of online test for central and edge areas.

<span id="page-11-6"></span>

Figure 13: The average difference between the positive and negative peaks versus the error level.

truth. We validated the proposed model with real-time EEG 868 data obtained from human participants during a navigation 869 task. The agent can adaptively change its search direction 870 based on human feedback. The good performance of the model 871 in simulations and experiments with real human participants 872 suggests that our method is effective in human-robot shared  $873$ autonomy environments with uncertain noise input, such as 874 neural activities.

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APPENDIX 1105

	episode										10						16		18	9	Failed
	distance		. .	. I		4			18			16			1 U		20				Number
S <sub>2</sub>	step		14	42	60	32	$\sim$	45	20	45		44			◠ $\overline{1}$	9	26	$\sim$ ∸	<sub>6</sub>	$\sim$ 23	
S4	step	60	32	54	31	-60	⌒ $\sim$ 1		30	60		49	20			60	42		<sub>6</sub>	49	
S5	step	$\overline{\phantom{a}}$	າາ ∸	Ω	45	42	$\cap$ 23	$\mathbf{\tau}$	18	$^{\circ}$ 41					36	9	20	18	36	60	
S6	step	$^{\circ}$ ∠⊥	24	16	35	56	60		60	60		56	16	ີ 22	60	60	60	60	36	55 ر ر	
S8	step	$2^{\circ}$ دے	20	26	57 J	32 ے د	$\sim$ $\sim$ 1		20	60		43		4 <sub>1</sub>	18	60	24	31	60	60	
S <sub>10</sub>	step	52 ر ر	50	-60	60	$\mathcal{D}$ ∠∠	$\gamma$ 28		60	25		16			34		42	40	14	-	
$\overline{S15}$	step	$\overline{ }$	60	60	48	38	60		23	$\overline{45}$		55			т.		60	50	34	60	

Table A1: Number of steps used in environment 1 with real human participants

	episode										II.		∸		4ء		16		18	B	Failed
	Distance			4		۰.					ιч			<b>I</b>	∼	18	10	20		16	Number
S <sub>2</sub>	Steps		23	48		60	$\sqrt{2}$ ∼	19	ΙV	$\cap$ . .	53 ت ر	29		24		28	30	60	$\mathbf{\tau}$	16	
S4	<b>Steps</b>	43	≘ ∠⊥	30		$\sim$		19	10	29	31	60	38	60	28	26	58	24	-41	60	
S <sub>5</sub>	<b>Steps</b>			$\gamma$ $\angle$		∸	$\sim$ ∼	60	$\overline{1}$	40	37	60	◠	16	16	38	38	36	60	34	
S6	<b>Steps</b>		60	58		4,	60	60	60	30	60	31	36	26		38	22	60	60	38	
S <sub>8</sub>	Steps		19	$\sim$ ∠∠	$\overline{ }$	$\sim$		. .		60	24	24		^ 1 U		60	14	40		$\sim$ 34	
S <sub>10</sub>	<b>Steps</b>	د.	$\mathcal{L}$ ∠	-60				. .	$\overline{1}$	37	29	33		20	46	44	34	30		$\cap$ ∸	
S <sub>15</sub>	Steps	⌒	$\mathcal{L}$ <u>، ،</u>	$\Omega$ $\circ$		- 43	60	60	$\sim$ 1 V	1 <sub>2</sub> $\overline{1}$	1 C	29		38		24	40	$\sim$ $\overline{\phantom{a}}$	18	20	

Table A2: Number of steps used in environment 2