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Downstream Semi-Circular Obstacles' Influence on Floods Arising from the Failure of Dams with Different Levels of Reservoir Silting 2

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ABSTRACT 16

17 Dam-break wave-propagation in a debris flood event is strongly influenced by accumulated reservoir-bound sediment and downstream obstacles. For instance, the Brumadinho dam disaster in 18 19 January 2019 released 12×10^6 m³ of mud and iron tailings and inflicted 270 casualties. The present 20 work was motivated by the apparent lack of experimental or numerical studies on silted-up reservoir 21 dam-breaks with downriver semi-circular obstacles. Accordingly, 24 dam-break scenarios with different reservoir sediment depths and with or without obstacles were observed experimentally and 22 23 verified numerically. Multiphase flood waves were filmed, and sediment depths, water levels and values 24 of front wave celerity were measured to improve our scientific understanding of shock wave propagation over an abruptly changing topography. The strength of OpenFOAM software in estimating 25 such complex phenomenon was assessed using two approaches: Volume of Fluid (VOF) and Eulerian. 26 27 An acceptable agreement was attained between numerical and experimental records (errors ranged from 28 1 to 13.6%), with the Eulerian outperforming the VOF method in estimating both sediment depth and 29 water level profiles. This difference was most notable when more than half of the reservoir depth was 30 initially filled by sediment (≥ 0.15 m) and particularly in bumpy bed scenarios.

Keywords: Silted-Up Dam-break, Semi-Circular Obstacle, Image Processing, Abruptly Changing 31 32 Topography, Multiphase Shock Wave, OpenFOAM

33 INTRODUCTION

34 Sediment deposition in dam-bound reservoirs has become a considerable and widely occurring problem, posing a serious challenge to the design of and completion of dams (Vischer and Hager 1998). 35 The problem is particularly critical for smaller reservoirs lacking a bottom outlet system, as these 36 frequently become completely silted-up (Vischer and Hager 1998). Floods, which involve the mixing 37 of a massive saturated sediment layer with free surface water, occur predominantly during dam-break 38 39 events that are coupled with silted-up reservoirs (Shi et al. 2019). Considering the complex phenomena generated by such events, the behaviour of three phases must be considered: air, clear water (no 40 sediment), subtended by a saturated sediment level (Duarte et al. 2011). 41

A break in a silted-up dam results in the movement of dense sediment deposited in the reservoir and may lead to irreparable destruction and casualties. Infrastructure and agricultural areas located along the dam, downstream of the dam, or in the lower reaches of adjacent river basins may be buried under a large quantity of mud and debris flow. For instance, in January 2019, Brazil's Brumadinho dam-break released roughly 12×10^6 m³ of iron ore tailings and mudflow, which destroyed houses, farms, inns, mine's offices, and roads downstream from the dam. In the Brumadinho township, many agricultural areas were affected or totally destroyed, and at least 270 people died (Wikipedia 2019).

49 Interactions between reservoir water and the large volume of sediment stored in dam reservoirs strongly affect sediment layer motion and flood propagation (Yang 1996). In addition, structures and 50 installations located in flood-prone areas downstream from a dam may act as obstacles to a flood's 51 52 propagation following a dam-break, with potentially harmful consequences in terms of the collapse of 53 remaining structures. The presence of such obstacles in the flood plain adjoining the river may also 54 influence flood characteristics, such as wave velocity and depths downstream from obstacles. 55 Consequently, the accurate prediction of silted-up dam-break flow behaviour over natural terrain and 56 bumpy downstream reaches is vital to prevent and mitigate catastrophic flood disasters.

57 Although the failure of dams retaining water-filled reservoirs (no sediment) is a major consideration 58 in hydraulic engineering and has been widely scrutinised numerically and experimentally, only a few 59 studies have investigated the severe problems of sedimentation in dam reservoirs (Duarte et al. 2011). 60 Most relevant experimental (Xue et al. 2011) and numerical studies (Wu and Wang 2007; Valiani et al. 2002) on reservoirs with sedimentation were only recently conducted in the 21st century. The 61 62 characteristics of dam-breaks and their resulting flood waves were extensively investigated and documented for clear water, with experiments addressing a wide range of upstream and downstream 63 64 initial simple conditions but only simple one- or two-dimensional scenarios (Wu and Wang 2007; 65 Valiani et al. 2002). While past studies mostly focused on constant bed scenarios (Crespo et al. 2008), 66 the role of sediment movement in failure of a dam with a mobile bed has lately gained more attention 67 (Postacchini et al. 2014; Evangelista et al. 2013). To the best of the authors' knowledge, there are limited 68 numerical or experimental studies concerning dam-break multiphase shock flood waves from a 69 reservoir with a high degree of silting.

70 Recently, the incorporation of downstream obstacles into increasingly complex mobile-bed dambreak scenarios has been studied (Issakhov and Imanberdiyeva 2019; Kattel et al. 2018; Kamra et al. 71 72 2019; Mokhtar et al. 2019). Specifically, these works used considered obstacles of various geometric 73 shapes, such as a vertical wall (Mokhtar et al. 2019), triangular-shaped barriers (Ozmen-Cagatay et al. 74 2014), lateral sidewalls (Kocaman et al. 2012), vertical cylinder (Kamra et al. 2019), single cube (Aureli 75 et al. 2015), and group of cubes (Goseberg et al. 2016; Güney et al. 2014). Moreover, there have been 76 extensive numerical studies on the influence of obstacles on dam-break phenomena (Gallegos et al. 77 2009; Hänsch et al. 2014; Jeong et al. 2012; Saghi and Lakzian 2019; Singh et al. 2011). A dam-break 78 is usually investigated numerically with triangular downstream obstacles (Kattel et al. 2018; Cheng et 79 al. 2017; Saghi and Lakzian 2019; Singh et al. 2011) or a group of cubes to represent an urban area 80 (Jeong et al. 2012; Wang et al. 2017). However, similar scenarios with a vertical wall (Hänsch et al. 81 2014), single cube (Aureli et al. 2015), trapezoidal obstacles (Issakhov et al. 2018; Kattel et al. 2018), 82 and groups of obstacles that represent vegetation have also been studied numerically (He et al. 2017). Since typical forms of obstacles in nature are semi-circular (e.g., humps and hill-like barriers), rounded 83 84 downstream obstacles with different cross-sections were investigated in the present study to better reflect natural terrain. To the authors' knowledge, such obstacles have rarely been presented in the 85 literature compared to triangular and trapezoidal obstacles. 86

Shock floods arising from dam-break phenomena on a mobile bed and sediment motion in open channel flows are critical issues and have been investigated both numerically and experimentally (Shi et al. 2019; Fu and Jin 2016; Zhang and Wu 2011; Mambretti et al. 2008). Nevertheless, there is a great distinction between the usual sediment height in a typical reservoir or river bed and the high sediment level in a silted-up reservoir, which has rarely been addressed (Duarte et al. 2011).

92 A rigorous literature review revealed the limited amount of studies on the behaviour of floodwaters 93 when they meet a semi-circular obstacle in situations where the failed dam had a silted-up reservoir. 94 Therefore, our study is novel in that it involved both experimental analysis and numerical verification of multi-layer shock wave characteristics (e.g., water level, sediment depth, and wave celerity) in a 95 situation where semi-circular obstacles were present. Various upstream sediment depths, which 96 97 occupied 10-80% of the reservoir's total height, combined with the downstream presence or absence of semi-circular obstacles of various cross-sections at a specified distance from a dam section, created 24 98 99 different scenarios. The experimental results were carefully filmed using high-speed professional 100 cameras. Experimental data, including water levels and sediment depths along the experimental flume, 101 have been provided and can be used for validation in other studies. The numerical portion of the current 102 research verified the 24 dam-break experimental scenarios via OpenFOAM software using two distinct methods (OpenVFOAM 2015): VOF (Volume of Fluid) and Eulerian. Laboratory records were 103 rigorously compared with the predictions of both numerical methods. 104

105 EXPERIMENTAL MODELLING

106 All experiments were performed in the Hydraulic Lab of Shiraz University (Iran). The dimensions 107 of the studied rectangular channel were 0.3 m width, 6 m length, and 0.32 m depth, including a 108 horizontal smooth bed. The bottom was steel, and both lateral walls were glass. The length of the flume was partitioned via a moving gate installed to create a reservoir with a length of 1.52 m (Fig. 1a), and a 109 110 downstream channel with a length of 4.5 m (Vosoughi 2018). Dam-break waves were produced in the 111 downstream part of the flume by the instantaneous release of reservoir water. The effects of semi-112 circular downstream obstacles on multiphase flood waves in an initially dry-bed downstream were 113 examined. The schematic illustration of the three-phase shock wave propagating along the flume and

over the hump is detailed in Fig. 1b. Representing natural topography, the hump can lead to a sudden

115 change in flood wave propagation in certain parts of the downstream channel.



Fig. 1. Schematic side view of (a) experimental setting (b) dam break multiphase flow. a) Plan view of flume components, instruments' locations and the obstacle position. All not to scale (Vosoughi 2018). b) Side view of silted-up dam break wave propagation over a downstream semi-circular obstacle and the schematic geometry of obstacles

116 Experimental set-up

The experimental environment, facilities, and instruments used in this study are shown in Figures 2a-g. Throughout the 6-month study, three high-speed cameras were mounted in fixed positions at equal intervals over the 5.52 m stretch of the flume (Figs. 2c-e) to record videos and collect high-quality water level, sediment depth. Two powerful spotlights were located at each channel extremity to provide illumination. The flume was equipped with a sudden opening gate (i.e., the dam) and a position to affix the semi-circular obstacle downstream from the dam (Fig. 1). The gate consisted of two plates made of Plexiglass separated by a wider rubber layer (to prevent leakage at the edges) and totalled 0.01 m in thickness. Two powerful wooden clamps were attached to the gate to make it more stable. Grease was
applied to the edges of the gate to allow for easier motion. The beginning of the reservoir was blocked
by two walls fabricated with Styrofoam sheets and medium-density fibreboard (MDF).



Fig. 2. Experimental environment and facilities; (a) highly exposed zone inside the flume, (b & g) right and left spotlights, respectively, (c, d & e) first, middle and third cameras, respectively, (f) onset of the reservoir (channel's first point)

127 In order to simulate a silted-up reservoir, a quartz sand mixture with uniform grain sizes of mainly 128 0.2-0.4 mm in diameter (see Supplementary Material; Table S1 and Fig. S1) served as the experimental 129 dam-retained sediment. Prior to each test, the sediment was rinsed and desiccated, the reservoir was 130 filled to the required sediment depth, and the horizontal surface of the sediment layer was smoothed by 131 hand with a putty knife. Water was then injected at a very low rate into the reservoir up to a height 132 (h_0) of 0.3 m. After each test, the flume was cleaned and dried in order to keep adhesive forces between 133 the flume and other materials relatively constant.

To physically simulate dam-break flow, a complex mechanism was constructed and installed in the flume with a gate (dam) that could be suddenly lifted. The sluice gate release time should be smaller than $\sqrt{2(h_0/g)}$, where g represents the acceleration of gravity (Lauber and Hager 1998). Considering $h_0 = 0.3$ m, the greatest release time was calculated as 0.247 s. However, the actual sluice gate release time ranged from 0.08 to 0.16 s, which was confirmed using high-speed videos.

139 Experimental scenarios

A reservoir with clear water (no sediment) and seven distinct depths of sediment (S_0 = 0.03, 0.075, 0.15, 0.175, 0.2, 0.22, and 0.24 m) were tested as the initial conditions in the upstream to scrutinize different silted-up flood depths and velocities. A completely dry bottom with or without an obstacle was set as the downstream hydraulic conditions. Scenarios in the absence of downstream obstacles (smooth bed) were considered to obtain an appropriate comparison basis for other initial conditions.

Two humps (semi-circular obstacles) with various cross-sections (0.045 and 0.075 m) were firmly 145 installed at the bottom of the downstream channel (1 m after the dam section) and further stuck to the 146 147 channel's side walls using rubber sheets. Both obstacles were made of Styrofoam sheets with a 148 schematic geometry, as illustrated in Fig. 1b; the obstacles displayed lengths of 0.3 m and widths of 149 0.09 and 0.15 m. A relatively heavy weight was bolted to the obstacle's downstream side to provide sufficient stability during flood wave impacts. The obstacles' O_r/h_0 ratios were 0.15 and 0.25, where 150 h_0 and O_r represents the initial reservoir water level and downstream obstacle's radius, respectively. 151 Table 1 lists the 24 scenarios examined in this research, outlining the upstream sediment depths and 152 downstream hydraulic conditions. To verify repeatability, achieve high quality data, and ensure reliable 153 results, scenarios were repeated twice. Changes between experimental replicates remained under 3%. 154

155 Data collection and image processing

A digital image processing technique was applied to measure the required physical parameters from
silted-up dam-break shock waves over a bumpy downstream bed. The high-quality data were acquired

158 by simultaneous imaging with three high-speed digital cameras (Canon EOS 70D) that covered the entire channel length and operated at fifty frames per second. All raw recorded videos had a resolution 159 160 of 1920×1080 pixels (Full HD/1080p). To create sufficient contrast for filming and avoid uncontrolled 161 lights and reflections, the surrounding laboratory was partly isolated using black curtains installed 162 behind the cameras. Windows were covered with thick dark plastic sheets, and a black curtain was 163 installed on opposite side of the flume's wall to mask objects behind it. Three video files were obtained 164 from the cameras after each experiment and transferred to the computer. Required parameters, including 165 water levels and sediment depths, were extracted by analysing the first 300 frames (6 s @ 50 fps).

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Table 1. List of the experimental scenarios investigated in the present study

# Scenarios	S ₀ (m)	$\frac{S_0}{h_0}(\%)$	O _r (m)	$rac{m{0}_r}{m{h}_0}(\%)$	# Scenarios	S ₀ (m)	$\frac{S_0}{h_0}(\%)$	O _r (m)	$rac{m{0}_r}{m{h}_0}(\%)$
1	Clear water	0	No obstacle	0	13	0.0175	58.3	No obstacle	0
2	Clear water	0	0.045	15	14	0.0175	58.3	0.045	15
3	Clear water	0	0.075	25	15	0.0175	58.3	0.075	25
4	0.03	10	No obstacle	0	16	0.2	66.7	No obstacle	0
5	0.03	10	0.045	15	17	0.2	66.7	0.045	15
6	0.03	10	0.075	25	18	0.2	66.7	0.075	25
7	0.075	25	No obstacle	0	19	0.22	73.3	No obstacle	0
8	0.075	25	0.045	15	20	0.22	73.3	0.045	15
9	0.075	25	0.075	25	21	0.22	73.3	0.075	25
10	0.15	50	No obstacle	0	22	0.24	80	No obstacle	0
11	0.15	50	0.045	15	23	0.24	80	0.045	15
12	0.15	50	0.075	25	24	0.24	80	0.075	25

Note: S_0 = Initial upstream sediment depth (m); O_r = Obstacle radius (m).

More than 10 measuring rulers with an accuracy of ± 1 mm were mounted vertically on the sides of 167 the flume, roughly 0.50 m apart along its length, and used to measure water levels and sediment depths 168 169 at any arbitrary point along the flume. Several rulers monitored by two adjacent cameras were employed as references to align the extracted photographs. Two striped rulers, each with an accuracy of ± 1 mm, 170 171 were pasted horizontally on the upper and lower portions of the lateral wall. The study evaluated 20 positions along the flume (Fig. 3): 0.00, 0.76, 1.02, 1.27, 1.37, 1.42, 1.47, 1.52, 1.57, 1.67, 1.77, 1.87, 172 173 2.42, 2.47, 2.52, 2.57, 2.62, 3.52, 4.52, and 5.52 m. Fifteen post-dam-break snaps were assessed: 0.04, 174 0.08, 0.12, 0.2, 0.3, 0.4, 0.6, 0.8, 1, 1.5, 2, 3, 4, 5, and 6 s. A total of 1080 video images (24 different 175 scenarios, 15 snap times and 3 cameras) were rigorously analysed. Image editing was required to obtain

adequate contrast and minimize interfering lights and reflections. Consequently, the sharpness,
brightness, contrast, and colour of the photos were adjusted to better identify the interfaces between air,
water, and sediment layers. This procedure was repeated for all images.



 ${}^{*}L_{i}$: Surveyed locations (sections) throughout the channel

Fig. 3. A graphic picture of the experimental channel; L1 to L20 are depth gauging locations

A non-disturbing procedure was consecutively employed for each video image via Grapher[®]. After 179 180 initiating the coordinates of at least two confirmed positions in each photograph on a diagonal line, clicking on any random spot would lead to a presentation of the coordinates of that spot on the x- and 181 y-axes. Hence, the development of water and sediment depths with time (h versus t) could be acquired 182 precisely from photographs for any arbitrary chosen spot, without any flow interruptions resulted from 183 184 experimental devices. The sediment depth and water level profiles along the flume could thus be 185 obtained at any time after the dam-break. Although this procedure was laborious, it led to high-quality and precise outcomes. Since two physical parameters were extracted from 20 locations along the flume, 186 187 all images comprised 14400 data points (2 parameters \times 20 locations \times 15 times \times 24 scenarios); these are available online in the public repository accompanying this study (Vosoughi et al. 2021a; b; c). The 188 practical purpose of performing this process was to accurately investigate the areas buried by the 189 sediment layer at specific times and snapshots (time-steps) after the dam-break. 190

To validate the experimental modelling records, a specific dam-break scenario was modelled both numerically and experimentally for various initial downstream bed conditions, including dry- and wetbeds (Vosoughi 2018). Outcomes were evaluated by comparison with results of previously published reports (Fig. 4) (Ozmen-Cagatay and Kocaman 2010). Fig. S2 in the Supplementary Material compares the experimental records quantitatively with experimental measurements from the literature (LaRocque et al. 2013). A set of experimental video images at 12 snap times after the failure of the dam (from 0 to 40 s) when the initial sediment depth in the reservoir was 0.22 m and a 0.075-m-tall obstacle was mounted on the downstream channel bottom is presented in the Supplementary Material (Fig. S5).



Fig. 4. Image-based comparison of dam-break shock waves side views h(x) at various time snaps: (a) available laboratory records (Ozmen-Cagatay and Kocaman 2010), (b) current laboratory records (Vosoughi 2018), and (c) OpenFOAM results (Vosoughi 2018). Unit of length is cm, and \bar{h} is the ratio of downstream initial water depth to initial upstream height of 0.3 m

199 NUMERICAL MODELLING

In the numerical modelling portion of the study, an open-source and license-free CFD
(computational fluid dynamics) package called OpenFOAM was employed (Open⊽FOAM 2015). This

software is the best-known and most frequently used free CFD package, which operates on the Linux kernel operating system. Its source code is easily expandable as it employs the object-oriented programming language, C⁺⁺ (Openfoamwiki 2020). As previously mentioned, numerical modelling concerning the effect of semi-circular obstacles on the multi-layer waves arising from a silted-up dambreak has not been performed to-date. For the presented study, the purpose of performing this numerical process was to verify the relative responsiveness of simple numerical models, which are also publicly available, to predict this complex phenomenon and experimental data.

209 Euler-Euler approach

210 The Euler-Euler approach is a dominant numerical method in OpenFOAM to model multi-layer 211 flows, in which each phase is mathematically treated as a continuum. Thus, these models are called 212 "multi-fluid models", which can appropriately demonstrate separated flows where each phase may be 213 categorized as a continuum. The Euler-Euler method may also be utilized to model discrete flows, where the full movement of phases is of interest rather than exploring a single phase. This approach is 214 215 particularly helpful when detecting the boundary between phases is preferred (Nilsson 2010). In order to specify a discrete phase as a continuum, the particles' volume fraction must be high; therefore, this 216 method is appropriate for modelling condensed flow. Additionally, since particles are spread and, yet, 217 defined as a continuous layer, conservation equations may be employed to model such layers 218 219 (Open∇FOAM 2015).

Once a silted-up flood propagates, the saturated sediment deposit might act similarly to a viscid fluid until it stops completely and the water layer flows smoothly over its top (Duarte et al. 2011). In this study, the saturated sediment phase was assumed to be a highly viscid fluid. The three Euler-Euler multiphase models in OpenFOAM (Open ∇ FOAM 2015) included the volume of fluid (VOF), Eulerian, and mixture models. The wave following the failure of a silted-up dam and how it propagates over downstream semi-circular obstacles was simulated using VOF and Eulerian models. It is pertinent to mention that these models were applied in this study as it was assumed that all phases were continuous.

227 Volume of fluid (VOF) model

228 The volume of fluid (VOF) model is a subset of the Euler-Euler approach, where each phase is 229 treated as a continuum. Although interpenetrating of the layers is not allowed, the purpose of this 230 method is to model non-miscible (layered) multi-fluids particularly when the interface position among 231 the fluids is significant. This method considers a particular group of equations of continuity and 232 momentum, which are resolved and shared for each flow layer, whilst the fluid volume fraction is 233 tracked in each of the cells within the computational domain. The VOF model can address a wide 234 spectrum of issues, such as free surface flows and dam-break waves. In this study, VOF simulations 235 were ran using the interFoam, and multiphaseInterFoam solvers.

In the VOF model, the properties used in the governing equations are defined for all phases in each of the control volumes. For instance, in a dual-phase model, if the second phase's volume fraction is being tracked, the density, ρ , for each of the cells is presented by (Torres et al. 2021):

239
$$\rho = \alpha_2 \rho_2 + (1 - \alpha_2) \rho_1$$
 (1)

240 where α_2 is the water fraction; and ρ_1 and ρ_2 are the densities of air and clear water, respectively.

Generally, for a *k*-phase model, the volume-fraction-averaged viscosity, μ_m , and the volumefraction-averaged density, ρ_m , take on the following forms (Barbosa et al. 2019; Wang et al. 2020b):

243
$$\mu_m = \sum_{i=1}^k \mu_i \alpha_i$$
(2)

244
$$\rho_m = \sum_{i=1}^k \rho_i \alpha_i \tag{3}$$

Then, the apparent viscosity, μ_m , and density, ρ_m , of multiphase silted-up flood waves are calculated as $\mu_m = \mu_1 \alpha_1 + \mu_2 \alpha_2 + \mu_3 \alpha_3$ and $\rho_m = \rho_1 \alpha_1 + \rho_2 \alpha_2 + \rho_3 \alpha_3$, in which, μ_1 , μ_2 and μ_3 are the viscosities and ρ_1 , ρ_2 and ρ_3 are the densities of air, clear water, and saturated sediment layer, respectively. Each phase fraction, α_k , is also defined in relation to the other phase fractions, whereby the sum of all volume fractions should be equal to 1 (Wang et al. 2020b):

$$250 \qquad \sum_{i=1}^{k} \alpha_i = 1 \tag{4}$$

In this study, the air fraction, α_1 is defined in relation to the water fraction, α_2 , and saturated sediment layer fraction, α_3 , while $\alpha_1 + \alpha_2 + \alpha_3 = 1$.

The three-phase flood wave equations solved in the VOF method for isothermal and incompressible flow are presented below as a group equation of continuity and momentum (Barbosa et al. 2019; Miliani et al. 2021; Panda et al. 2017; Torres et al. 2021; Wang et al. 2020a; b):

256
$$\frac{\partial \rho_m}{\partial t} + \nabla \cdot (\rho_m \mathbf{U}) = 0$$
(5)

257
$$\frac{\partial \rho_m \mathbf{U}}{\partial t} + \nabla \cdot (\rho_m \mathbf{U} \mathbf{U}) = -\nabla \mathbf{P} + \nabla \cdot \boldsymbol{\tau} + \rho_m \mathbf{g} + \mathbf{S} = 0$$
(6)

where ρ_m represents the volume-fraction-averaged density; **U** is the velocity; **g** is the "gravitational acceleration"; τ denotes the "viscous stress tensor"; **P** is pressure; and **S** is the force due to the "surface tension". The "viscous stress tensor", τ , is also described as (Barbosa et al. 2019; Wang et al. 2020b):

261
$$\boldsymbol{\tau} = \mu_m [(\nabla \mathbf{U}) + (\nabla \mathbf{U})^{\mathrm{T}}]$$
(7)

where ∇U denotes the gradient of the velocity. In Cartesian coordinates, ∇U is the Jacobian matrix, and (∇U)^T is the transpose of the gradient ∇U (Wang et al. 2020a). In OpenFOAM, there are two surface tension models: the "continuum surface force" (CSF) and "continuum surface stress" (CSS). In the CSF, the nonconservative form of the surface tension force, **S**, may be described as (Wang et al. 2020b):

$$266 \qquad \mathbf{S} = \sigma K \nabla \alpha \tag{8}$$

267 where σ is the "surface tension constant"; α represents the volume fraction of the fluid; and *K* is the 268 "curvature of the surface", given by (Wang et al. 2020b):

269
$$K = -\nabla \left(\frac{\nabla \alpha_k}{|\nabla \alpha_k|} \right)$$
(9)

where $\nabla \alpha = \hat{n}$ is the vector normal to the interface (see Eq. 17); and the surface tension constant, σ , is set to be a constant (0.07 *N*/m) for all phases (Table 2). Also, considering α_k as a function of time in order to approximate the interphases' position, the transport equation for α_k must be solved:

273
$$\frac{\partial \alpha_k}{\partial t} + \nabla \cdot (\alpha_k \mathbf{U}) = 0$$
(10)

OpenFOAM applies the interface capturing technique (Weller 2008) by introducing an additional compressive term in Eq. (10). The extended transport equation for the volume fraction α_k used in *multiphaseInterFoam* solver may be described as:

277
$$\frac{\partial \alpha_k}{\partial t} + \nabla \cdot (\mathbf{U}\alpha_k) + \nabla \cdot [\mathbf{U}_r \alpha_k (1 - \alpha_k)] = 0$$
(11)

where the relative velocity, \mathbf{U}_r , is employed in the interface to compress the "volume fraction" area and keep the interface sharp (Wang et al. 2020b); and $\alpha_k(1 - \alpha_k)$ is a nonzero term that guarantees that the compression term is effective in the interface area. \mathbf{U}_r , is also presented by (Barbosa et al. 2019):

281
$$\mathbf{U}_{r} = min(C_{\alpha}|\mathbf{U}|, max(|\mathbf{U}|)) \frac{\nabla \alpha}{|\nabla \alpha|}$$
(12)

where the compressibility coefficient, C_{α} , is applied to control interfacial compression. The *min* operator is locally operated on each cell's face, and the *max* operator is globally operated in the entire domain. The $\nabla \alpha / |\nabla \alpha|$ adds the interface unit vector normal to the direction in which \mathbf{U}_r is applied. Since C_{α} can be any amount ≥ 0 , if $C_{\alpha} \leq 1$, then Eq. (12) becomes (Barbosa et al. 2019):

286
$$\mathbf{U}_r = C_\alpha |\mathbf{U}| \frac{\nabla \alpha}{|\nabla \alpha|}$$
(13)

where C_{α} in the *multiphaseInterFoam* solver simplifies to a binary coefficient that shifts to 1 for interface sharpening "on" and 0 for "off".

289 Eulerian model

290 The most complicated multi-layer model in OpenFOAM is the Eulerian model, where each phase is considered as an interpenetrating layer, and a set of k continuity and momentum equations is resolved 291 292 separately for each phase. The model's computational time is, therefore, much longer than that of VOF, 293 but a specific pressure is allocated by all phases. This model is particularly applicable to flows where 294 fluid boundaries may mix together (interpenetrate) through the process, e.g., multiphase fluids with 295 miscible boundaries. The Eulerian multi-layer method in OpenFOAM enables the modelling of several distinct, yet, interpenetrating layers. The layers may be solids, gases, and liquids in each combination. 296 297 In this study, such simulations were done using the highly efficient solver *multiphaseEulerFoam*. The 298 multiphase flow equations for *k* continuous phases solved in the Eulerian model are shown below as a 299 group of continuity and momentum equations (Fluent 2013; Open ∇ FOAM 2015; Wang et al. 2020b):

$$300 \quad \frac{\partial \alpha_k \rho_k}{\partial t} + \nabla \cdot (\alpha_k \rho_k \mathbf{U}_k) = 0 \tag{14}$$

301
$$\frac{\partial \alpha_k \rho_k \mathbf{U}_k}{\partial t} + \nabla \cdot (\alpha_k \rho_k \mathbf{U}_k \mathbf{U}_k) = -\alpha_k \nabla \mathbf{p} + \nabla \cdot \boldsymbol{\tau}_k + \alpha_k \rho_k \mathbf{g}_k + \mathbf{S}_k = 0$$
(15)

302 where \mathbf{U}_k is the mean velocity field; subscript *k* refers to the k^{th} continuous phase; **p** is the mean 303 pressure; and $\boldsymbol{\tau}_k$ is the k^{th} phase stress tensor, given by (Barbosa et al. 2019):

304
$$\boldsymbol{\tau}_k = \alpha_k \mu_k [(\nabla \mathbf{U}_k) + (\nabla \mathbf{U}_k)^{\mathrm{T}}]$$
(16)

The *multiphaseEulerFoam* solver applies additional limits called "Multidimensional Universal Limiter with Explicit Solution" (MULES) on the result of the phase transport equations to guarantee the phase conservation against the boundedness in the results of hyperbolic problems. (Nilsson 2010). Theoretical details of MULES (Section S2) and comprehensive aspects of the OpenFOAM setup (Section S13) are provided in the Supplementary Materials.

310 Initial and boundary conditions, and computational domains

311 Owing to the experimental flume dimensions, the computational area was 6-m long, 0.32-m deep, 312 and 0.3-m wide. Two semi-circular obstacles with 0.045 and 0.075-m radii were specified and 313 positioned 1 m downstream of the dam section. The silted-up flood wave was modelled as a three-phase incompressible system (air-water-sediment layer) using VOF and Eulerian methods, including the 314 influence of kinematic viscosity, density, and surface tension. The simulation input data are given in 315 Table 2. A sloping bed may lead to an increase or decrease in flood wave propagation (Dias and Dutykh 316 2007), which can be affected by parameters, such as bed roughness (Bocchiola et al. 2006). To keep the 317 numerical models as simple as possible, flume and obstacle sides in connection with the flood wave 318 were assumed to be smooth, and a horizontal bed was used. However, the influence of such factors on 319 320 silted-up dam-break flood waves require further exploration.

321 Under the initial conditions, the experimental reservoir (1.52-m long, 0.3-m wide, and 0.3-m deep)
322 was filled to the required level with a saturated sediment deposit. The remainder of the reservoir was

filled by sediment-free water, and everything above was deemed air. To define boundary conditions, as there was no lateral inflow, the beginning of the flume, bottom, and side boundaries were chosen as the "*wall functions*". The static contact angle at the walls was set to 90° for all combinations of mixtures in order to avoid the use of the surface tension force between the wall and fluid. The normal vector, \hat{n} , to the interface of the wall can be described as (Open ∇ FOAM 2015):

$$328 \qquad \hat{n} = n_w \cos(\theta_{eq}) - n_t \sin(\theta_{eq}) \tag{17}$$

where n_w is the unit vector pointing towards the wall; θ_{eq} is the static contact angle set to 90°; and n_t is the unit vector tangential to the wall pointing toward the fluid. The interface of the fluid is then, in fact, normal to the wall. If θ_{eq} is less than 90°, this would indicate that the fluid wets the wall. The downstream endpoint of the experimental flume was set as a "*pressure outlet*", and the flume's upper edge was selected as a "*pressure inlet*" considering atmospheric pressure. There was no set contact angle since the fluids should never come in contact with this region. Hence, when the simulation was initiated, the gravitational force led to sudden movement of reservoir's content.

3	3	6	
3	3	6	

Table 2. The simulation input data

	Units	Name in OpenFOAM	Air	Water	Saturated packed sediment layer	
Kinematic viscosity	$m^2 s^{-1}$	nu	1.48×10^{-5}	$1.0 imes 10^{-6}$	6.27×10^{-2}	
Density	$kg m^{-3}$	rho	1.0	$1.0 imes 10^3$	$2.08\times\mathbf{10^{3}}$	
Note: Surface tension or sigma in OpenFOAM was set at 0.07 ($N m^{-1}$).						

337 *Computational meshes and time steps*

In this study, 8 mesh sizes (30, 25, 20, 15, 10, 5, 3.3, and 2.5 mm) were adopted to analyse the results. Considering the error values and runtimes, rectangular cube cells with a length, width, and depth of 0.005 m were designated. Hence, the resulting 3D solution domain was discretized into a total of 4.6 million cube cells. A finer variable mesh size (up to 2 mm) was applied as it approached the obstacle's crest at an interval of 0.1 m before and after the obstacle to better simulate that region. After rigorously analysing several distinct time steps (0.01, 0.005, 0.001, and 0.0005 s), a constant time step of 0.001 s was adopted due to the error values, runtime, and the courant number. Comprehensive details of timestep and mesh size analyses are provided in the Supplementary Materials (Section S14).

In order to validate the experimental records and OpenFOAM predictions, a specific dam-break 346 scenario was modelled both numerically and experimentally with various downstream hydraulic 347 conditions: initially dry or wet downstream (Vosoughi 2018). Results were evaluated through 348 comparison with an experimental study (Ozmen-Cagatay and Kocaman 2010). Accordingly, Fig. 4, 349 350 depicts a group of photograph-based comparisons at several snap-times following the failure of the dam, to visually assess the outcomes of the current research compared to other research results. Figs. S3 and 351 S4 (see Supplementary Materials) compare the numerical predictions of OpenFOAM both visually and 352 quantitatively with available experimental measurements (LaRocque et al. 2013). A group of VOF 353 354 replication results at a reservoir initial sediment height of 0.015 m and with an obstacle radius of 0.045 355 m located downstream is described in the Supplementary Materials (Fig. S7).

356 **RESULTS**

357 *Experimental results*

358 Fig. 5 displays a set of experimental images that can serve as a visual comparison of sediment depth 359 and free surface water level profiles for different initial reservoir sediment depths. All images were extracted from two specific time snaps, 0.5 and 0.8 s after dam failure, in the presence of a downstream 360 semi-circular obstacle with a radius of 0.045 m. As the reservoir sediment layer height increased, the 361 362 flood wave propagated more slowly. For instance, for the water-filled reservoir (sediment-free) at 0.5 s 363 after the dam-break, the flood wave had already hit and passed over the obstacle by about 0.8 m; however, with initial reservoir sediment layer heights of 0.22 and 0.24 m, the wave had not even reached 364 365 the obstacle. The wave's tip was thrown up and forward after it hit the obstacle, and the sediment layer 366 stretched and dampened as it advanced downstream. A further set of experimental video images was classified for all different upstream sediment depths and a semi-circular obstacle of radius 0.075 m, 367 368 which is presented in the Supplementary Materials (Fig. S6).



 $*S_0$: Initial upstream sediment depth (m)

Fig. 5. A visual comparison of experimental images at 0.5 s (a) and 0.8 s (b) after dam break, for 8 different initial upstream sediment depths (S₀); 0, 0.03, 0.075, 0.15, 0.175, 0.2, 0.22 and 0.24 m, when a semi-circular obstacle with radius 0.045 m is located downstream. A vertical line represents the gate section

Figures 6a-f present six sets of ternary images taken 6, 5, 4, 3, 2, and 1 s after the dam-break at six

distinct upstream sediment depths (0, 0.03, 0.075, 0.15, 0.2 and 0.24 m). Three different downstream
conditions were evaluated: no obstacle (top image), obstacle with a radius of 0.045 m (middle image)
and obstacle with a radius 0.075 m (bottom image). Figs. 6a-c show that the water level dropped
significantly after passing the obstacle, compared to the water level in the absence of an obstacle.
Although the larger obstacle led to a shallower flood downstream, the flood wave before the obstacle
was proportionately deeper (Figs. 6a-d). As the downstream obstacle increased in height, the dam-break
wave propagated more slowly, and the front wave celerity subsequently decreased (Fig. 6f).



* S_0 : Initial upstream sediment depth (m); **t : The time after dam break (s); *** O_r : The obstacle's radius (m)

Fig. 6. Six sets of ternary images, each showing 3 different downstream conditions; absence of obstacle, presence of semi-circular obstacle with radius of 0.045 m and 0.075 m. For different times of 6, 5, 4, 3, 2, and 1 s after dam-break and upstream sediment depths of 0, 0.03, 0.075, 0.15, 0.2 and 0.24 m respectively (a-f). A vertical line represents dam section

377 Using video images, front wave celerity values were carefully measured at four intervals, each 1 m in length, along the flume portion downstream from the dam. The first downstream interval ranged 378 1.52-2.52 m from the beginning point of the reservoir, and the other intervals were 2.52-3.52, 3.52-379 380 4.52, and 4.52-5.52 m. The values of front wave celerity in the mentioned intervals are classified in 381 Tables S2-S4, one for each of downstream condition, in Section S7 of the Supplementary Materials, 382 with additional technical details. The average computed dam-break front wave celerity along the 383 downstream channel for the 24 different scenarios are presented in Table 3.

384

Table 3. Average computed front wave celerity through the channel (m/s)

Average front wave celerity (m/s)							
Initial depth of	Downstream initial condition						
sediment in the reservoir (m)	No obstacle	Obstacle with 0.045 m radius	Obstacle with 0.075 m radius				
0	2.32	2.13	2.10				
VAR	0.01	0.01	0.02				
0.03	2.26	2.08	2.01				
VAR	0.01	0.02	0.03				
0.075	2.17	1.94	1.90				
VAR	0.01	0.02	0.04				
0.15	2.04	1.70	1.65				
VAR	0.01	0.06	0.08				
0.175	1.92	1.60	1.53				
VAR	0.01	0.08	0.10				
0.20	1.75	1.52	1.42				
VAR	0.03	0.08	0.11				
0.22	1.65	1.42	1.35				
VAR	0.02	0.06	0.09				
0.24	1.28	1.20	1.03				
VAR	0.04	0.06	0.10				

Note: VAR = Variance value (m^2/s^2) .

385 Based on Table 3, the initial depth of reservoir sediment strongly influenced wave celerity: the greater the initial reservoir sediment depth, the slower the shock wave progression. Lower water depths 386 on top of the sediment coat led to a decrease in celerity of the front wave. The presence of a downstream 387 388 obstacle also led to a reduction in multiphase wave celerity once the shock wave hit the obstacle, where 389 the taller obstacle reduced the front wave celerity more than the shorter obstacle. In all scenarios, the 390 mean front wave celerity values caused by the dam-break along the flume varied from 1 to 2.3 m/s, depending on the upstream and downstream initial hydraulic conditions. The variances of all average 391

celerity values are presented in Table 3 (VAR line). The computed variances were minor and fluctuated between 0.01 and 0.1 m^2/s^2 . The maximum variance occurred in the scenarios where the flood depth suddenly dropped due to the presence of a downstream obstacle, resulting in a noticeable decrease in wave celerity.

396 Comparison of experimental measurements and numerical results

As described in the Experimental Modelling section, a total of 20 positions along the channel and 15 time-snaps following dam-break were selected to obtain the required data. A short distance between two adjacent locations along the dam was set to capture the sudden depth changes and high turbulence in that region. Once the dam-break occurred, the intervals between time snaps were brief and then increased with time.

402 Flow pattern comparison

Image comparisons provided in this section and the Supplementary Materials (Section S8) visually illustrate the experimental and numerical conditions. The images were depicted below each other for 8 different times (0, 0.1, 0.2, 0.3, 0.4, 0.6, 0.8, and 1 s) after the dam-break. A channel section about 2.2 m in length was covered by the images (1.32 to 3.52 m from the beginning point of the reservoir). Fig. 7 depicts an image comparison when the reservoir initial sediment height was 0.075 m and a semicircular obstacle with a radius of 0.075 m was mounted downstream. Experimental images and VOF and Eulerian predictions are depicted below each other at the appropriate and comparable positions.

410 As can be seen from Figs. 7g-i, at 0.2 s, the flood wave reached 0.5 m downstream from the dam 411 and the water level dropped about 7 cm at the dam section. At 0.8 and 1 s, the sediment coat had 412 progressed about 13 cm downstream, and the sediment depth at the dam section decreased about 3 cm 413 (Figs. 7s and v). For the VOF vs Eulerian predictions at 0.8 and 1 s, it is evident that the amount of 414 sediment movement downstream and its depth at the dam section were similar. Although experimental 415 records and both numerical results were in good agreement, the Eulerian method seemed to be more 416 accurate in simulating this situation. Fig. S10 compares a set of experimental images to VOF results for 417 a case with a water-filled reservoir (sediment-free) and a semi-circular obstacle of radius 0.045 m 418 located downstream from the dam. Fig. S11 shows a similar comparison when the reservoir initial419 sediment height was 0.03 m.



Fig. 7. Image-based comparison of experimental records (a, d, g, j, m, p, s & v) versus VOF (b, e, h, k, n, q, t & w) and Eulerian results (c, f, i, l, o, r, u & x) indicating sediment depth and water level profiles, at various time snaps: 0 (a, b & c), 0.1 (d, e & f), 0.2 (g, h & i), 0.3 (j, k & l), 0.4 (m, n & o), 0.6 (p, q & r), 0.8 (s, t & u) and 1 (v, w & x) seconds. The reservoir initial sediment depth was 0.075 m and a semi-circular obstacle with radius of 0.075 m is mounted downstream from the dam. The vertical line represents the dam section

420 Sediment depth and free surface water level profiles

A selection from the large number of sediment depth and water level profiles based on data extracted from video images is presented in this section to evaluate the influence of downstream semi-circular obstacles on the multiphase flood wave propagation. All graphs represent both measured data (points) and numerical predictions (lines). The $h_t/h_0(-)$ ratio represents the nondimensional water level, where h_t is the height of the water at a particular time along the channel and h_0 is the initial reservoir water 426 height (0.3 m in all cases). The ratio $S_t/S_0(-)$ is the nondimensional sediment depth, where S_t is the 427 sediment depth at a particular time along the flume and S_0 is the initial upstream sediment depth.

428 Fig. 8 depicts the experimental vs VOF results in estimating the free surface water profile along the channel when the reservoir was filled with sediment-free water. Six distinct times after the dam-break 429 430 are illustrated in Fig. 8: early times (0.04 and 0.2 s) and later times (0.4, 1, 2 and 6 s). Two different 431 semi-circular obstacles with a radius of 0.045 m (a and c) or 0.075 m (b and d) were located 1 m 432 downstream from the dam. The wave generated by the dam-break created a huge bulge after hitting the obstacle and passing over it. The taller the obstacle, the larger the bulge created in the flood wave and, 433 434 consequently, the shallower the flood after the obstacle (Figs. 8c and d). Moreover, it seems that smaller 435 changes occurred immediately after the dam-break (Figs. 8a and b). Considering the lack of significant 436 statistical error values, there was a strong concurrence between the experimental and VOF results. The 437 highest Mean Absolute Error (MAE) and Root Mean Square Error (RMSE) values were 0.009 and 0.012 m, respectively, which were negligible relative to $h_0 = 0.3$ m. 438

439 Figures 9 shows the VOF (a and c) and Eulerian (b and d) predictions vs experimental measurements 440 at three time-snaps following the dam-break: 0.4, 2 and 6 s. Figure 9 also compares VOF (a) and 441 Eulerian (b) results in determining the free surface water level profile when the initial sediment height in the reservoir was 0.15 m and a semi-circular obstacle with a radius of 0.045 m was mounted 442 443 downstream. Both numerical methods and measured data were in agreement. The highest MAE and RMSE occurred for VOF results with values of 0.0174 and 0.026 m, respectively, and were very low 444 445 compared to $h_0 = 0.3$ m. Considering the values of statistical error indices, the Eulerian showed better 446 concurrence with measured data than the VOF method. As can be seen, at 2 s, the water level increased sharply at the downstream obstacle location, then suddenly dropped after it, which was predicted well 447 448 by both VOF and Eulerian methods.

An evaluation of the numerical outcomes in matching the measured sediment depth profile (Figs. 9c and d) for a reservoir initial sediment depth of 0.2 m and a semi-circular obstacle with radius 0.075 m mounted downstream showed the Eulerian method (max. RMSE = 0.0307 m and max. MAE = 0.0179 m) outperformed VOF (max. RMSE = 0.0366 m and max. MAE = 0.0228 m). Assuming the reservoir sediment coat to be a viscid fluid in numerical modelling, the outcomes were plausible. VOF predictions
indicated that, 6 s after the dam failure, the sediment layer had reached the obstacle and accumulated
behind it (Fig. 9c). In comparison, the Eulerian predictions suggested that the sediment layer had
reached a position just slightly before the obstacle (Fig. 9d.)



Fig. 8. Laboratory records vs VOF estimations in determining the water level profiles at distinct times; (a & b) 0.04 and 0.2 s, (c & d) 0.4, 1, 2 and 6 s. The reservoir was filled by sediment-free water and a semi-circular obstacle with a radius of 0.045 m (a & c) or 0.075 m (b & d) was mounted downstream from the dam. Dashed lines represent dam and downstream obstacle sections, respectively. $h_t/h_0(-)$ is nondimensional water level along the flume, where $h_0 = 0.3 m$

In general, comparisons with measured data demonstrate better Eulerian performances than VOF, particularly in simulating a silted-up dam-break wave for a highly-silted reservoir and in modelling multiphase flood wave propagation over a bumpy bed. Despite its better prediction accuracy, the 460 Eulerian approach suffers from longer computational times and more complex simulation conditions,



461 as shown in Table S6 (run times) in the Supplementary Materials (Section S11).

Fig. 9. Experimental measurements *vs.* both VOF (a & c) and Eulerian predictions (b & d) in determining profiles of water level (a & b) and sediment depth (c & d) at various time snaps of 0.4, 2 and 6 s. Reservoir initial sediment depth is 0.15 m (a & b) or 0.2 m (c & d). A semi-circular obstacle with radius of 0.045 m (a & b) or 0.075 m (c & d) is mounted downstream from the dam. Dashed lines represent dam and downstream obstacle sections, respectively. $h_t/h_0(-)$ and $S_t/S_0(-)$ are nondimensional water level and sediment depth along the flume and $h_0 = 0.3 m$

Table 4 compares the RMSE and MAE values of the prediction of free surface water level profiles 462 under all various initial upstream and downstream conditions and at four time-snaps after the dam-break 463 (0.4, 1, 2, and 6 s). The highest RMSE and MAE were found using the VOF method when the reservoir 464 initial sediment depth was 0.22 m. The table illustrates that the greater the reservoir initial sediment 465 466 height, the higher the reported error values. Assuming the sediment layer to be a viscous fluid played a major role in increasing the error values due to an increase in the upstream sediment depth. However, 467 both numerical methods had good performances in predicting more complicated downstream-bed 468 hydraulic conditions. According to Table 4, the reported error values of the Eulerian method were 469

smaller in most scenarios, and there was a higher visual concurrence between the experimental measurements and Eulerian results than those of VOF. Additional error values of VOF and Eulerian outcomes in estimating sediment depths are shown in Table S5 in the Supplementary Materials. Based on Tables 4 and S5, it can be concluded that the Eulerian results were more accurate and better matched the recorded data than VOF in estimating sediment depth and water level profiles, especially when more than half of the reservoir depth was initially filled by sediment (≥ 0.15 m).

476 Table 4. The statistical error values in estimating free surface water level profiles via VOF and Eulerian numerical methods computed using four different times after the dam break; 0.4, 1, 2 and 6 s

Downstream	Numerical	Statistical error indices	Upstream sediment depth (m)							
conditions	methods		0.00	0.03	0.075	0.15	0.175	0.2	0.22	0.24
	VOE	RMSE (m)	0.0035	0.0131	0.0094	0.0315	0.0320	0.0381	0.0411	0.0403
No	VOF	MAE (m)	0.0028	0.0099	0.0069	0.0228	0.0231	0.0276	0.0305	0.0293
obstacle	P 1	RMSE (m)	_	0.0085	0.0087	0.0234	0.0284	0.0357	0.0345	0.0387
	Eulerian	MAE (m)	_	0.0073	0.0064	0.0166	0.0195	0.0234	0.0239	0.0282
	VOF	RMSE (m)	0.011	0.0099	0.0108	0.0260	0.0291	0.0339	0.0373	0.0372
		MAE (m)	0.009	0.0073	0.0078	0.0174	0.0200	0.0223	0.0261	0.0271
radius of 0.045 m	045 m Eulerian	RMSE (m)	_	0.0084	0.0098	0.0204	0.0279	0.0295	0.0346	0.0360
		MAE (m)	_	0.0063	0.0068	0.0123	0.0164	0.0179	0.0216	0.0247
	VOE	RMSE (m)	0.0104	0.0076	0.0111	0.0228	0.0253	0.0287	0.0360	0.0387
	VOF	MAE (m)	0.0081	0.0060	0.0081	0.0149	0.0168	0.0193	0.0253	0.0279
radius of 0.075 m	s of 0.075 m Eulerian	RMSE (m)	_	0.0073	0.0099	0.0183	0.0244	0.0251	0.0345	0.0360
		MAE (m)	_	0.0051	0.0067	0.0122	0.0164	0.0170	0.0211	0.0244

Note: RMSE = Root Mean Square Error; MAE = Mean Absolute Error.

478 *Sediment depth and water level variations over time*

Sediment depth and water level variations after a dam-break event were investigated at three control
points along the flume (0.76, 1.52 and 2.52 m from the reservoir's beginning point). A schematic 3D
view of the flume with these control points is depicted in the Supplementary Materials (Fig. S12).
Figures 10a and b present the comparisons of measured data and VOF results in estimating water surface
changes by elapsing time after a dam-break event when a semi-circular obstacle with a radius of 0.045
m (a) or 0.075 m (b) was positioned downstream of the dam.

The VOF predictions and measured data fit well, and the highest MAE and RMSE values were 0.007 and 0.0109 m, respectively. The values varied from 2.2% to 3.6% for $h_0 = 0.3$ m. As shown in Fig. 10a and b, the error indices increased as the downstream semi-circular obstacle became taller. At the first 488 control point in the middle of the reservoir (0.76 m), the water level dropped slowly until 4 s and then 489 increased due to a negative wave generated by the downstream obstacle. The water surface at the second 490 control point (dam location) dropped rapidly once the dam-break occurred then decreased slowly until 491 the negative wave developed. Fig. 10a and b show that the higher the obstacle, the deeper and faster the 492 negative wave was generated. At the third control point (obstacle section), the water level increased 493 until 2 s and then decreased slowly and steadily. The maximum water level at the third control point 494 was 0.15 m when a 0.045-m tall obstacle was mounted in the downstream bed and was 0.175 m for a 495 0.075-m tall obstacle.

496 Figures 10c-f depict the sediment depth and water level variations over elapsed time after dam failure at the three control points along the flume using measured VOF (c and e) and Eulerian estimation (d 497 498 and f) data. As illustrated in Figures 10c and d, the initial height of the sediment layer in the upstream 499 reservoir was 0.175 m, and a downstream obstacle had a radius of 0.045 m. Reservoir sediment with an 500 initial height of 0.24 m and obstacle with a radius of 0.075 m are presented in Figs. 10e and f, 501 respectively. According to Figures 10c-f, VOF and Eulerian estimates were in adequate agreement with recorded data. The highest MAE and RMSE were 0.0246 and 0.0351 m, respectively, for the VOF and 502 503 were improved upon under the Eulerian approach (0.0304 and 0.0208 m). As the initial upstream 504 sediment became deeper, the statistical error indices increased. The nondimensional parameter of $\frac{y_t}{y_0}$ (-), which is presented on the vertical axes in Figs. 10c-f, represents both h_t/h_0 (-) and S_t/S_0 (-). 505

At the first control point (0.76 m) in Figs. 10c and d, the water level decreased slowly after the dambreak, and the sediment coat transformed insignificantly. However, at the dam section (second control point), the sediment depth and water level changed rapidly immediately after the failure of the dam and then decreased slowly. The water level at the third control point (downstream) increased until 2 s then decreased slowly. For the 80% silted-up reservoir (Figs. 10e and f), all analyses were similar to those in Figures 10c and d. However, at 3 s, the water level increased then decreased again under the influence of the negative wave due to the downstream obstacle.



Fig. 10. A comparison of experimental measurements with VOF (a, b, c & e) and Eulerian results (d & f) in estimating sediment depth and water level variations over elapsed time at 3 control points along the flume; 0.76 m (the reservoir mid-point), 1.52 m (gate section) and 2.52 m (obstacle section). Initial height of sediment in reservoir is 0.00 m (a & b), 0.175 m (c & d) or 0.24 m (e & f), and a semi-circular obstacle with radius of 0.045 m (a, c & d) or 0.075 m (b, e & f) is mounted downstream from the dam. The nondimensional parameter of y_t/y_0 (–) at the vertical axes of figures c, d, e and f, represents both h_t/h_0 (–) and S_t/S_0 (–). $h_0 = 0.3 m$

513 Correlation analysis of measured data and numerical predictions

514 Figure 11 depicts the correlation between laboratory data and numerical outcomes by VOF (a and

b) and Eulerian methods (c) using the Coefficient of Determination (R^2) as a correlation index. The

516 horizontal axes represent experimental data, while the vertical axes depict numerical results in determining water level values at 20 positions in the flume at 7 time-snaps. Fig. 11a presents the case 517 518 where the reservoir was filled by sediment-free water, and a 0.075 m radius obstacle was mounted dowstream from the dam. Here, the VOF results were highly correlated with measured data (R^2 = 519 520 0.9851). The correlation between laboratory records with VOF (Fig. 11b) and Eulerian (Fig. 11c) 521 results, when the initial height of reservoir sediment was 0.15 m and the obstacle had a radius of 0.045 m, indicated that both VOF and Eulerian predictions were highly correlated with measured data. R^2 522 values were 0.9402 and 0.9631, respectively, indicating that the Eulerian approach provided a closer 523 match than the VOF method. The opportunity of mixing the boundaries between layers in the Eulerian 524 525 method might have explained its better outcome.



Fig. 11. Correlation analyses of experimental measurements and VOF (a & b) or Eulerian results (c) for different upstream and downstream conditions; (a) the upstream channel is filled up by sediment-free water with a 0.045-m-high downstream obstacle, (b & c) the upstream initial sediment height is 0.15 m with a 0.075-m-high downstream

526 Run time analysis

A comparison of the required run times between the VOF and Eulerian approaches for all 24 scenarios are shown in Table S6 in the Supplementary Materials (Section S11). For VOF simulations, run times ranged from 5.96 to 31.42 h using a PC notebook with an Intel Core i5-4200U 2.3 GHz, 6 GB RAM, 64-bit processing system for a modelling duration of 10 s. For Eulerian simulations, run times ranged from 13.02 to 52.02 h, which are far longer than those of VOF (Table S6). Hence, the VOF method may be more attractive for wide-scale computational domains considering its simulation simplicity and less computational effort or time compared to the Eulerian approach.

534 CONCLUSIONS

535 Upon a dam's failure, the influence of the massive movement of sediment deposited behind the dam caused by a sudden dam-break flood wave is of great importance. Evaluating the effect of a downstream 536 semi-circular obstacle on such a complex phenomenon is vital as it leads to a better technical and 537 practical understanding of the effect of sudden variations in topography in flood-prone areas. As far as 538 we are aware, this topic has never been examined, either experimentally or numerically, in prior 539 540 research. In this study, the influences of the presence or absence of downstream humps (semi-circular obstacles) on multiphase shock flood waves, caused by the failure of dams with different levels of 541 reservoir silting, were investigated experimentally and verified numerically for a total of 24 dam-break 542 scenarios. The multiphase flood shock wave was recorded by high-speed digital cameras positioned 543 544 alongside the flume. Sediment layer depths, free surface water levels, and front wave celerity values at various locations and times were extracted by means of image processing. For this purpose, 20 distinct 545 546 positions along the channel and 15 time-snaps following the dam-break were examined. This multiphase 547 complex flood wave over a downstream obstacle was simulated by OpenFOAM using two numerical methods: VOF and Eulerian. Numerical results were rigorously compared with measured data. 548

Numerical predictions were in close agreement with measured data, with statistical error indices varying between 0.003 and 0.041 m. The lack of leakage from the edges of the gate, its rapid time of release (0.08-0.16 s), and good-quality recording may contribute to this agreement. The Eulerian approach offered better (3% to 25%) performances than the VOF, particularly for scenarios with deep initial sediment coats ($S_d \ge 0.15$ m). The possibility of simulating the mixing of boundaries between phases under the Eulerian approach may explain its better results. However, the Eulerian method required computational times that were 2-fold greater than the VOF method (Table S6).

556 Upstream sediment depth was a highly influential factor with respect to celerity of the flood wave. 557 The deeper the initial sediment coat, the more gently the shock wave progressed, most likely because 558 of the difference between the faster water velocity and slower sediment layer propagation velocity. 559 However, as the initial sediment coat became deeper, the sediment coat moved forward more rapidly after the dam-break, and its depth increased proportionally in the downstream area. This may intensifythe burial risk of infrastructure located downstream of the dam.

Bumpy downstream reaches in a natural terrain or the artificial creation of such conditions at a 562 specified distance in the downstream bed may extensively affect the physical characteristics of the dam-563 break flood wave. Such conditions can lead to a significant reduction in shock wave celerity, sediment 564 layer propagation and flood depth downstream of the obstacle. Considering all scenarios, the mean front 565 566 wave celerity varied between 1.0 and 2.3 m/s (Table 3). As the front wave celerity decreased, the destructive power of the flood decreased accordingly. The presence of a downstream obstacle led to 567 reductions in front wave celerity, and taller downstream obstacles reduced celerity to a greater extent 568 than shorter obstacles. Thus, different upstream and downstream conditions can change the front wave 569 570 celerity by up to 230%. However, the area between the dam and obstacle location may be the most 571 hazardous and insecure zone after the dam-break, as this is where the deepest sediment layer as well as 572 the highest water level are located. Therefore, it is highly inappropriate to position and maintain any 573 expensive equipment or infrastructure or to construct any office or residential buildings in this area.

In conclusion, the Eulerian method, despite its more accurate predictions, has drawbacks, such as longer computation time and more complicated modelling conditions. Accordingly, the VOF method, given its comparative simulation simplicity and lesser computational needs and time, may be more attractive for wide-scale computational domains. It is noteworthy that collections of original data are accessible online in the public repository accompanying this article (Vosoughi et al. 2021a; b; c).

A key component in upcoming research to explore the effects of upstream sediment on flood propagation would be to include distinct kinds of sediments using different grain sizes or consider suspended and bed load in a saturated sediment layer. It is suggested that future research assess the application of expert systems on estimating such phenomena. Comparing the potential effects of different obstacle shapes on multi-layer shock flood wave propagation would also be a valuable part of future studies. Moreover, simulating the upstream sediment coat as mixtures of particles and water could prove to be important.

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586 SUPPLEMENTARY MATERIAL

587 See <u>Supplementary Material</u> for the complete details of the study.

588 DECLARATION OF INTERESTS

- 589 The authors declare that they have no known competing financial interests or personal
- relationships that could have appeared to influence the work reported in this paper.

591 DATA AVAILABILITY STATEMENT

- All data, models, and codes generated or used during the study are available online in a public
- repository or appear in the submitted article (Vosoughi et al. 2021a; b; c). DOIs:
- 594 1- <u>https://doi.org/10.6084/m9.figshare.13686142</u>
- 595 2- <u>https://doi.org/10.6084/m9.figshare.13686205</u>
- 596 3- <u>https://doi.org/10.6084/m9.figshare.13677454</u>

597 AUTHORS' CONTRIBUTIONS

Authors	Contribution
Foad Vosoughi	Conceptualization, Software, Validation, Investigation, Resources, Data Curation, Writing - Original Draft, Visualization, Writing - Review & Editing.
Mohammad Reza Nikoo	Conceptualization, Methodology, Supervision, Writing - Review & Editing
Gholamreza Rakhshandehroo	Conceptualization, Methodology, Supervision, Writing - Review & Editing
Jan Franklin Adamowski	Supervision, Writing - Review & Editing
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598 **REFERENCES**

- Aureli, F., Dazzi, S., Maranzoni, A., Mignosa, P., and Vacondio, R. 2015. "Experimental and numerical evaluation
 of the force due to the impact of a dam-break wave on a structure." *Advances in Water Resources*.
 https://doi.org/10.1016/j.advwatres.2014.11.009.
- Barbosa, D. V. E., Santos, A. L. G., dos Santos, E. D., and Souza, J. A. 2019. "Overtopping device numerical
 study: Openfoam solution verification and evaluation of curved ramps performances." *International Journal of Heat and Mass Transfer*. https://doi.org/10.1016/j.ijheatmasstransfer.2018.11.071.
- 605 Bocchiola, D., Rulli, M. C., and Rosso, R. 2006. "Transport of large woody debris in the presence of obstacles."

- 606 *Geomorphology*. https://doi.org/10.1016/j.geomorph.2005.08.016.
- 607 Cheng, D., Zhao, X. zeng, Zhang, D. ke, and Chen, Y. 2017. "Numerical study of dam-break induced tsunami608 like bore with a hump of different slopes." *China Ocean Engineering*. https://doi.org/10.1007/s13344-017609 0078-2.
- 610 Crespo, A. J. C., Gómez-Gesteira, M., and Dalrymple, R. A. 2008. "Modeling dam-break behavior over a wet bed
 611 by a SPH technique." *Journal of Waterway, Port, Coastal and Ocean Engineering*.
 612 https://doi.org/10.1061/(ASCE)0733-950X(2008)134:6(313).
- Dias, F., and Dutykh, D. 2007. "Dynamics of Tsunami waves." NATO Security through Science Series C:
 Environmental Security. https://doi.org/10.1007/978-1-4020-5656-7_8.
- Duarte, R., Ribeiro, J., Boillat, J. L., and Schleiss, A. 2011. "Experimental Study on Dam-Break Waves for SiltedUp Reservoirs." *Journal of Hydraulic Engineering*. https://doi.org/10.1061/(ASCE)HY.19437900.0000444.
- Evangelista, S., Altinakar, M. S., Di Cristo, C., and Leopardi, A. 2013. "Simulation of dam-break waves on
 movable beds using a multi-stage centered scheme." *International Journal of Sediment Research*.
 https://doi.org/10.1016/S1001-6279(13)60039-6.
- 621 Fluent Thoery Guide. 2013. "Ansys Fluent Theory Guide." ANSYS Inc., USA, 15317(November), 724–746.
- Fu, L., and Jin, Y. C. 2016. "mproved multiphase lagrangian method for simulating sediment transport in dam break flows." *Journal of Hydraulic Engineering*. https://doi.org/10.1061/(ASCE)HY.1943-7900.0001132.
- Gallegos, H. A., Schubert, J. E., and Sanders, B. F. 2009. "Two-dimensional, high-resolution modeling of urban
 dam-break flooding: A case study of Baldwin Hills, California." *Advances in Water Resources*.
 https://doi.org/10.1016/j.advwatres.2009.05.008.
- Goseberg, N., Stolle, J., Nistor, I., and Shibayama, T. 2016. "Experimental analysis of debris motion due the
 obstruction from fixed obstacles in tsunami-like flow conditions." *Coastal Engineering*.
 https://doi.org/10.1016/j.coastaleng.2016.08.012.
- Güney, M. S., Tayfur, G., Bombar, G., and Elci, S. 2014. "Distorted physical model to study sudden partial dambreak flows in an urban area." *Journal of Hydraulic Engineering*. https://doi.org/10.1061/(ASCE)HY.1943-7900.0000926.
- Hänsch, S., Lucas, D., Höhne, T., and Krepper, E. 2014. "Application of a new concept for multi-scale interfacial
 structures to the dam-break case with an obstacle." *Nuclear Engineering and Design*.
 https://doi.org/10.1016/j.nucengdes.2014.02.006.
- He, Z., Wu, T., Weng, H., Hu, P., and Wu, G. 2017. "Numerical simulation of dam-break flow and bed change
 considering the vegetation effects." *International Journal of Sediment Research*.
 https://doi.org/10.1016/j.ijsrc.2015.04.004.
- Issakhov, A., and Imanberdiyeva, M. 2019. "Numerical simulation of the movement of water surface of dambreak flow by VOF methods for various obstacles." *International Journal of Heat and Mass Transfer*.
 https://doi.org/10.1016/j.ijheatmasstransfer.2019.03.034.
- 642 Issakhov, A., Zhandaulet, Y., and Nogaeva, A. 2018. "Numerical simulation of dam-break flow for various forms 643 obstacle VOF method." International Journal Multiphase Flow. of the by of 644 https://doi.org/10.1016/j.ijmultiphaseflow.2018.08.003.

- Jeong, W., Yoon, J. S., and Cho, Y. S. 2012. "Numerical study on effects of building groups on dam-break flow
 in urban areas." *Journal of Hydro-Environment Research*. https://doi.org/10.1016/j.jher.2012.01.001.
- Kamra, M. M., Al Salami, J., Sueyoshi, M., and Hu, C. 2019. "Experimental study of the interaction of dambreak
 with a vertical cylinder." *Journal of Fluids and Structures*.
 https://doi.org/10.1016/j.jfluidstructs.2019.01.015.
- Kattel, P., Kafle, J., Fischer, J. T., Mergili, M., Tuladhar, B. M., and Pudasaini, S. P. 2018. "Interaction of two phase debris flow with obstacles." *Engineering Geology*. https://doi.org/10.1016/j.enggeo.2018.05.023.
- Kocaman, S., and Ozmen-Cagatay, H. 2012. "The effect of lateral channel contraction on dam-break flows:
 Laboratory experiment." *Journal of Hydrology*. https://doi.org/10.1016/j.jhydrol.2012.02.035.
- LaRocque, L. A., Imran, J., and Chaudhry, M. H. 2013. "Experimental and numerical investigations of twodimensional dam-break flows." *Journal of Hydraulic Engineering*.
 https://doi.org/10.1061/(ASCE)HY.1943-7900.0000705.
- Lauber, G., and Hager, W. H. 1998. "Experiments to dambreak wave: Horizontal channel." *Journal of Hydraulic Research*. https://doi.org/10.1080/00221689809498620.
- Mambretti, S., Larcan, E., and De Wrachien, D. 2008. "1D modelling of dam-break surges with floating debris."
 Biosystems Engineering. https://doi.org/10.1016/j.biosystemseng.2008.02.011.
- Miliani, S., Montessori, A., La Rocca, M., and Prestininzi, P. (2021). "Dam-Break Modeling: LBM as the Way
 towards Fully 3D, Large-Scale Applications." *Journal of Hydraulic Engineering*, American Society of Civil
 Engineers (ASCE), 147(5).
- Mokhtar, Z. A., Mohammed, T. A., Yusuf, B., and Lau, T. L. 2019. "Experimental investigation of tsunami bore
 impact pressure on a perforated seawall." *Applied Ocean Research*.
 https://doi.org/10.1016/j.apor.2018.12.015.
- Nilsson, H. 2010. "Proceedings of CFD with OpenSource Software." Accessed September 2, 2021.
 http://dx.doi.org/10.17196/OS_CFD#YEAR_2010.
- Open⊽FOAM. 2015. "Open⊽FOAM The Open Source CFD Toolbox User Guide." OpenFOAM Foundation
 15th December 2015.
- 671 Openfoamwiki. 2020. "Unofficial OpenFOAM wiki." Accessed November 24, 2021.
 672 https://openfoamwiki.net/index.php/Main_Page.
- Ozmen-Cagatay, H., and Kocaman, S. 2010. "Dam-break flows during initial stage using SWE and RANS approaches." *Journal of Hydraulic Research*. https://doi.org/10.1080/00221686.2010.507342.
- Ozmen-Cagatay, H., Kocaman, S., and Guzel, H. 2014. "Investigation of dam-break flood waves in a dry channel
 with a hump." *Journal of Hydro-Environment Research*. https://doi.org/10.1016/j.jher.2014.01.005.
- Panda, S. K., Singh, K. K., Shenoy, K. T., and Buwa, V. V. 2017. "Numerical simulations of liquid-liquid flow
 in a continuous gravity settler using OpenFOAM and experimental verification." *Chemical Engineering Journal*. https://doi.org/10.1016/j.cej.2016.10.102.
- Postacchini, M., Othman, I. K., Brocchini, M., and Baldock, T. E. 2014. "Sediment transport and morphodynamics
 generated by a dam-break swash uprush: Coupled vs uncoupled modeling." *Coastal Engineering*.
 https://doi.org/10.1016/j.coastaleng.2014.04.003.

- Saghi, H., and Lakzian, E. 2019. "Effects of using obstacles on the dam-break flow based on entropy generation
 analysis." *European Physical Journal Plus*, Springer Verlag, 134(5). https://doi.org/10.1140/epjp/i201912592-3.
- Schiller, L., and Naumann, Z. 1935. "A drag coefficient correlation." *Z.Ver.Deutsch.Ing*, Elsevier Ltd, 77, 318 320. http://dx.doi.org/10.1016/j.ijheatmasstransfer.2009.02.006
- Shi, H., Si, P., Dong, P., and Yu, X. 2019. "A two-phase SPH model for massive sediment motion in free surface
 flows." *Advances in Water Resources*, Elsevier Ltd, 129, 80–98.
 https://doi.org/10.1016/j.advwatres.2019.05.006.
- Singh, J., Altinakar, M. S., and Ding, Y. 2011. "Two-dimensional numerical modeling of dam-break flows over
 natural terrain using a central explicit scheme." *Advances in Water Resources*.
 https://doi.org/10.1016/j.advwatres.2011.07.007.
- Torres, C., Borman, D., Sleigh, A., and Neeve, D. (2021). "Application of Three-Dimensional CFD VOF to
 Characterize Free-Surface Flow over Trapezoidal Labyrinth Weir and Spillway." *Journal of Hydraulic Engineering*, American Society of Civil Engineers (ASCE), 147(3), 04021002.
- Valiani, A., Caleffi, V., and Zanni, A. 2002. "Case study: Malpasset dam-break simulation using a twodimensional finite volume method." *Journal of Hydraulic Engineering*.
 https://doi.org/10.1061/(ASCE)0733-9429(2002)128:5(460).
- 700 Vischer, D. L., and Hager, W. H. 1998. *Dam Hydraulics*. Wiley: Chichester, New York.
- Vosoughi, F. 2018. "Experimental and Numerical Investigation of Dam-Break Phenomena in Silted-Up
 Reservoirs under Different Hydraulic Conditions." M.Sc. thesis, Departement of civil and environmental
 engineering, Shiraz university, Shiraz, Iran.
- 704 [Dataset] Vosoughi, F., Nikoo, M. R., Rakhshandehroo, G., Adamowski, J. F. 2021a "Experimental dataset on 705 sediment depths in scrutinizing the influences of downstream semi-circular obstacles on floods arising from 706 the failure of dams with different levels of reservoir silting. V2." Figshare. Dataset. Accessed November 707 24, 2021. https://doi.org/10.6084/m9.figshare.13686205
- 708 [Dataset] Vosoughi, F., Nikoo, M. R., Rakhshandehroo, G., Adamowski, J. F. 2021b "Experimental dataset on
 709 water levels in scrutinizing the influences of downstream semi-circular obstacles on floods arising from the
 710 failure of dams with different levels of reservoir silting. V2." Figshare. Dataset. Accessed November 24,
 711 2021. https://doi.org/10.6084/m9.figshare.13686142
- 712 [Dataset] Vosoughi, F., Nikoo, M. R., Rakhshandehroo, G., Adamowski, J. F. 2021c "Laboratory videos in scrutinizing the influences of downstream semi-circular obstacles on multi-layer shock waves with various sedimentation degrees in the upstream reservoir. V2." Figshare. Media. Accessed November 24, 2021. https://doi.org/10.6084/m9.figshare.13677454
- Wang, B., Liu, X., Zhang, J., Guo, Y., Chen, Y., Peng, Y., Liu, W., Yang, S., and Zhang, F. (2020a). "Analytical and Experimental Investigations of Dam-Break Flows in Triangular Channels with Wet-Bed Conditions." *Journal of Hydraulic Engineering*, American Society of Civil Engineers (ASCE), 146(10), 04020070.
- Wang, X., Chen, W., Zhou, Z., Zhu, Y., Wang, C., and Liu, Z. 2017. "Three-dimensional flood routing of a dambreak based on a high-precision digital model of a dense urban area." *Natural Hazards*.
 https://doi.org/10.1007/s11069-016-2734-x.
- Wang, Y., Liu, X., Yao, C., and Li, Y. (2020b). "Debris-Flow Impact on Piers with Different Cross-Sectional
 Shapes." *Journal of Hydraulic Engineering*, American Society of Civil Engineers (ASCE), 146(1),

- **724** 04019045.
- Weller, H. G. 2008. "A New Approach to VOF-based Interface Capturing Methods for Incompressible and
 Compressible Flow." *Technical Report*, (May), 13.
- 727 Wikipedia®. 2019. "Brumadinho dam disaster." Accessed November 24, 2021.
 728 https://en.wikipedia.org/wiki/Brumadinho_dam_disaster.
- Wu, W., and Wang, S. Y. 2007. "One-dimensional modeling of dam-break flow over movable beds." *Journal of Hydraulic Engineering*. https://doi.org/10.1061/(ASCE)0733-9429(2007)133:1(48).
- Xue, Y., Xu, W. L., Luo, S. J., Chen, H. Y., Li, N. W., and Xu, L. J. 2011. "Experimental study of dam-break
 flow in cascade reservoirs with steep bottom slope." *Journal of Hydrodynamics*.
 https://doi.org/10.1016/S1001-6058(10)60140-0.
- Yang, C. T. 1996. Sediment transport: theory and practice. McGraw-Hill series in water resources and
 environmental engineering, McGraw-Hill.
- Zhang, M., and Wu, W. M. 2011. "A two dimensional hydrodynamic and sediment transport model for dam-break
 based on finite volume method with quadtree grid." *Applied Ocean Research*.
 https://doi.org/10.1016/j.apor.2011.07.004.

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