Design of a Parallel Shoulder Assistive Robot with Pneumatic Muscle Actuators

by

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Physical Human Robot Interaction Group

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Declaration of Authorship

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Abstract

Given the increasing stroke incidence and ageing population, robotic assistance for people suffering from physically weak upper limbs in their activities of daily life (ADL) is becoming more promising. However, most of the current upper limb assistive robots (or upper limb exoskeletons) are bulky and heavy when designed to meet the requirements of sufficient degrees of freedom (DoFs), workspace and joint torques. The objective of this thesis is to develop dynamic models of pneumatic actuators and design a new mechanism towards developing a compact and lightweight upper limb exoskeleton, while providing proper kinematic capability to assist a human’s upper limbs in their ADL.

This research first focused on parallel mechanisms given their advantages of compactness and high stiffness. Multiple parallel mechanisms are reviewed in terms of their capability in delivering 3D rotational motion and safety concerning the forces transmitted to the shoulder joint when mechanisms are applied as a shoulder joint. Then, a 3UPU wrist mechanism is selected given its superior kinematic capability. An alternative forward kinematics solution for the 3UPU wrist mechanism is presented so that the upper limb’s orientation can be estimated using the universal joint’s rotation angles on the base, rather than measuring the mechanism’s limb length.

Pneumatic muscle actuators (PMAs) are then selected for driving the robotic exoskeleton because of their superiority of high strength-to-weight ratio and inherent elasticity. An enhanced dynamic force model is developed to depict the PMA’s nonlinear relationship between its length, pressure and external load. By introducing a model of Coulomb friction element, this dynamic force model overcomes the problems related to the current over-simplified models. The improvement of this enhanced model is evidently witnessed in situations where softer and more elastic PMAs are pressurised to perform large contractions.

A 3UPU wrist mechanism test rig that can measure the universal joint angles is developed for verifying the mechanism’s inverse kinematics and the proposed alternative forward kinematics. Experimental results validated the inverse kinematics of this mechanism in most cases and verified the solutions of platform orientation obtained from the alternative forward kinematics. A prototype exoskeleton is developed based on the 3UPU wrist mechanism, and is used to test the performance...
of the PMAs and the 3UPU wrist mechanism. A proportional–integral (PI) controller is used for the PMA position control. Two basic ADL movements are tested on the prototype. The experimental results and future work are then discussed.
Acknowledgements

I would like to thank my supervisor Professor Dikai Liu for his continual encouragement and belief in me, and most importantly, for his assistance throughout my course. Without his conscientious attitude and uncountable hours of intellectual interaction, I couldn’t have completed this thesis.

Thank you to the rest of the team at CAS, especially the physical human robot interaction team, Marc Carmichael, Gabriel Aguirre-Ollinger and others; the weekly meetings helped me a lot in providing suggestions for problems I met during the project. Many thanks also to Chris Hamid, who worked together with me in accomplishing the mechanical parts of this project.

I extend my gratitude to the knowledgeable and obliging engineers in the FEIT faculty, Mr Chris Chapman, Mr Richard Dibbs and the UTS Motorsports Team, for their intellectual and hardware support. Thanks also to the UTS workshop who manufactured the prototype parts.

A special thank you goes to my family and close friends—my loving parents who have supported and cared for me from far away the whole time. Thank you to Mr Xiao Lan, my closest friend who supported me financially.
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# Abbreviations

<table>
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<th>Description</th>
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<tbody>
<tr>
<td>ADL</td>
<td>Activities of Daily Life</td>
</tr>
<tr>
<td>CVT</td>
<td>Continuously Variable Transmission</td>
</tr>
<tr>
<td>DoF(s)</td>
<td>Degree(s) of Freedom</td>
</tr>
<tr>
<td>EAP</td>
<td>Electroactive Polymer</td>
</tr>
<tr>
<td>IMU</td>
<td>Inertial Measurement Unit</td>
</tr>
<tr>
<td>PI</td>
<td>Proportional–integral (Controller)</td>
</tr>
<tr>
<td>PID</td>
<td>Proportional–integral–derivative (Controller)</td>
</tr>
<tr>
<td>PMA/PM Actuator</td>
<td>Pneumatic Muscle Actuator</td>
</tr>
<tr>
<td>PWM</td>
<td>Pulse width modulation</td>
</tr>
<tr>
<td>ROM</td>
<td>Range(s) of Motion</td>
</tr>
<tr>
<td>SMA</td>
<td>Shape Memory Alloy</td>
</tr>
<tr>
<td>2D</td>
<td>Two dimensional</td>
</tr>
<tr>
<td>3D</td>
<td>Three dimensional</td>
</tr>
<tr>
<td>3UPU</td>
<td>Three Universal-Prismatic-Universal joint limbs (Mechanism)</td>
</tr>
<tr>
<td>nSPS+S</td>
<td>( n ) Spherical-Prismatic-Spherical joint limbs plus one passive Spherical joint (Mechanism)</td>
</tr>
<tr>
<td>3RRR</td>
<td>Three Revolute-Revolute-Revolute joint limbs (Mechanism)</td>
</tr>
<tr>
<td>3RPS</td>
<td>Three Revolute-Prismatic-Revolute joint limbs (Mechanism)</td>
</tr>
<tr>
<td>3UPS+S</td>
<td>Three Universal-Prismatic-Spherical joint limbs plus one passive Spherical joint (Mechanism)</td>
</tr>
<tr>
<td>3UPU wrist</td>
<td>Three Universal-Prismatic-Universal joint limbs pure rotational (Mechanism)</td>
</tr>
</tbody>
</table>
**Nomenclature**

*General Style*

- \(\{O_A, X_A, Y_A, Z_A\}\): Coordinate frame with origin at point \(O_A\) and axis \(X_A, Y_A, \) and \(Z_A\)
- \(\dot{\cdot}, \ddot{\cdot}\): Differentiation and quadratic differentiation of a variable
- \(\vec{\cdot}\): Vector
- \(\vec{\cdot}^{(O)}\): Vector \(\vec{\cdot}\) in coordinate frame \(\{O\}\)
- \(|\cdot|\): Absolute value
- \(\|\cdot\|\): Vector length and normalised vector
- \(\angle O_1 O_A A_i\): Angle between vector \(\overrightarrow{O_1 O_A}\) and \(\overrightarrow{O_A A_i}\) at point \(O_A\)
- \(\cdot^T\): Transpose of a matrix
- \(\delta L, \delta \theta\): Virtual displacement, virtual rotation angle
- \(\partial \theta\): Partial derivative of variable \(\theta\)
- \(P(t)\): Variable \(P\) as a time dependent

*Specific Symbol Usage for 3UPU Wrist Mechanism*

*Geometric Points*

- \(O, O_A, O_B\): The intersection point of the revolute pairs’ axes from both the platform and the base, from the base, and from the platform in the 3UPU wrist, respectively
- \(A_i, B_i\): Rotation centre of universal joints on the base and platform connected to the \(i^{th}\) limb, respectively
- \(O_1, O_2\): Plane centre (circular centre) of the base and platform plane, respectively

*Geometric Constants and Variables*

- \(r_A, r_B\): Length of \(|A_i O_1|\) and \(|B_i O_2|\), respectively
- \(h_A, h_B\): Distance from rotation centre \(O\) to the circular centre of base \(O_1\) and \(O_2\)
platform plane, respectively

\( \theta_x, \theta_y, \theta_z \) Rotation angles of the platform relative to the base at point \( O \), around \( X \), \( Y \) and \( Z \) axis, respectively

\( \vec{\omega} = (\omega_x, \omega_y, \omega_z) \) Angular velocity and angular acceleration of the platform

\( \vec{\eta} = (\eta_x, \eta_y, \eta_z) \)

\( \theta_{x,i}, \theta_{y,i} \) Rotation angles in the \( i^{th} \) universal joint on the base around axis \( X_{Ai} \) and axis \( Y_{Ai} \), respectively

\( \omega_{x,i}, \omega_{y,i} \) Angular velocity in the \( i^{th} \) universal joint on the base around axis \( X_{Ai} \) and axis \( Y_{Ai} \), respectively

\( l_i \) Length of the \( i^{th} \) limb

**Coordinate Frames**

\( \{O_A\}, \{O_B\} \) Coordinate frame with origin at point \( O_A \) and \( O_B \), attached to the immobile base and moving platform, respectively

\( \{A_i; X_{Ai}, Y_{Ai}, Z_{Ai}\} \) Immobile that is attached to immobile part of the \( i^{th} \) universal joint that is adjacent to the base.

\( \{O_{Ai}; X_{Oi}, Y_{Oi}, Z_{Oi}\} \) mobile that is attached to the moving part of the \( i^{th} \) universal joint that is adjacent to the base.

**Matrices**

\( R, R_x, R_y, R_z \) Rotation matrix from platform to base, rotation matrix for around \( X \), \( Y \) and \( Z \) axis alone, respectively

\( R_{Oi} \) Rotation matrix from coordinate frame \( \{A_i\} \) to frame \( \{O_A\} \)

\( R_{Ai} \) Rotation matrix from coordinate frame \( \{O_A\} \) to frame \( \{A_i\} \)

\( J \) Jacobian matrix

\( \vec{I}_i, \vec{S}_i \) The vector representing the \( i^{th} \) limb part and unit vector in the same direction, respectively

\( \Phi \) Objective function index of workspace optimisation

**Specific Symbol Usage for PMA**

\( F(x, P) \) PMA force determined by variable contraction length \( x \) and pressure \( P \)
<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$F_{\text{static}}(x, P)$</td>
<td>Static PMAA force determined by variable contraction length $x$ and pressure $P$</td>
</tr>
<tr>
<td>$F_{ce}(P)$</td>
<td>Force exerted by the contractile element</td>
</tr>
<tr>
<td>$F_{\text{adjust}}(x)$</td>
<td>Adjustment force added on static force to eliminate estimation error</td>
</tr>
<tr>
<td>$F_{\text{coulomb}}(x)$</td>
<td>Coulomb friction force</td>
</tr>
<tr>
<td>$F_{\text{Damp}}(x)$</td>
<td>Damping force</td>
</tr>
<tr>
<td>$x(t), \dot{x}(t), \ddot{x}(t)$</td>
<td>Contraction length, linear contraction velocity and contraction acceleration</td>
</tr>
<tr>
<td>$L(t)$</td>
<td>Length of the PMA</td>
</tr>
<tr>
<td>$D(t)$</td>
<td>Diameter of the PMA</td>
</tr>
<tr>
<td>$L_0$</td>
<td>Normal length of the PMA</td>
</tr>
<tr>
<td>$P(t)$</td>
<td>Pressure in the $i^{th}$ PMA</td>
</tr>
<tr>
<td>$K(x, P)$</td>
<td>Stiffness of spring element parameterised by contraction length and pressure</td>
</tr>
<tr>
<td>$K_1, K_2$</td>
<td>Coefficients of stiffness of spring element</td>
</tr>
<tr>
<td>$S_1, S_2, S_3$</td>
<td>Coefficients of passive element</td>
</tr>
<tr>
<td>$C_1$</td>
<td>Coefficients of contractile element</td>
</tr>
<tr>
<td>$N_1, N_2, N_0$</td>
<td>Coefficients of Coulomb friction force</td>
</tr>
<tr>
<td>$D_1, D_2$</td>
<td>Viscous damping friction force coefficient</td>
</tr>
<tr>
<td>$b$</td>
<td>Total length of the outer mesh threads of the PMA</td>
</tr>
<tr>
<td>$n$</td>
<td>Turns of threads of the outer mesh of the PMA</td>
</tr>
<tr>
<td>$\mu$</td>
<td>Viscosity of air gas</td>
</tr>
<tr>
<td>$v(t)$</td>
<td>Velocity of air</td>
</tr>
</tbody>
</table>