Assessing a feature's trustworthiness and two approaches to feature selection

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THESIS

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CERTIFICATE OF AUTHORSHIP/ORIGINALITY

I certify that the work in this thesis has not previously been submitted for a degree nor has it been submitted as part of requirements for a degree except as fully acknowledged within the text.

I also certify that this thesis has been written by me. Any help that I have received in my research work and the preparation of the thesis itself has been acknowledged. In addition, I certify that all information sources and literature sources used are indicated in the thesis.

Signature of Student

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Your word is a lamp to my feet and a light for my path. (Psalms 119:105 NIV)

Therefore everyone who hears these words of mine and puts them into practice is like a wise man who built his house on the rock. The rain came down, the streams rose, and the winds blew and beat against that house; yet it did not fall, because it had its foundation on the rock. (Matthew 7:24-25 NIV)

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Abstract

Improvements in technology have led to a relentless deluge of information that current data mining approaches have trouble dealing with. An extreme example of this is a problem domain that is referred to as "non-classical". Non-classical problems fail to fulfill the requirements of statistical theory: that the number of instances in the sample set be much greater than the number of dimensions. Non-classical problems are mainly characterized by many dimensions (or features) and few noise-affected samples.

Microarray technology provides one source of non-classical problems, which typically produces data sets with a dimensionality exceeding ten thousand and containing just a few hundred instances. A risk with such a data set is building a model that is significantly influenced by coincidental correlations between the inputs (or the model's features) and the output. A classical strategy for managing this risk is reducing the dimensionality without significantly affecting the correlation between the remaining features and the model's output. However this strategy does not explicitly consider the impact

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of poor data quality (or noise) and having few data samples.

In order to actively manage noise—a feature selection strategy is needed that not only considers the correlation between the features and the output, but also the quality of the features. It is proposed that feature quality, or simply the feature's "trustworthiness", should be incorporated within feature selection. As the trustworthiness of a feature increases, it is expected that the ability to accurately extract the underlying structure of the data will also increase. Another characteristic of non-classical problems is significant feature redundancy (where information provided within one dimension is also present in one or other dimensions). This research postulates that the use of feature trustworthiness and redundancy provides an opportunity to actively reduce the noise associated with the selected feature set, while still finding features that are well correlated with the model's output.

Two fundamental contributions are provided by this thesis: the notion of feature "trustworthiness" and how trustworthiness can be integrated within feature selection. Trustworthiness provides a flexible approach for evaluating the quality of a feature's sample data and in certain cases, the quality of the test data. This flexibility encourages the use of prior knowledge about the specific problem and in particular, how the quality of the data is best estimated. Traditionally feature selection implicitly assumes that every instance of data, supplied by preprocessing, has the same quality. Trustworthiness

also provides an opportunity for incorporating a measure of the changes applied to the data set as a result of data cleaning.

Using an area of computational learning, a theoretical justification was constructed that showed the difficulty of building an accurate model for a non-classical problem. The justification showed how a modest data quality problem can result in insufficient sample data to permit successful learning. It also showed how selecting less noisy data, or sufficiently trustworthy features, can enable successful learning using the available data points.

This thesis presents two methodologies that incorporate a measure of data quality within feature selection: one methodology only uses training data, while the other also incorporates test data while evaluating feature trustworthiness. The two methodologies are contrasted with each other and with a traditional feature selection methodology, which does not consider data quality.

A number of data sets were used to test these methodologies, with the main data sets being: synthetic data, childhood leukaemia and chronic fatigue syndrome. In most cases the three feature selection methodologies achieved similar accuracy however there were clear differences in the features selected by each. Using heat maps to visualize the clarity of the separation of the class labels by the selected features—showed dramatic differences. The two methodologies that incorporate trustworthiness provided a clearer

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separation, while the traditional methodology was substantially inferior and appeared to be heavily influenced by artifacts. Using Gene Set Enrichment Analysis (GSEA), a widely used resource for evaluating the biological meaningfulness of gene sets (Subramanian, Tamayo, Mootha, Mukherjee, Ebert, Gillette, Paulovich, Pomeroy, Golub, Lander, and Mesirov, 2005), showed that the two proposed methodologies selected genes that were more biologically meaningful than those selected by a traditional feature selection methodology.

The experiments also evaluated the sensitivity of trustworthiness to differences in the data set. By evaluating the trustworthiness of every feature, it was shown that considerable changes occurred across data folds. This result agrees with findings in the literature, such as (Ein-Dor, Kela, Getz, Givol, and Domany, 2005) and provides one explanation for the difficulty of modeling non-classical problems.

Contributions to knowledge

1. Two approaches for estimating data quality

This thesis describes two approaches for estimating the quality of a feature's data set, one using a measure of signal-to-noise and the other, only a measure of noise. The latter approach permits the use of test data within the estimate of a feature's utility. In calculating the quality of a feature's data set, both approaches use prior knowledge about the data set.

2. Definition and measure of feature trustworthiness

This thesis defines "trustworthiness" as an overall measure of the quality of a feature. Trustworthiness is required since each item of data associated with a feature has a unique level of quality. As a feature's trustworthiness increases, its utility approaches the estimated information it provides.

3. Definition and measure of feature utility

Feature selection methodologies typically evaluate a feature's usefulness according to the feature's inherent information. However, noise may falsely increase its information; hence reduce the feature's trustworthiness. This thesis describes a measure of a feature's usefulness called "feature utility", which is a function of information provided by the feature and the noise present within its data set.

4. Two feature selection methodologies based on feature utility

This thesis develops and evaluates two feature selection methodologies based on feature utility. The methodologies, "Feature Utility Ranking 1" and "Feature Utility Ranking 2", use respectively, a signal-to-noise ratio and a noise-only measure of quality.

The methodologies were evaluated using computational learning theory, a series of synthetic data experiments and three biomedical data sets, which are characterized by high dimensionality, few samples and significant noise. The biomedical data experiments consist of leukaemia cell type classification, leukaemia treatment outcome prediction and chronic fatigue syndrome prediction.

5. Mechanism for using data quality information collected during data cleaning

A mechanism for merging data cleaning outcomes within feature selection is explored. This approach allows the degree of change imposed by data cleaning to be incorporated in a feature's utility.

Publications

The work in this thesis has been published in:

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