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Single channel blind source separation based local mean decomposition for Biomedical applications

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Abstract—Single Channel Blind Source Separation (SCBSS) is an extreme case of underdetermined (more sources and fewer sensors) Blind Source Separation (BSS) problem. In this paper, we propose a novel technique using Local Mean Decomposition (LMD) and Independent Component Analysis (ICA) combined with single channel BSS (LMD_ICA). First, the LMD was used to decompose the single channel source into a series of data sequences, which are called as Product Functions (PF), then, ICA algorithm was used to process PFs to get similar independent components and extract the original signals. A comparison was made between LMD_ICA and previously proposed single channel ICA method (EEMD_ICA). The real time experimental results demonstrated the advantage of the proposed single channel source separation method for artifact removal and in biomedical source separation applications.

I. Introduction

Single channel source separation is one of the challenging tasks in Blind Source Separation (BSS) technique. It uses the technique to restore the original source signals from one sensor, and it has large potential applications in many areas, including communication engineering, biomedical signal denoising, audio signal processing, etc. [1].

In recent years, many researchers have proposed several algorithms to tackle this problem. A maximum likelihood approach was proposed to separate two music signals and two sounds, which needed to learn a priori sets of timedomain basis functions of sound sources [2]. So, unsupervised BSS algorithms were proposed. Adaptation of Bayesian models for single-channel source separation was introduced to separate audio, and it can perform better than non-adapted models [3]. Nonnegative matrix factorization was used to factorize the magnitude spectrogram of an input signal and then parameters of the components are estimated by minimizing the reconstruction error between the input spectrogram and the model [4]. However, the model methods needed to train the prior parameters, which required more computation time [5, 6].

Independence component analysis (ICA) has been proved to be a very powerful tool in BSS, when the number of sensors is greater or equal to the number of source signals. Many researchers changed single-channel signal into pseudo-Multi-Input and Multi-Output (MIMO) mode, then each source signal was separated via ICA. Single channel ICA (SCICA) was first proposed by Davies [7]; it can mainly separate the source signals which have disjoint spectral, e.g.,

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maternal/fetal ECG signal, however, it failed to separate the two signals. Another technique, Singular spectrum analysis (SSA) is used to process the single channel signal, then ICA is used to separate the independent components, unfortunately, this method needs to determine a right window length for constructing the pseudo-MIMO [8]. Bogdan Mijovic proposed an algorithm, which combines Ensemble Empirical-Mode Decomposition (EEMD) and ICA to successfully separate overlapped spectrum signals [9]. The algorithm first uses the EEMD to decompose the single channel into a series of data sequence called Intrinsic Mode Functions (IMFs) and then ICA was applied to IMFs to generate independent components. However, when ICA was used to process IMFs, it failed to converge even with maximum iterations.

Local Mean Decomposition (LMD) is recently proposed by J. S. Smith [10] to process Electroencephalogram (EEG) signal, as well as EMD, a data-driven tool to process nonlinear and non-stationary signal. In [11, 12], LMD was compared with EMD, the result shows that LMD is suitable and have better performance than EMD in the incipient fault detection. In this paper, we propose a novel single channel source separation algorithm combining the LMD and ICA. To verify the validity of this algorithm, real-life biomedical examples are analysed.

The rest of the paper is organized as follows: the basic principle of LMD is described in Section 2. In section 3 the novel single channel BSS method is introduced. In Section 4, the results and analysis of the real life biomedical experimental results are presented. Finally, in section 5, we summarize our algorithm and give suggestions for the future work.

II. LOCAL MEAN DECOMPOSITION

The LMD method is an effective tool to analyse nonlinear and non-stationary signals which can be used for analysis of a wide variety of natural signals such as EEG, Functional Magnetic Resonance Imaging (FMRI) data, and earthquake data, etc. The main principle of LMD method is decomposing a multi-component modulation signal into a series of frequency modulated signals and envelope components known as local magnitude functions. The LMD is briefly described as follows [11].

. To process the original signal x(t), calculate the mean of the successive maximum and minimum $n_{k,c}$ and $n_{k,c+1}$ which determine the local mean value $m_{i,k,c}$. Here, $a_{i,k,c}$ is the local magnitude, 'c' is the index of the extrema, 'i' denote the order of product function (PF) and 'k' is the iteration number in a process of PF.

$$m_{i,k,c} = \frac{n_{k,c} + n_{k,c+1}}{2} \tag{1}$$

$$a_{i,k,c} = \frac{n_{k,c} - n_{k,c+1}}{2} \tag{2}$$

- ii. Interpolate straight lines of local mean $m_{i,k}$ and local magnitude values $n_{i,k}$, then moving average filter is used to Smooth the interpolated local mean and local magnitude, get $m_{i,k}(t)$ and $a_{i,k}(t)$.
- iii. Let $h_{i,k}(t) = x(t) \tilde{m_{i,k}}(t)$, get the frequency modulated (FM) signal $s_{i,k}(t) = \frac{h_{i,k}(t)}{\tilde{a_{i,k}}(t)}$, If $s_{i,k}(t)$ is a normalized

FM signal, then go to step v. Otherwise, steps i and ii will be repeated, until $s_{i,k}(t)$ is the flat FM signal,

$$\tilde{a}_{i}(t) = \tilde{a}_{i,1}(t) \times \tilde{a}_{i,1}(t) \times \tilde{a}_{i,1}(t) \dots \times \tilde{a}_{i,p}(t) = \prod_{q=1}^{p} \tilde{a}_{i,q}(t)$$

- iv. Envelope function, q denotes the number of iterations for computing the PF. The corresponding instantaneously phase (IP) is $\varphi_i(t) = \arccos(s_{i,p}(t))$ and instantaneous frequency is (IF) $f_i(t) = \frac{d\varphi_i}{dt}$.
- v. With the envelope function $a_i(t)$ and the final frequency demodulated signal, the product function (PF) is written as $PF_i = a_i(t) \times s_{i,p}(t)$.
- vi. Then $u_i(t) = x(t) PF_i$ is treated as the smoothed version of the new x(t) and the procedure is repeated from i to v, until $u_i(t)$ is a monotonic function. The final

result can be expressed as
$$x(t) = \sum_{i=1}^{p} PF_i(t) + u_p(t)$$
.

III. ICA ALGORITHM AND SIGNAL RECONSTRUCTION

The goal of ICA is to separate mixed signals from the mixed matrix x into their independent sources s, without prior knowledge, such that x = Ms, where M is called the mixing matrix. It is possible to estimate the contributing sources from the mixtures provided; they are statistically independent of each other. In our research, the FastICA algorithm [13] which has been proved to be fast and robust was used to separate mixed signals. The steps of the whole SCBSS are as follows:

- i. The LMD algorithm is applied to the mixed signal to obtain a series of PFs which are the input signals of FastICA algorithm.
- ii. After the FastICA algorithm, a series of independent components are obtained as well as estimated mixing matrix M and unmixed matrix W. Then similar

- components of source signal's independent components are extracted.
- iii. Select the interested independent components and multiply with the estimated mixing matrix *M* and a new series of PF components are derived.

Add all the newly derived PFs and one source signal can be reconstructed. The other source signals are reconstructed in similar way.

IV. SIMULATION RESULTS AND DISCUSSION

In order to validate the effectiveness of the proposed method, we designed two different experiments, which are explained as below:

In this section, the novel SCBSS algorithm is used to separate the single channel sensor signal which is mixture of Electrocardiogram (ECG) and Electromyography (EMG). All simulations and analyses are performed using MATLAB programming language. The surface EMG (sEMG) signal is a kind of important biological electric signal produced with the muscle activity, which has been widely used in clinical muscle disease diagnosis, sports science, rehabilitation engineering and gesture recognition [14] etc. For the large overlap between the ECG interfere spectrum and of the sEMG signal (5-500Hz for sEMG, 0-75Hz for ECG), it is hard to extract sEMG signal from mixed signal using normal filter.

In this experiment, ECG artifact was removed from sEMG signal. We used the LMD-ICA and EEMD-ICA to remove ECG signal from sEMG signal respectively. To evaluate the proposed algorithm, we adopt the same criteria in [9]; ECG and sEMG signals were mixed by the model as equation (3),

$$x(t) = a(t) + \lambda b(t) \tag{3}$$

where x(t) is the mixed single channel signal, a(t) is the sEMG, and b(t) is the noise signal which is ECG signal. The Noise to Signal Ratio (NSR) which is an important measure is defined as follows:

$$NSR = \frac{RMS(\lambda b(t))}{RMS(a(t))}$$
 (4)

The performance of the simulation is relative root mean squared error (RRMSE) which is explained as follows:

$$RRMSE = \frac{RMS\left(a(t) - \tilde{a}(t)\right)}{RMS\left(a(t)\right)} \times 100\%$$
 (5)

where a(t) is estimated signal, $RMS(\bullet)$ equals to root mean square.

We obtained the ECG signal from MIT/BIH database, and the sEMG signal is achieved from our self-made equipment which we have obtained national patent [15] as shown in Figure 1.

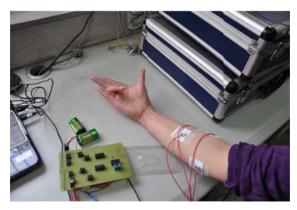


Figure 1. A demonstration of sEMG signal acquisition

Figure 2 shows the source signals and mixed signal with *NSR* = 0.6342. We can clearly find 4 heart beat interference peaks in the mixed signal.

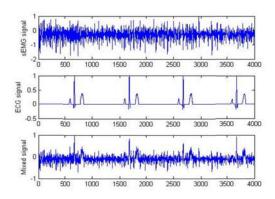


Figure 2. Source signals and mixed single channel signal

A. Decompose mixed single channel

The LMD algorithm is applied to this single channel mixed signal, the PFs is shown in Figure 3.

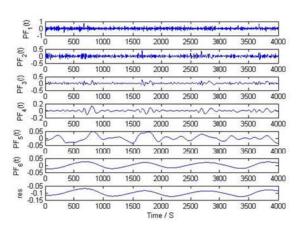


Figure 3. PFs of the mixed single channel

Then, the EEMD algorithm is used to process mixed single channel. The noise and artefacts does influence the success of the EEMD algorithm. Hence, in this experiment, we set the noise parameter to 0.2 and an ensemble trial is set as 100 [16], the IMFs of mixed single channel is shown in Figure 4.

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2	500	1000	1500	2000	2500	3000	3500	4000

Figure 4. IMFs of the mixed single channel

B. Blind source separation

The mixed single channel is decomposed by LMD and EEMD respectively. The FastICA algorithm is used to process these components. For calculation of the independent components, the non-quadratic nonlinearity function $g(u) = u^3$ is chosen. The results of the FastICA are shown in Figure 5 and Figure 6 respectively. The iteration of FastICA for processing IMFs and PFs are shown in table I. The iterate number of PFs obviously smaller than IMFs.

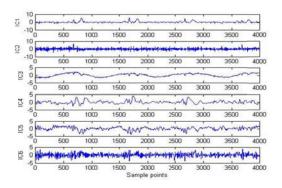


Figure 5. Independent components by LMD-ICA

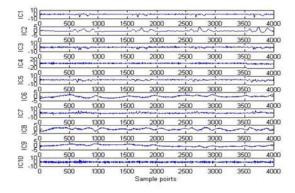


Figure 6. Independent components by EEMD-ICA

From Figure 5, we can clearly see that the IC(1) and IC(4) are related to the ECG signal. However, in Figure 6, we can only find the IC (2) close to ECG, the other part components of original ECG signal still mixed in other components.

C. Reconstruct the source signal

Here, the interested IC's are multiplied with the estimated mixing matrix and added together. Finally the source signals are reconstructed as shown in Figure 7. From Figure 7, we can see that both the algorithms can separate the ECG and sEMG very well, meanwhile, we can observe the amplitude of R wave in ECG(a) are weakened, so the performance of EEMD-ICA is not ideal.

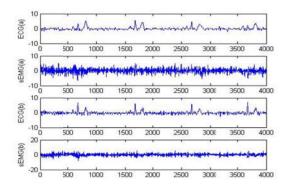


Figure 7. Separation results of two algorithms, ECG(a) and sEMG (a) separated by the EEMD_ICA, ECG(b) and sEMG (b) were separated by the LMD_ICA.

For a comprehensive comparison of the two algorithm's separation performance we repeated the above process with the NSR values ranging from 0.1 to 2.0 which are shown in Figure 8.

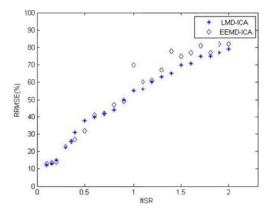


Figure 8. Comparison of algorithms performances

From Figure 8 it can be seen that, with the increase in NSR, the value of RRMSE also increases, i.e. the separation effect is worse. Both the algorithms performed very well when the NSR is small, however, as the NSR value increases, the stability and performance of EEMD-ICA is worse than LMD-ICA. This is because, when reconstruct the source signal from the EEMD-ICA, the components of source signal still give out multiple ICs (refer to Figure 7).

TABLE I ITERATES OF THE FASTICA

Method	IC1	IC2	IC3	IC4	IC5	IC6	IC7	IC8	IC9	IC10
EEMD-ICA	15	16	15	12	10	43	10	57	5	2
LMD-ICA	40	9	15	13	7	4	-	-	-	-

V. CONCLUSION

In this paper, we presented a novel single channel BSS method based on the LMD and ICA. Single channel signal was decomposed into ICs, which combines LMD and ICA. We compared it with the EEMD-ICA [9], and the experimental results have confirmed the outstanding performance of novel algorithm. The real-life example which separated ECG and EMG mixed single channel source proved that the method is a powerful tool to extract various biomedical sources. We also find that when the NSR is high, the performance of the two algorithms is poor. In this context, we would like to conduct further research on single channel BSS using high NSR values.

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