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# EXPERIMENTAL AND NUMERICAL STUDY OF TIME-DEPENDENT BEHAVIOUR OF REINFORCED SELF-COMPACTING CONCRETE SLABS

By

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### **CERTIFICATE OF ORIGINAL AUTHORSHIP**

I certify that the work in this thesis has not previously been submitted for a degree nor has it been submitted as part of requirements for a degree except as fully acknowledged within the text.

I also certify that the thesis has been written by me. Any help that I have received in my research work and the preparation of the thesis itself has been acknowledged. In addition, I certify that all information sources and literature used are indicated in the thesis.

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### LIST OF PUBLICATIONS

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## LIST OF NOTATIONS

Chapter 3	
γ	unit weight of concrete
$\phi$	fibre inclination angle
λ, μ	coefficients of linear equation of the stress-strain curve
$\lambda_f, \mu_f$	coefficients of linear equation of the SFRSCC stress-strain curve
$\kappa_l$	first proposed constant value for MOE prediction
$\kappa_2$	second proposed constant value for MOE prediction
$\eta_{I}$	first proposed constant value for TS prediction
$\eta_2$	second proposed constant value for TS prediction
$\mu_i$	initial coefficient of friction
$\mu_{ss}$	steady state value of the coefficient of friction attained at large pullout
	distances
$\sigma_c$	concrete stress
$\sigma_{cf}$	SFRSCC compressive stress
$\sigma_{ctf}$	SFRSCC tensile stress
З	concrete strain
$\varepsilon'_c$	strain corresponding with the maximum stress $f'_c$
$\varepsilon'_{cf}$	strain at peak stress of SFRSCC
$\varepsilon^*$	corresponding strain to the $0.85 f_{ctf}$
$\mathcal{E}_{ct}$	tensile concrete strain
$\mathcal{E}_{f}$	SFRSCC strain
$ au_{max}$	maximum bond strength
$ au_{max(app)}$	maximum apparent bond shear strength
$ au_{f(app)}$	fibre apparent bond shear strength
$ au_{f}$	fibre bond shear strength
$ au_u$	ultimate bond strength
а	radius of fibre
С	concrete cover

c (fibre)	a constant that governs the rate at which the coefficient of friction decays	
	with increase in pullout distance	
$d_b$	diameter of the steel bar	
$d_{f}$	diameter of fibre	
$E_c$	modulus of elasticity of concrete	
$E_{cf}$	modulus of elasticity of SFRSCC	
$E_{sec}$	secant modulus of elasticity	
$E_{secf}$	secant modulus of elasticity of SFRSCC	
f	snubbing friction coefficient	
$f_c$	maximum compressive strength of concrete	
$f_{\it cf}$	compressive strength of SFRSCC	
$f'_{cy}$	maximum compressive strength of cylinder concrete specimens	
$f'_{cu}$	maximum compressive strength of cube concrete specimens	
$f_{cr}$	modulus of rupture of concrete	
$f_{ct}$	tensile strength of concrete	
$f_{ctf}$	tensile strength of SFRSCC	
k	spalling coefficient and $\phi$ is in radians	
$l_d$	embedded length of the steel bar	
$l_f$	length of fibre	
$l_f/d_f$	aspect ratio	
n	material parameter that depends on the shape of the stress-strain curve	
n <sub>f</sub>	SFRSCC parameter that depends on the shape of the stress-strain curve	
$n_1$	modified material parameter at the ascending branch	
<i>n</i> <sub>lf</sub>	modified SFRSCC parameter at the ascending branch	
$n_2$	modified material parameter at the descending branch	
$n_{2f}$	modified SFRSCC parameter at the descending branch	
$p_{d1}$ and $p_{d2}$	fibre pullout distances	
$P_{p_{d1}}$ and $P_{p_{d2}}$	fibre pullout loads corresponding to pullout distances $p_{d1}$ and $p_{d2}$	
$P_m$	measured fibre pullout load	
R.I.	fibre reinforcing index	
S, S <sub>1</sub> , S <sub>2</sub> , S <sub>3</sub>	slip related to pullout bond test	

$U_{\textit{peak}}(\pmb{\phi})$	peak slip displacement corresponding to the peak load with the inclination	
	angle $\phi$	
$V_f$	fibre volume fraction	
$W_p$	work of fibre pullout	
Chapter 4		
α	coefficient representing the influence of the cement type	
eta	represents time dependency of drying shrinkage	
γ	coefficient representing the influence of the cement and admixtures type	
η	constant related to compressive strength and water content	
κ	conventional scalar damage index	
$\mu$ , $\lambda$ and $\alpha$	parameters to be obtained from a least square minimization procedure	
$eta_{ m sc}$	coefficient which depends on the type of cement	
$\sigma'_{cp}$	creep stress unit	
$\varepsilon'_{sh}$	final value of shrinkage strain	
$\varepsilon'_{ds ho}$	the final value of drying shrinkage strain	
$\varepsilon'_{ds\infty}$	final value of drying shrinkage	
$\varepsilon'_{as\infty}$	final value of autogenous shrinkage strain	
ε' <sub>cr</sub>	final value of creep strain per unit stress	
$\varepsilon'_{bc}$	final value of basic creep strain per unit stress	
$\varepsilon'_{dc}$	final value of drying creep strain per unit stress	
$(\varepsilon_{\rm sh})_{\rm u}$	ultimate shrinkage strain	
$\varepsilon_e(t)$	instantaneous strain	
$\varepsilon'_{cs}(t,t_0)$	shrinkage strain of concrete from age to t	
$\varepsilon'_{ds}(t,t_0)$	drying shrinkage strain of concrete from age to t	
$\varepsilon'_{as}(t,t_0)$	autogenous shrinkage strain of concrete from age to t	
$\varepsilon'_{sc}(t,t_0)$	shrinkage strain of concrete from age of $t_0$ to $t$	
$\varepsilon'_{as}(t,t_0)$	autogenous shrinkage strain of concrete from the start of setting to age $t$	
$\varepsilon'_{cc}(t, t', t_0)$	creep strain	
$\Delta t_i$	number of days where the temperature T prevails	
$T(\Delta t_i)$	temperature (°C) during the time period $\Delta t_i$	
С	cement	

c/p	cement to powder ratio	
$f_c$	compressive strength	
$f_{c,28d}$	compressive strength at the age of 28 days	
$f_{\rm cm}$	mean compressive strength of concrete at the age of 28 day	
$f_{ m cmo}$	10 MPa	
$f_{cm}(t)$	mean value of compressive strength at time t	
f	constant based on the duration of curing	
$h_0$	100 mm	
h	notional size of member (mm)	
$RH_0$	100%	
RH	relative humidity (%)	
s' and n	parameters that have to be specifically calibrated for each SCC concrete	
	mix by using experimental results	
$t_1$	1 day	
$t_0$	effective age (days) of concrete at the beginning of drying	
t'	effective age (days) of concrete at the beginning of loading	
t	effective age (days) of concrete during loading respectively	
$T_0$	1 °C	
v/s	volume to surface ratio	
W	water	
w/c	water to cement ratio	
Chapter 5		
$\alpha$ and $\beta$	empirical constants related to compressive strength model	
$\eta$ and $\mu$	d $\mu$ empirical constants related to modulus of elasticity	
$\gamma$ and $\lambda$	empirical constants related to tensile strength	
$\psi$ and $\phi$	empirical constants related to modulus of rupture	
$\omega$ and $\rho$	empirical constants related to energy dissipated under compression	
χ, ζ	coefficients of linear equation of stress-strain curve	
$\sigma_c$	concrete stress	
З	concrete strain	
$\varepsilon_c'$	strain corresponding with the maximum stress $f_c$	

$\mathcal{E}_{u}$	ultimate deformation
$E_c$	modulus of elasticity
$E_{cN}$	N-SCC mix modulus of elasticity
$E_{cfD}$	D-SCC mix modulus of elasticity
$E_{cfS}$	S-SCC mix modulus of elasticity
$E_{cfDS}$	DS-SCC mix modulus of elasticity
$E_{sec}$	secant modulus of elasticity
$f_c'$	maximum compressive strength of concrete
$f'_{cN}$	N-SCC mix compressive strength
$f'_{c\!f\!D}$	D-SCC mix compressive strength
$f'_{cfS}$	S-SCC mix compressive strength
$f_{cfDS}$	DS-SCC mix compressive strength
$f_{ctN}$	N-SCC mix tensile strength
$f_{ctfD}$	D-SCC mix tensile strength
$f_{ctfS}$	S-SCC mix tensile strength
$f_{ctfDS}$	DS-SCC mix tensile strength
$f_{crN}$	N-SCC mix modulus of rupture
$f_{crfD}$	D-SCC mix modulus of rupture
$f_{crfS}$	S-SCC mix modulus of rupture
$f_{crfDS}$	DS-SCC mix modulus of rupture
$G_c$	energy dissipated under compression
$G_{cN}$	N-SCC mix energy dissipated under compression
$G_{cfD}$	D-SCC mix energy dissipated under compression
$G_{cfS}$	S-SCC mix energy dissipated under compression
$G_{cfDS}$	DS-SCC mix energy dissipated under compression
n	material parameter that depends on the shape of the stress-strain curve
$n_1$	modified material parameter at the ascending branch
$n_2$	modified material parameter at the descending branch
Chapter 6	
$ au_b$	bond shear stress
$M_s$	in-service bending moment

$M_{cr}$	cracking moment
kd	compression chord of depth
b	width
$A_{st}$	tensile reinforcement of area
$A_{ct}$	area of tensile concrete
d	depth
Icr	second moment of area about the centroidal axis
$\sigma_{ct}$	uniform tensile stress of concrete
$b^*$	width of the section at the level of the centroid of the tensile steel
ρ	tensile reinforcement ratio
n	modular ratio
М	applied moment
$f_y$	steel yield stress
$f_{ct}$	direct tensile strength of the concrete
$\lambda_1$	load duration factor
$\lambda_2$	reduction in bond stress as the steel stress $\sigma_{st1}$ factor
$\lambda_3$	significant increase in bond stress factor
$ ho_{tc}$	reinforcement ratio of the tension chord
$d_b$	reinforcing bar diameter
S <sub>min</sub>	minimum crack spacing
S <sub>max</sub>	maximum crack spacing
$(w_i)_{tc}$	instantaneous crack width
k <sub>cover</sub>	a term to account for the dependence of crack width on the clear concrete
	cover
<i>W<sub>max</sub></i>	maximum crack width
les	transfer length
$\mathcal{E}_{sm}$	mean steel strain
$\varepsilon_{cm}$	mean concrete strain
$\sigma_{cf}$	stress in the fibre reinforced concrete
$\sigma^{i}_{cf,cr}$	imaginary cracking stress of the fibre reinforced concrete
$ au_{sm}$	average bond stress over load transmission length

$E_s$	modulus of elasticity of reinforcing bar
$ ho_s$	reinforcing ratio of steel reinforcement
$lpha_b$	shape coefficient of strain courses
$lpha_E$	ratio of the modulus of elasticity of steel to the modulus of elasticity of
	concrete
$f_R$	relative rib area of the rebars
$\sigma_s$	stress in the reinforcing bar at a crack
F	applied load
$A_s$	cross-sectional area of the steel bars
$G_{f}$	fracture energy of the concrete matrix
$\sigma_{cf0}$	maximum post-cracking stress
$w_0$	crack width corresponding to maximum post-cracking stress
$\sigma_{cf0}$	maximum post-cracking stress
η	coefficient of fibre orientation
g	coefficient of fibre efficiency
$ ho_{f}$	volume fraction of fibres
$l_f$	fibre length
$d_{f}$	fibre diameter
$ au_{fm}$	mean fibre-matrix bond stress
$f_{ctm}$	mean tensile strength of the plain concrete matrix
$E_{f}$	modulus of elasticity of the fibres
$\sigma^{i}_{cf,cr}$	maximum stress of the ascending fibre phase
Chapter 7	
$lpha_b$	shape coefficient of strain courses
$lpha_{E,s}$	ratio of the modulus of elasticity of steel to the modulus of elasticity of
	concrete
$lpha_{E,f}$	ratio of the modulus of elasticity of fibre to the modulus of elasticity of
	concrete
η	fibre orientation coefficient
$\mathcal{E}_{f,shr}$	shrinkage shortening of the fibres
$ ho_s$	reinforcing ratio of steel reinforcement

$ ho_{f}$	fibre content	
$ ho_{tc}$	reinforcement ratio of the tension chord	
$\sigma_{cf}$	stress in the fibre reinforced concrete	
$ au_b$	bond shear stress	
$ au_{sm}$	average bond stress over load transmission length	
$A_{st}$	tensile reinforcement of area	
$A_{ct}$	area of tensile concrete	
b	width	
$d_b$	reinforcing bar diameter	
$E_s$	modulus of elasticity of reinforcing bar	
kd	compression chord of depth	
$M_{cr}$	cracking moment	
$M_s$	in-service bending moment	
<i>S</i> *	final maximum crack spacing	
Chapter 8		
$\alpha_e$	modular ratio = $E_s / E_c$	
$lpha_b$	shape coefficient of strain courses	
$lpha_E$	ratio of the modulus of elasticity of steel to the modulus of elasticity of	
	concrete	
eta	empirical coefficient to assess the mean strain over $l_{s,max}$	
$eta_{ac}$	ratio of the distances from the neutral axis to the extreme tension fibre	
$eta_{ec}$	coefficient relating the average crack width to the design value	
$\beta_{mc}$	empirical coefficient to assess the average strain within $l_{s,max}$	
$\phi$	diameter of the steel fibre	
ρ	relaxation coefficient	
$ ho_{e\!f}$	effective steel ratio	
arphi	creep coefficient	
$\sigma_{s}$	steel stress	
$\sigma_{sr}$	maximum steel stress in a crack in the crack formation stage	
$\sigma_{cti}$	uniform average tensile stress	
$ au_{bi}$	short-term bond stress	

$ au_{bm}$	mean bond strength
$ au_{sm}$	average bond stress over load transmission length
E <sub>cm</sub>	mean strain in the concrete between the cracks
$\mathcal{E}_{s2}$	maximum steel strain at the crack
$\mathcal{E}_{sr2}$	steel strain at the crack
$\mathcal{E}_{CS}$	free shrinkage strain of concrete
$\mathcal{E}_{sm}$	mean strain in the reinforcement at the design loads
$\eta_r$	coefficient taking account of shrinkage contribution
$A_{ct}$	cross-sectional area of concrete in the tensile zone
$A_{c,eff}$	effective area of the tensile concrete surrounding the tensile reinforcement
	of depth
$A_e$	effective tension area of concrete surrounding the flexural tension
	reinforcement
$A_{s,min}$	minimum tensile reinforcement area
$A_{st}$	cross-sectional area of tensile steel reinforcement
С	clear cover to the longitudinal reinforcement
d	depth to the tensile reinforcement
$d_b$	bar diameter
$d_c$	distance from centre of bar to extreme tension fibre
$d_n$	depth of compression zone in a fully cracked section
D	overall depth of a cross-section
$E_s$	steel modulus of elasticity
$f_{ct}$	concrete matrix tensile strength
$f_{ct,eff}$	mean value of the axial tensile strength of concrete at the time cracking
$f_{ctm}$	mean value of axial tensile strength
$F_{cr}$	cracking force
$f_{Fts}$	steel fibre tensile strength
$f_s$	maximum stress permitted in the reinforcement immediately after crack
	formation
$f_y$	steel bar yield stress
$k_t$	factor that depends on the duration of load

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- $k_1$  coefficient depending upon bond quality
- $k_2$  coefficient depending upon the shape of the strain diagram
- *l<sub>es</sub>* transfer length
- $l_{s,max}$  length over which slip between steel and concrete occurs
- *L* length of the steel fibre
- $M_{cr}$  cracking moment
- *M<sub>max</sub>* maximum moment
- $n_b$  number of reinforcing bar
- s bar spacing
- *s*<sub>rm</sub> average crack spacing
- *s<sub>r,max</sub>* maximum crack spacing
- $w_k$  maximum crack width
- $w_m$  average crack width
- *w<sub>max</sub>* maximum crack width

## LIST OF ACRONYMS

AEA	air-entraining admixtures	
CA	coarse aggregate	
CC	conventional concrete	
CD	casting direction	
CRI	concrete research institute	
CRC	conventional reinforced concrete	
CS	compressive strength	
CSSC	compressive stress-strain curve	
c/p	cement to powder ratio	
EFA	Eraring Fly Ash	
FA	fine aggregate	
FCL	first crack load	
FCD	first crack deflection	
FEM	finite element method	
FRC	fibre-reinforced concrete	
FRSCC	fibre-reinforced self-compacting concrete	
FTS	flexural tensile strength	
Н	horizontal casting direction	
HMR	high moment region	
HRWR	high range water reducer	
GGBFS	ground granulated blast furnace slag	
LVDT	linear variable displacement transducer	
MOE	modulus of elasticity	
MOR	modulus of rupture	
RH	relative humidity	
RC	reinforced concrete	
RVE	representative volume element	
SC	slag cement	

SCC	self-compacting concrete	
SFC	super flowable concrete	
SFRC	steel fibre-reinforced concrete	
SFRSCC	steel fibre reinforced self-compacting concrete	
SHCC	strain hardening cementitious composites	
SLC	shrinkage limited cement	
SP	superplaticizers	
SUCST	specimen utilized in the compressive strength test	
TS	tensile strength	
UHPFRC	high and ultrahigh performance fibre reinforced concrete	
V-D	vertical down casting direction	
V-U	vertical up casting direction	
w/c	water-cement ratio	
w/cm	water-cementitious materials ratio	
VMA	viscosity modifying admixture	
WHS	workplace health and safety	
WR	water reducer	

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### ABSTRACT

Developments in concrete technology provide engineers, designers, suppliers and contractors with new methods of approaching engineering problems. Many of these developments are engineered solutions to technical and commercial problems, by either improving the current practices or overcoming limitations in the existing technology. One of the developments is Self-Compacting Concrete (SCC). SCC refers to a 'highly flow-able, non-segregating concrete that can be spread into place, fill the formwork, and encapsulate the reinforcement without the aid of any mechanical consolidation' as defined by the American Concrete Institute (ACI). SCC is regarded as one of the most promising developments in concrete technology due to significant advantages over Conventional Concrete (CC). Many different factors can influence a decision to adopt SCC over CC ranging from structural performance to associated costs. These decisions should be well informed and based on a sound understanding of such factors.

In addition, Fibre Reinforced Self-Compacting Concrete (FRSCC) is a relatively new composite material which congregates the benefits of the SCC technology with the profits derived from the fibre addition to a brittle cementitious matrix. Fibres improve many of the properties of SCC elements including tensile strength, ductility, toughness, energy absorption capacity, fracture toughness and cracking.

For a structure (made by CC, SCC and FRSCC) to remain serviceable, crack widths must be small enough to be acceptable from an aesthetic point of view, to avoid waterproofing and deterioration problems by preventing the ingress of water and harmful substances. Crack control is therefore an important aspect of the design of reinforced concrete structures at the serviceability limit state. Limited researches have been undertaken to understand cracking and crack control of SCC and FRSCC members. Since, the timedependent mechanisms of SCC and FRSCC are still not completely understood; a reliable and universally accepted design procedure for cracking and crack control of SCC and FRSCC members has not been developed yet. There exists a need for both theoretical and experimental research to study the critical factors which affect the time-dependent cracking of SCC and FRSCC members. In this study cracking caused by external loads in reinforced SCC and FRSCC slabs is examined experimentally and analytically. The mechanisms associated with the flexural cracking due to the combined effects of constant sustained service loads and shrinkage are observed. One of the primary objectives of this study is to develop analytical models that accurately predict the hardened mechanical properties of SCC and FRSCC. Subsequently, these models have been successfully applied to simulate time-dependent cracking of SCC and FRSCC one-way slabs.

Series of tests on eight prismatic, singly reinforced concrete one-way slabs subjected to monotonically increasing loads or to constant sustained service loads for up to 240 days, were conducted. An analytical model is presented to simulate instantaneous and time-dependent flexural cracking of SCC and FRSCC members. It should be emphasized that any analytical model developed for calculation of crack width and crack spacing of reinforced SCC and FRSCC slabs must be calibrated by experimental data and verified by utilizing Finite Element Method (FEM). The analytical predictions of crack width and crack spacing for the SCC and FRSCC one-way slabs are in reasonably good agreement with the experimental observations.