INTRODUCTION

In the last decade, the performance of fuel cells has been greatly improved mainly thanks to the advancement of proton exchange membrane fuel cells (PEMFCs). A large amount of work was conducted by various researchers for predicting the performance, which is a key factor in the development of new applications. Unfortunately, the performance of a PEMFC is extremely difficult to model analytically, so empirical formulations are often used. Its performance depends on many variables, such as temperature, pressure, current density, and water content of the membrane. Many of these variables depend on each other yielding non-linearity in the performance models [1]. This makes the study on PEMFC control systems very difficult.

In this paper, a fuzzy logic controller with PI control loops is designed and implemented to directly control the H2 and air mass flows in a 500W PEMFC power system. The fuzzy-PI controller is used to automatically fine-tune the parameters of a conventional PI controller. Depending on the output voltage and current of the stack, the fuzzy controller constantly interprets the process reaction and calculates the optimal P and I gains. The output voltage of the PI controller directly regulates the flow rate of H2 and air. The experimental results demonstrate that the fuzzy-PI controller can improve the voltage and current performance of the system when the load changes.

2 REVIEW ON MODEL-BASED CONTROL STRATEGIES

The transient response of a PEMFC due to a load change is a complex phenomenon. The transient model has to account for the electrochemical reaction of the fuel and air, and multi-phase transport of the water and gas components. Moreover, heat and charge transports occur in the PEMFC.

Kuwata et al. [2] described a control method for a DC-DC converter and its characteristics. The converter can maintain the maximum fuel cell output to keep total efficiency high, and can achieve stable fuel cell operation even when the AC power fails or the load varies.

Ro and Rahman [3] developed a controller for a fuel cell power plant to assist the conventional generators for
damping oscillation. The controller receives the grid bus voltage magnitude and system frequency variations, which are taken as the feedback inputs. A power conditioning subsystem fulfills the DC-AC power conversion by turning on and off switches according to a switching scheme.

Sedghisigarchi [4] analyzed the dynamics of distribution systems that contains fuel cells and the enhancement of the stability of these systems by controlling the fuel cells. The control loops through the power conditioning units were first explained using an one-machine infinite bus system.

Sakhare et al. [5] adopted a solid oxide fuel cell mathematical model, and designed a power condition unit for this solid oxide fuel cell and for fuel cells in general. The fuzzy logic control strategy is used in the design of the controllers for DC-AC and DC-DC converters. The output is converted to a controlled DC voltage by a control scheme that adjusts the duty ratio of the converter and also protects the fuel cell against sudden load variations and current reversal.

Iqbal [6] presented the dynamic modeling of various components of an isolated power system containing fuel cells. The selection of control strategies and design of controllers for the system is described. A software package, SIMNON™, is used for simulating this highly nonlinear system. A proportional-integral-differential (PID) type fuel cell controller is used to adjust the fuel (H₂) inlet and oxygen pressure to maintain a constant stack output voltage. The controller can compensate the voltage drop in the fuel cell stack caused by the load current variation. In the simulation, Iqbal used the PID type controller to control the fuel cell voltage by varying the H₂ and O₂ flow rates.

Based on their previous work, Khan and Iqbal [7] conducted a dynamic modeling and simulation of a small wind-fuel cell hybrid energy system. The system, however, has never been implemented.

Abtahi et al. [8] presented a control strategy for a fuel cell system based on a pressure regulator. Different pulsing profiles for the pulsed air source were investigated. The pulse amplitude, frequency and duty cycle were varied and their impact on the fuel cell power density was studied. The authors discussed the applicability of fuzzy logic to implement the control strategy. Pulsing of the air pressure cannot be applied in our fuel cell system because we use fans for the air supply.

3 DESIGN OF FUZZY LOGIC CONTROLLER

3.1 Model of PEMFC System

A PEMFC model used in this paper was developed by Balkin, Holland and Zhu [9]. In this model, the PEMFC stack terminal voltage, \( V_{\text{stack}} \) is determined by subtracting the various voltage losses from the reversible voltage as

\[
V_{\text{stack}} = V_{\text{reversible}} - V_{\text{ohmLOSS}} - V_{\text{actLOSS}} - V_{\text{conLOSS}} \quad (1)
\]

where \( V_{\text{reversible}} \), \( V_{\text{ohmLOSS}} \), \( V_{\text{actLOSS}} \) and \( V_{\text{conLOSS}} \) are the maximum theoretical voltage, ohmic voltage loss, activation voltage loss and concentration voltage loss, respectively.

Incorporated in these voltage loss terms is an internal current. These voltage losses result in an operating voltage that is less than the reversible voltage as shown in the typical polarization curve in Fig. 1.

![Typical polarization curve of fuel cell stack](https://via.placeholder.com/150)

The reversible voltage at varying temperature and pressure can be expressed as

\[
V_{\text{reversible}} = N_{\text{cell}} V^0 + \frac{RT}{2F} \ln \left[ \frac{P_{\text{H}_2} (P_{\text{O}_2})^{1/2}}{P_{\text{H}_2}^* (P_{\text{O}_2})^{1/2}} \right] + N_{\text{cell}} \Delta S_{298.15K} \left( T - 298.15 \right) \quad (2)
\]

where \( N_{\text{cell}} \), \( V^0 \), \( R \), \( T \), \( F \), \( P_{\text{H}_2}^* \), \( \Delta S_{298.15K} \) and \( P_{\text{O}_2}^* \) are the number of cells in the PEMFC stack, reversible fuel cell voltage at the standard temperature and pressure (STP), universal gas constant, temperature of the PEMFC stack in K, Faraday’s constant, standard pressure, change in the molar entropy at STP, and pressure of species \( m \) (H₂, O₂, or H₂O), respectively.

With the pressure in atmosphere and using the standard values for the constants in (2), the reversible voltage can be reduced to

\[
V_{\text{reversible}} = N_{\text{cell}} \times 1.229 + \left( 4.308 \times 10^{-5} \right) F \ln \left[ \frac{P_{\text{H}_2}^* (P_{\text{O}_2})^{1/2}}{P_{\text{H}_2}^* (P_{\text{O}_2})^{1/2}} \right] - N_{\text{cell}} \times \left( 8.453 \times 10^{-4} \right) \left( T - 298.15 \right) \quad (3)
\]
3.2 Design of Fuzzy-PI Controller

3.2.1 Design Concept

The fuzzy-PI controller, shown in Fig 2, uses the error signal and its change from the measured feedback data as the inputs. If the output signal describes the necessary difference toward the voltage and current output value, an intelligent fuzzy reasoning device is needed to build up the command variable value. That is to say, although the fuzzy-PI controller does not have a special operating point, the controller rules evaluate the difference between the measured values of voltage and current and the setting values, which is the error signal, and also evaluate the tendency of the error signal to determine whether to increase or decrease the control output variable. The absolute value of the command output variable is not influenced.

The advantage of a fuzzy-PI controller over a conventional PI controller is that it can implement nonlinear control strategies and that it uses linguistic rules. It is possible to consider only the error tendency when the error becomes small.

In this paper, in order to avoid the difficulty caused by that a large number of variables affect the performance of the PEMFC system and the use of a complex model, a fuzzy-PI controller based on PEMFC expert knowledge is proposed. The fuzzy-PI controller can produce a much better performance than a conventional PID controller.

The fuzzy-PI controller consists of five different steps and parts, including the definition of input-output variables of the controller, fuzzification, designing of fuzzy control rules, inference and defuzzification [10-14].

3.2.2 Definition of Input-output Variables

The air mass flow control loop is used as an example to show the design process of the fuzzy-PI controller as follows.

The controller input variables are the voltage error \( e(k) \), and the change of error \( c(k) \). The output variables are the optimal \( P \) and \( I \) gains of a subsequent PI controller device, one of them gives the proportional part \( K \) as a function of \( e(k) \) and \( c(k) \), and the other gives the increment \( \Delta T \), which is then integrated to provide the integral term \( T \) of the PI controller. The error \( e(k) \), change of error \( c(k) \) and the output variable \( u(k) \) of the controller are given by

\[
 e(k) = V_{\text{setpoint}} - V_{\text{stack}} \quad (4)
\]

\[
 c(k) = e(k) - e(k-1) \quad (5)
\]

\[
 u(k) = u(k-1) + K\{e(k) + \frac{1}{T} \sum_{i=1}^{k} (e(i) + e(i-1)) \Delta t\} \quad (6)
\]

3.2.3 Fuzzification and Membership Function

The triangular type membership function is chosen because of its linearity. The collections of the reference fuzzy set for the error, the change of error, and the control input are the same, but their scale factors are different. As shown in Fig 3, seven fuzzy subsets, i.e. positive big (PB), positive medium (PM), positive small (PS), zero (ZE), negative small (NS), negative medium (NM), and negative big (NB), are used for the input and output variables \( e(k), c(k), K \) and \( T \).

3.2.4 Design of Fuzzy Control Rules

Fuzzy control rules are obtained from the behavior analysis of the PEMFC system. Because the rule-base represents the intelligence of the controller, the formulations should be carefully considered. Correct use of control laws according to the operating conditions can greatly improve the system stability. A fast response with a small overshoot for the PEMFC system can be achieved with proper handling of the proportional and integral parts.

The selected control rules or laws are described as follows:

1) Far from the voltage set point: When the output voltage is far from the set point, i.e. \( e(k) \) is PB or NB, the corrective action must be strong. This means that \( K \) should be NB (or PB) while \( T \) should be zero (ZE), in order to prevent the continuous increase (or decrease) of integral term that would cause overshoots. In this case, the change of error plays little part.

The basic control rules are:

If \( e(k) \) is PB, then \( K \) is NB and \( T \) is ZE;
If \( e(k) \) is NB, then \( K \) is PB and \( T \) is ZE.

2) Close to the voltage set point: In this region, the change of error must be properly taken into account in order to ensure stability and speed of response. The goal of the
fuzzy controller is to achieve a satisfactory dynamic performance with small sensitivity to parameter variations.

The control rules are:
If both $e(k)$ and $c(k)$ are ZE, then $K$ and $T$ are ZE;
If both $e(k)$ and $c(k)$ is negative, $K$ and $T$ are negative;
If both $e(k)$ and $c(k)$ is positive, $K$ and $T$ are positive.

According to these criteria, the rule sets are derived as shown in Table 1 and Table 2.

### 3.2.5 Inference

There are various ways in which the observed input values can be used to identify which rules should be used to infer an appropriate fuzzy control action. The fuzzy inference methods are MAX-MIN fuzzy inference reasoning, MAX-PRODUCT inference reasoning, and SUM-PRODUCT fuzzy reasoning.

A basic and simple inference method, MAX-MIN fuzzy inference, is employed in this paper. One of the rules is expressed by

$$
\text{Rule } i: \text{ If } e \text{ is } E_i \text{ and } c \text{ is } C_i, \text{ then } P \text{ (or } T) \text{ is } P_i \text{ (or } T_i)
$$

The membership of the inferred consequence $P$ (or $T$) is point-wise, given by

$$
\mu_p(z) = \vee_{i=1}^{n} (\mu_{E_i}(e) \land \mu_{C_i}(c)) \land \mu_{P_i}(e, c)
$$

### 3.2.6 Defuzzification

Defuzzification is the process of mapping from a space of inferred fuzzy control actions to a space of non-fuzzy control actions. A defuzzification strategy aims to produce a non-fuzzy control action that best represents the possibility distribution of the inferred fuzzy control actions. In real-time implementation of fuzzy logic control, the commonly used defuzzification strategies include the mean of maximum (MOM), the center of maximum (COM), the center of area (COA) and the center of gravity (COG).

The COA is selected for the defuzzification process in this paper. The inferred values $P^*$ (or $T^*$) of the control action corresponding to the values $e(k)$ and $c(k)$ are obtained by

$$
P^* = \sum_{i=1}^{n} \mu_{P_i}(P_i) / \sum_{i=1}^{n} \mu_{P_i}(P_i)
$$

where $P_i$ is the singleton value of the fuzzy output variable using the $i$-th rule.

### 4 TEST SYSTEM AND RESULTS OF PEMFC FUZZY CONTROL

A testing PEMFC power system was constructed at UTS. The design of the prototype device has been investigated by the authors with the help of the description manual of the apparatus provided by the manufacturer. The evaluation of the functionality and effectiveness of the device was based on the experimental data of the 32-cell, 500W stack, which will be used for the stack performance testing, model and control evaluation, and investigation of new fuel cell technology. This apparatus has been designed to measure and basically control the mass flow rate, pressure, temperature, relative humidity of the hydrogen and air, and inlet temperature and outlet temperature of the water-cooling. Additionally, the test apparatus can measure the stack voltage and current, and coolant water temperature change across the stack.

The PEMFC test system is comprised of a PEMFC module and a control software. The module consists of a PEMFC stack, water-cooling components, air-cooling, hydrogen humidification filtering and temperature monitoring. There are three gases used to operate this system: hydrogen, nitrogen and oxygen. The control software is used to control the whole process.

The proposed fuzzy-PI logic controller is tested and implemented in the UTS PEMFC power system. Based on the control software LabVIEW™, the control interface is designed and shown in Fig 4.

The output voltage and current are set according to the stoichiometry chart of the PEMFC stack. Some experimental results are given in Fig. 5.

The experimental results reveal that while the PEMFC stack works in the open-loop state, according to the stoichiometry chart, after the $H_2$ and air flow values have been set, the output voltage and current values will change when load and other conditions change. Once the fuzzy-PI controller is introduced, the output voltage and current characteristic could be adjusted to the desired values. The characteristics of fuzzy-PI controller are better than those of the PID controller. Its overshoot is smaller while the settling time is similar.
5 CONCLUSION

A fuzzy-PI controller for PEMFC power systems based on double closed-loop control is presented. Compared to the open-loop and standard PI control, the new controller can improve significantly the load performance of the fuel cell stack. Both the theoretical and experimental results have proved that the fuzzy control scheme can work well without using an accurate mathematical model. A major advantage of the fuzzy-PI controller over a conventional PI controller is its capability to implement nonlinear control strategies by using linguistic rules. It is possible to consider only the error tendency when the error becomes small. With fuzzy logic controllers, the experience and the knowledge obtained by the supervising operators can be used to form fuzzy rules, which are important in developing a fuzzy logic controller. The effectiveness of the proposed intelligent fuzzy controller has been verified by experimental results of a PEMFC power system.

REFERENCES