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# Coupling carbon allocation with leaf and root phenology predicts tree-grass partitioning along a savanna rainfall gradient

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## Abstract

The relative complexity of the mechanisms underlying savanna ecosystem dynamics, in comparison to other biomes such as temperate and tropical forests, challenges the representation of such dynamics in ecosystem and Earth system models. A realistic representation of processes governing carbon allocation and phenology for the two defining elements of savanna vegetation (namely trees and grasses) may be a key to understanding variations in tree/grass partitioning in time and space across the savanna biome worldwide. Here we present a new approach for modelling coupled phenology and carbon allocation, applied to competing tree and grass plant functional types. The approach accounts for a temporal shift between assimilation and growth, mediated by a labile carbohydrate store. This is combined with a method to maximise long-term net primary production (NPP) by optimally partitioning plant growth between fine roots and (leaves + stem). The computational efficiency of the analytic method used here allows it to be uniquely and readily applied at regional scale, as required, for example, within the framework of a global biogeochemical model.

We demonstrate the approach by encoding it in a new simple carbon/water cycle model that we call HAVANA (Hydrology and Vegetation-dynamics Algorithm for Northern Australia), coupled to the existing POP (Population Orders Physiology) model for tree demography and disturbance-mediated heterogeneity. HAVANA-POP is calibrated using monthly remotely-sensed fraction of absorbed photosynthetically active radiation (fPAR) and eddy-covariance-based estimates of carbon and water fluxes at 5 tower sites along the Northern Australian Tropical Transect (NATT), which is characterized by large gradients in rainfall and wildfire disturbance. The calibrated model replicates observed gradients of fPAR, tree leaf area index, basal area and foliage projective cover along the NATT. The model behaviour emerges from complex feed-backs between the plant physiology and vegetation dynamics, mediated by shifting above- vs. below-ground resources, and not from imposed hypotheses about the controls on tree/grass

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co-existence. Results support the hypothesis that resource limitation is a stronger determinant of tree cover than disturbance in Australian savannas.

## 1 Introduction

Savannas constitute one of the world's most extensive biomes and provide ecosystem services as rangelands and marginal agricultural lands for one-fifth of the world's population (Lehmann et al., 2009). Being sensitive to variations in rainfall and water availability, they have a primary role in governing interannual variability in biosphere-atmosphere carbon exchange and the CO<sub>2</sub> concentration of the atmosphere (Ahlström et al., 2015; Poulter et al., 2014). For the last three decades, semi-arid ecosystems (including savannas) globally have exhibited a positive net carbon uptake trend (Ahlström et al., 2015), coinciding with regional observations of woody encroachment and increased vegetation greenness when viewed from space (Donohue et al., 2009; Liu et al., 2015). The biogeochemical dynamics of seasonally dry savannas are modulated by stress tolerance and pulse response behaviour of the drought adapted biota as the environment shifts seasonally in the relative availability of above- (light) and below-ground (mainly water) resources. Resource competition – or avoidance of competition through spatial and temporal niche segregation (Ward et al., 2013) – between trees and grasses, as well as disturbances due to grazing animals and fires (Lehmann et al., 2014; Sankaran et al., 2005) drives shifts in allocation and tree vs. grass performance that feed back to and tightly couple the water and carbon cycles. The relative complexity of the mechanisms underlying savanna ecosystem dynamics, in comparison to other biomes such as temperate and tropical forests, challenges the representation of such dynamics in ecosystem and Earth system models (Baudena et al., 2015).

Phenology and allocation of carbon to leaves, roots and stems are critical determinants of savanna productivity (Ma et al., 2013; Scholes and Walker, 2004). Savanna vegetation occurs in regions of high rainfall variability and, while vegetation is often water-limited, light can limit production seasonally or during heavy precipitation

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episodes (Whitley et al., 2011). Species may partition available carbon seasonally and interannually in order to optimise uptake of variably available resources above and below ground. Resource availability often changes quickly: species respond by producing resource uptake surfaces quickly to optimise uptake of the most limiting resource – leaves to capture light when soil water is abundant, fine roots to increase water uptake as supplies deplete. To enable a rapid response to changing resources, plants draw on stored non-structural carbohydrates (NSC) in storage, which are accumulated during times of plenty. This must lead to a temporal shift between plant growth and carbon capture.

10 A realistic representation of processes governing carbon allocation and phenology for the defining elements of savanna vegetation (namely trees and grasses) may thus be a key to understanding variations in tree/grass partitioning in time and space in the savanna biome worldwide. Global vegetation models typically treat allocation and phenology as independent processes. One exception is the ADGVM model of Scheiter and  
15 Higgins (2009) which is specialised for the simulation of savannas. It uses an individual plant's carbon status to determine the transition between active and dormant states, dynamically allocating carbon based on resource (light or water) limitation. However, no large-scale vegetation model of which we are aware allows phenology to emerge as a result of allocation of assimilated carbon to leaves and roots in response to changing  
20 relative availability of above- and below-ground resources during the course of a growing season or between years.

Here we present a new approach that links phenology and allocation, accounting for a temporal shift between assimilation and growth, which is mediated by a labile carbohydrate store. The novelty of the approach lies in the dynamic constraint of plant  
25 growth such that the long term change in store (net primary production minus growth) is zero (a requirement for carbon conservation). This is combined with the use of an optimal response method for analytically predicting the partitioning of plant growth between fine roots and (leaves + stem), which optimises long term NPP. While optimal response methods for carbon allocation are not new (Franklin et al., 2012), and have

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been applied to savanna vegetation (Schymanski et al., 2009) the computational efficiency of the analytic method used here allows it to be uniquely readily applied at regional scale, as required, for example, within the framework of a land surface model or ESM.

5 We demonstrate the approach by encoding it in a simple carbon/water cycle model that we call HAVANA (Hydrology and Vegetation-dynamics Algorithm for Northern Australia), coupled to the POP (Population Orders Physiology) model for tree demography and disturbance-mediated heterogeneity (Haverd et al., 2013b, 2014). HAVANA-POP is applied to and tested against observations from the Northern Australian Tropical Transect, featuring gradients in rainfall and wildfire disturbance. In particular, the model is  
10 evaluated against a suite of observations that are sensitive to the tree-grass ratio along the transect, namely: eddy-covariance-based estimates of carbon and water fluxes at 5 tower sites; dynamics of remotely-sensed fPAR; tree leaf area index derived from digital hemispheric photography and satellite observations; gradients of tree basal area and foliage projective cover.  
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## 2 Model description

HAVANA is a new model of landscape water balance and plant function. It contains two water stores (upper and lower soil) and leaf and fine root compartments for each of two competing vegetation types: trees and grass. The tree vegetation type also has a stem  
20 compartment, which includes coarse roots. The stem compartment is partitioned between sapwood and heartwood via coupling to the POP module (Haverd et al., 2013b), which accounts for tree demography and landscape-heterogeneity mediated by disturbance.

Qualitative relationships between key variables for a single vegetation type (trees) are shown in Fig. 1. The schematic also applies to grass, except that the stem component does not apply in grasses, and grass fine-roots do not access the deep soil  
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moisture store. Although not represented in Fig. 1, trees and grass interact via competition for water in the shallow upper soil layer, and competition for light.

In the model, soil water stores change in response to input from precipitation and losses due to evapotranspiration, deep drainage and surface runoff (Fig. 1). Dynamics of vegetation carbon stores are governed by growth and turnover rates. Growth is constrained to be equal to net primary production (NPP, equal to gross primary production minus autotrophic respiration) in the long term, but is temporally dependent on the size of the NSC store, soil water availability and the deviation of the structural carbon store from an internally computed carbon carrying capacity, above which growth stops and NPP is stored away as NSC. Growth is partitioned between (leaf + stem) and fine root compartments using an optimal response theory in which long term NPP is the fitness proxy. That is, we assume the ecological optimality hypothesis, that evolutionary selection pressures drive ecosystems towards maximal utilization of available resources for the production of biomass, so that long-term NPP over many reproductive cycles takes the largest possible value under the constraints of available resources (Raupach, 2005). This leads to a negative feed-back of soil moisture on allocation to fine roots, in favour of the combined (leaf + stem) compartment. Partitioning of growth between leaf and stem is influenced by the relative magnitudes of leaf and sapwood compartments, which are constrained by the Pipe Model (Shinozaki et al., 1964), in which sapwood cross-sectional area is assumed to be a constant proportion of total leaf area. Leaf and fine root carbon stores are subject to first order decay, while turnover of woody biomass is given by the mortality (both resource-limitation and disturbance components, including fire) computed within the POP module (Sect. 2.3 and Appendix A).

The carbon and water cycles are primarily linked by the transpiration component of evapotranspiration, with a secondary link being the dependences of growth and growth-partitioning on soil moisture. Transpiration, equivalent to root water extraction, is modelled as the lesser of evaporative demand (dependent on radiation, air temperature and fraction cover) and supply-limited root water uptake, which depends both on soil moisture and root density in each soil layer.

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Trees and grass compete for light and water. Tree roots can potentially access water in both shallow and deep soil layers, whereas grass roots are assumed unable to access the deep soil moisture store. Further, grass is partially shaded by trees as a function of tree cover.

A quantitative description of the model follows. All parameter symbols, meaning, values and sources are listed in Table 1.

## 2.1 Water balance model

The water balance model is that of the Australian Water Availability Project (Raupach et al., 2009), with modification to the transpiration terms to allow for root-carbon dependence, and is described here in full for completeness.

*State variables:* The two state variables of the water balance model are soil water stores ( $W_1$ ,  $W_2$ ) [m water] corresponding to upper and lower soil layers. The layers together encompass the whole soil profile from which water is extracted by plant transpiration. Corresponding dimensionless variables are the relative soil water ( $w_1$ ,  $w_2$ ) in the two stores, between 0 and 1 and related to  $W_1$  and  $W_2$  by

$$w_i = W_i / (\theta_{S_i} Z_{W_i}) \quad (i = 1, 2) \quad (1)$$

where  $\theta_{S_i}$  [ $\text{m}^3 \text{m}^{-3}$ ] is the saturated volumetric water content and  $Z_{W_i}$  [m] is the thickness of layer  $i$ .

*Balance equations:* The dynamic equations governing  $W_1$  and  $W_2$  are the mass conservation equations for soil water:

$$\begin{aligned} \frac{dW_1}{dt} &= \theta_{S_1} Z_{W_1} \frac{dw_1}{dt} = \underset{\text{Precipitation}}{F_{WPrec}} - \underset{\text{Transpiration from layer 1}}{F_{WTra1}} - \underset{\text{Soil Evaporation}}{F_{WSoil}} - \underset{\text{Surface Runoff}}{F_{WRun}} - \underset{\text{Leaching from layer 1 to 2}}{F_{WLch1}} \\ \frac{dW_2}{dt} &= \theta_{S_2} Z_{W_2} \frac{dw_2}{dt} = \underset{\text{Leaching from layer 1 to 2}}{F_{WLch1}} - \underset{\text{Deep Drainage}}{F_{WLch2}} - \underset{\text{Transpiration from layer 2}}{F_{WTra2}} \end{aligned} \quad (2)$$

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where all water fluxes ( $F_W$ ) are in metres of water per day [ $\text{mH}_2\text{O d}^{-1}$ ].

*Phenomenological equations:* The phenomenological equations for water fluxes are as follows.

(1) *Precipitation* ( $F_{W\text{Prec}}$ ) is an external input.

(2) *Transpiration* ( $F_{W\text{Tra}}$ ) is defined for each soil layer ( $i = 1, 2$ ) and each plant type ( $j = \text{grass [g], trees [wood = w]}$ ) as the lesser of an energy-limited transpiration rate  $F_{W\text{Tra(ELim)},j}$  and a water-limited transpiration rate  $F_{W\text{Tra(WLim)},j}$ :

$$F_{W\text{Tra},i,j} = \min(F_{W\text{Tra(ELim)},i,j}, F_{W\text{Tra(WLim)},i,j}) \quad (3)$$

(Note here that  $F_{W\text{Tra},2,\text{grass}} = 0$ , as it is assumed that grass roots do not access the lower soil moisture store.)

The total energy-limited transpiration rate (summed over two soil layers) is partitioned among soil layers using the water-limited transpiration for each layer under prevailing (energy-limited) conditions, so that:

$$F_{W\text{Tra(ELim)},j} = F_{W\text{Tra(ELim)},j} [F_{W\text{Tra(WLim)},i,j} / (F_{W\text{Tra(WLim)},1,j} + F_{W\text{Tra(WLim)},2,j})] \quad (4)$$

The total energy-limited transpiration rate,  $F_{W\text{Tra(ELim)}}$ , and the water-limited transpiration for each layer,  $F_{W\text{Tra(WLim)},i}$ , are defined as follows.

The total energy-limited transpiration rate is the evaporation rate from the surface without soil water constraints. It is often defined using the Penman–Monteith equation, but for reasons of both physics (Raupach, 2001, 2000) and simplicity, it is defined here as

$$F_{W\text{Tra(ELim)},j} = \nu_j F_{W(\text{PT})} \quad (5)$$

where  $\nu_j$  is the tree or grass vegetation cover fraction and  $F_{W(\text{PT})}$  is the Priestley–Taylor evaporation rate [ $\text{mH}_2\text{O d}^{-1}$ ], a thermodynamic estimate of the energy-limited evaporation rate for the whole surface (vegetation plus soil). The factor  $\nu_j$  relates energy-limited total evaporation to the plant component only.

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From Raupach (2000, 2001),  $F_{W(\text{PT})}$  is

$$F_{W(\text{PT})} = c_{\text{PT}} \Phi_{\text{Eq}} / (\rho_W \lambda_W) \quad (6)$$

where  $\rho_W$  [ $\text{molH}_2\text{O m}^{-3}$ ] is the density of liquid water,  $\lambda_W$  [ $\text{J molH}_2\text{O}^{-1}$ ] is the latent heat of vaporisation of water,  $\Phi_{\text{Eq}}$  [ $\text{J m}^{-2} \text{d}^{-1}$ ] is the thermodynamic equilibrium latent heat flux, and  $c_{\text{PT}}$  is the Priestley–Taylor coefficient, a number which is well constrained at about 1.26 (Priestley and Taylor, 1972; Raupach, 2001). The equilibrium latent heat flux is given by

$$\Phi_{\text{Eq}} = \rho \varepsilon \Phi_A^* / (\rho \varepsilon + 1) \quad (7)$$

where  $\Phi_A^*$  is the isothermal available energy flux,  $\varepsilon$  is the ratio of latent to sensible heat content of saturated air (2.2 at  $20^\circ\text{C}$ , roughly doubling with each  $13^\circ\text{C}$  temperature increase) and  $\rho$  is a number slightly less than 1 accounting for radiative coupling:

$$\rho = \frac{G_a}{G_a + G_r} \quad (8)$$

where  $G_a$  is the aerodynamic conductance for heat and water vapour transfer;  $G_r = 4e\sigma T_a^3 / (\rho_A c_{\text{PA}})$  is the radiative conductance;  $\rho_A$  [ $\text{mol m}^{-3}$ ] is the density of air; and  $c_{\text{PA}}$  is the specific heat of air at constant pressure [ $\text{J mol}^{-1} \text{K}^{-1}$ ].

The isothermal available energy flux  $\Phi_A^*$  is given by

$$\Phi_A^* = (1 - a) \Phi_{\text{S}\downarrow} + e(\Phi_{\text{L}\downarrow} - \sigma T_a^4) \quad (9)$$

where  $\Phi_{\text{S}\downarrow}$  and  $\Phi_{\text{L}\downarrow}$  are the downward solar (shortwave) and thermal (longwave) irradiances;  $a$  and  $e$  are whole-surface albedo and emissivity, respectively;  $\sigma$  is the Stefan–Boltzmann constant;  $T_a$  [K] is the air temperature at a reference height.

Energy fluxes ( $\Phi$ ) are calculated as averages over daylight hours only, since it is assumed that total evaporation ( $F_{\text{WE}} = F_{W\text{Tra}} + F_{\text{WSoil}}$ ) and its components are all zero at

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night. Downward daytime longwave irradiance is estimated with the Swinbank (1963), formula:

$$\Phi_{Lj} = 335.97(T_a/293)^{6.0} \quad (10)$$

using average daytime  $T_a$  estimated as  $0.75T_{a,\max} + 0.25T_{a,\min}$ .

5 The water-limited transpiration rate in layer  $i$  by plant type  $j$  is parameterised as:

$$F_{W\text{Tra}(W\text{Lim})i,j} = k_{E,i,j} C_{R,i,j} W_i^{D_{\text{extract}}} \quad (11)$$

where  $k_{E,i,j}$  is a rate per unit root carbon density [ $\text{m d}^{-1} (\text{mol C m}^{-2})^{-1}$ ] for the uptake of water by roots from a drying soil under water-limited transpiration, and  $C_{R,i,j}$  is the root carbon density [ $\text{mol C m}^{-2}$ ] of soil layer  $i$  and plant type  $j$ .

10 (3) *Soil evaporation* ( $F_{W\text{Soil}}$ ) is formulated as:

$$F_{W\text{Soil}} = (1 - \nu) w_1^\beta F_{W(\text{PT})} \quad (12)$$

where  $\beta$  is an exponent specifying the response of soil evaporation to upper-layer soil water ( $w_1$ ).

(4) *Surface runoff* ( $F_{W\text{Run}}$ ) is given by

$$15 F_{W\text{Run}} = F_{W\text{Prec}} \text{Step}(w_1 - 1) \quad (13)$$

All precipitation runs off when the upper-layer soil is saturated, and there is no runoff otherwise.

(5) *Leaching* ( $F_{W\text{Lch}}$ ) or drainage downward out of soil layer  $i$  is given by

$$F_{W\text{Lch},i} = K_{S,i} w_i^\gamma \quad (14)$$

20 where  $\gamma$  is an exponent specifying the response of drainage to relative soil water  $w_i$ , and  $K_{S,i}$  [ $\text{m d}^{-1}$ ] is the saturated hydraulic conductivity of soil layer  $i$ .

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## 2.2 Model of vegetation function

*State variables and governing equations:* The state variables of the vegetation model are carbon pools in leaves and fine roots of trees and grass, and the woody carbon pool (stem plus coarse roots) in trees. The dynamics of these pools are governed by their mass conservation equations, with each pool augmented by a proportion  $\alpha$  of the growth flux. Leaf and fine root pools are depleted by first order decay, while all tree carbon pools are depleted by tree mortality:

$$5 \frac{dC_{L,j}}{dt} = \alpha_{L,j} F_{C,\text{Growth},j} - k_{L,j} C_{L,j} - \frac{C_{L,j}}{C_{\text{stem}}} m_{\text{stem},j} \quad (15)$$

$$\frac{dC_{R,i,j}}{dt} = \alpha_{R,i,j} F_{C,\text{Growth},j} - k_{R,i,j} C_{R,i,j} - \frac{C_{R,i,j}}{C_{\text{stem}}} m_{\text{stem},j} \quad (16)$$

$$10 \frac{dC_{\text{stem}}}{dt} = \alpha_{\text{stem}} F_{C,\text{Growth},w} - m_{\text{stem}} \quad (17)$$

In Eqs. (15)–(17),  $C$  denotes a carbon pool [ $\text{mol C m}^{-2}$ ];  $\alpha$  a carbon allocation coefficient; L leaves; R fine roots; stem trunk plus coarse roots  $k$  a first order rate constant [ $\text{d}^{-1}$ ];  $j$  a plant type (woody or grassy) and  $i$  a soil layer (upper or lower),  $m_{\text{stem},j}$  is stem biomass turnover [ $\text{mol C m}^{-2} \text{d}^{-1}$ ], which is zero for grass, and computed by POP for trees (See Sect. 2.3).

For woody vegetation, we adopt a dependence of leaf turnover on specific leaf area, based on the synthesis of Wright et al. (2002):

$$k_{L,w} = 1 / \left( 365 \left( \frac{A_{\text{SL},w}}{60} \right)^{-1.2} \right) \quad (18)$$

### 2.2.1 Growth

20 Growth (the flux of carbon to structural components) is parameterised by a logistic curve, inspired by Choler et al. (2010), who specified growth of grasses in water-

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controlled ecosystems as the product of (i) a growth scaling parameter, (ii) relative soil moisture content, (iii) one minus current leaf carbon, relative to a fixed carrying capacity and (iv) current leaf carbon

In contrast we specify growth following Eq. (19) as the product of: (i) a growth scaling parameter ( $\beta_{\text{growth}}$ ), (ii)  $f_{w,j}$ , an increasing function of soil water in the upper soil layer (grass) or lower soil layer (trees) (Eq. 20) (n.b. that trees and grass nonetheless compete for water in the upper soil layer via transpiration) (iii) one minus (leaf + fine root) carbon relative to a prognostic carrying capacity  $C_{\text{max},j}$ , above which growth stops and net primary production is stored away as non-structural carbohydrate, (iv) the sum of (a) long-term NPP, (b) a multiple of the long-term net flux (NPP – growth) to the NSC store, and (c) a residual component  $F_{0,\text{growth}}$ , allowing regrowth to occur, should the plant  $C$  stores decline to zero.

$$F_{C,\text{Growth},j} = \beta_{\text{growth}} f_{w,j} \max \left[ \left( 1 - \frac{C_{\text{leaf},j} + \sum_i C_{R,i,j}}{C_{\text{max},j}} \right), 0.0 \right] \left( F_{0,\text{growth}} + \max \left[ \overline{F_{C,\text{NPP},j}} + k_{\text{store}} \left( \overline{F_{C,\text{NPP},j}} - \overline{F_{C,\text{growth},j}} \right), 0.0 \right] \right) \quad (19)$$

$$f_w = \frac{1 - \left( 1 + \left( \frac{w}{w_{\text{thresh}}} \right)^{\rho_{\text{growth}}} \right)^{-1}}{1 - \left( 1 + \left( \frac{1}{w_{\text{thresh}}} \right)^{\rho_{\text{growth}}} \right)^{-1}} \quad (20)$$

## 2.2.2 Dynamic storage (coupling of net primary production and growth)

Growth is constrained to equal time-averaged NPP over some averaging period ( $t_{\text{av},j}$ ) (set here to 1 yr for grass and 3 yr for trees), producing a change in storage of carbohydrate (NPP minus Growth) which averages to zero. This is achieved by adjusting  $C_{\text{max},j}$

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dynamically according to:

$$\frac{dC_{\text{max},j}}{dt} = \begin{cases} K_{\text{growth}} \left( \frac{\overline{F_{C,\text{NPP},j}} - \overline{F_{C,\text{growth},j}}}{\overline{F_{C,\text{growth},j}}} \right)^2 \left( \frac{C_{\text{leaf},j} + \sum_i C_{R,i,j}}{C_{\text{max}}} \right) \left( C_{\text{leaf},j} + \sum_i C_{R,i,j} \right); & \overline{F_{C,\text{NPP},j}} - \overline{F_{C,\text{growth},j}} > 0 \\ -K_{\text{growth}} \left( \frac{\overline{F_{C,\text{NPP},j}} - \overline{F_{C,\text{growth},j}}}{\overline{F_{C,\text{growth},j}}} \right)^2 \left( \frac{C_{\text{leaf},j} + \sum_i C_{R,i,j}}{C_{\text{max}}} \right)^{-1} \left( C_{\text{leaf},j} + \sum_i C_{R,i,j} \right); & \overline{F_{C,\text{NPP},j}} - \overline{F_{C,\text{growth},j}} \leq 0 \end{cases} \quad (21)$$

Such that  $C_{\text{max},j}$  increases if time-averaged net primary production exceeds growth and decreases otherwise.  $C_{\text{max},j}$  is maintained above  $C_0$ .

## 2.2.3 Net Primary Production

Net primary production is the difference between gross primary production ( $F_{C,\text{GPP},j}$ ) and maintenance respiration of leaves and fine roots, scaled by  $(1 - c_{\text{growth}})$  to account for growth respiration (Ryan, 1991):

$$F_{C,\text{NPP},j} = (1 - c_{\text{growth}}) \left( F_{C,\text{GPP},j} - \sum_i F_{C,\text{Rm},R,i,j} - F_{C,\text{Rm},L,j} - F_{C,\text{Rm},w} \right) \quad (22)$$

## 2.2.4 Gross Primary Production

Plant gross primary production ( $F_{C,\text{GPP},j}$ ) is evaluated as the lesser of light- and water-limited components:

$$F_{C,\text{GPP},j} = \min[(\alpha_{Q,j} \nu_j F_Q), (\alpha_W \rho_W F_{W\text{Tra},j})] \quad (23)$$

where  $F_Q$  is the incident quantum flux of photosynthetically active radiation (PAR) on the surface [ $\text{mol quanta m}^{-2} \text{d}^{-1}$ ], and  $\alpha_Q$  and  $\alpha_W$  are respectively a PAR use efficiency

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[molC molquanta<sup>-1</sup>] and a transpired-water use efficiency [molC molH<sub>2</sub>O<sup>-1</sup>]. Of these,  $\alpha_Q$  is a prescribed parameter, and  $\alpha_W$  is calculated as

$$\alpha_W = m_{\alpha,j}([\text{CO}_2]_a - [\text{CO}_2]_c)/(1.6D_S) \quad (24)$$

where  $m_{\alpha,j}$  is a dimensionless multiplier,  $[\text{CO}_2]_a$  is the atmospheric CO<sub>2</sub> concentration,  $[\text{CO}_2]_c$  is the CO<sub>2</sub> compensation point [molC molAir<sup>-1</sup>] calculated using the (Von Caemmerer, 2000) algorithm:

$$[\text{CO}_2]_c = 37.0 \times 10^{-6} \times 1.37^{\frac{T_S - 25.0}{10.0}} \quad (25)$$

$D_S$  is the surface saturation deficit [molH<sub>2</sub>O<sup>-1</sup> molAir<sup>-1</sup>], calculated from the air saturation deficit  $D_a$  as in (Raupach, 1998):

$$D_S = D_a + \frac{\varepsilon(\rho(\Phi_A - \Phi_E)) - \Phi_E}{\rho_A C_p G_a} \quad (26)$$

and surface temperature  $T_S$  is given by:

$$T_S = T_a + \frac{\varepsilon(\rho(\Phi_A - \Phi_E))}{\rho_A C_p G_a} \quad (27)$$

### 2.2.5 Maintenance respiration

The rate of maintenance respiration for the  $j$ th compartment (sapwood, leaf or fine roots) is formulated as:

$$R_{m,j} = k_{\text{resp}} C_j / \text{ratio}_{\text{CtoN},j} g(T_a) \quad (28)$$

where  $k_{\text{resp}} = 0.0548 \text{ d}^{-1}$  is the rate constant for maintenance respiration (Sprugel et al., 1995), and  $g(T)$  is the ecosystem respiration temperature response function

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of Lloyd and Taylor (1994) adopted by Sitch et al. (2003) in the LPJ model:

$$g(T) = \exp \left[ 308.56 \left( \frac{1}{56.02} - \frac{1}{T - 227.13} \right) \right] \quad (29)$$

and  $\text{ratio}_{\text{CtoN}}$  is the mass ratio of carbon to nitrogen in the plant tissue, here taken as 30 for leaves and fine roots, and 300 for sapwood.

### 2.2.6 Carbon allocation

Following Raupach (2005), we choose time-dependent carbon allocation coefficients to maximise the total carbon gain, namely the long-term integral of  $F_{C,NPP,j}$  for each plant type. As discussed by Raupach (2005), the vector of allocation coefficients has "bang-bang" character, meaning that, at each instant  $t$ , an allocation coefficient of one is assigned to the pool for which the marginal return on invested growth is largest while all the other pools receive zero allocation:

$$\alpha_{L,j} + \alpha_{\text{stem},j} = H \left[ \frac{\delta F_{C,NPP,j}}{\delta C_{L,j}} - \frac{\delta F_{C,NPP,j}}{\delta C_{R,1,j}} \right] H \left[ \frac{\delta F_{C,NPP,j}}{\delta C_{L,j}} - \frac{\delta F_{C,NPP,j}}{\delta C_{R,2,j}} \right] \quad (30)$$

$$\alpha_{R,1,j} = H \left[ \frac{\delta F_{C,NPP,j}}{\delta C_{R,1,j}} - \frac{\delta F_{C,NPP,j}}{\delta C_{L,j}} \right] H \left[ \frac{\delta F_{C,NPP,j}}{\delta C_{R,1,j}} - \frac{\delta F_{C,NPP,j}}{\delta C_{R,2,j}} \right] \quad (31)$$

$$\alpha_{R,2,j} = H \left[ \frac{\delta F_{C,NPP,j}}{\delta C_{R,2,j}} - \frac{\delta F_{C,NPP,j}}{\delta C_{L,j}} \right] H \left[ \frac{\delta F_{C,NPP,j}}{\delta C_{R,2,j}} - \frac{\delta F_{C,NPP,j}}{\delta C_{R,1,j}} \right] \quad (32)$$

Where  $H$  is the Heaviside Step Function, the value of which is zero for a negative argument and one for a positive argument. Partial derivatives in Eqs. (30)–(32) are readily evaluated from analytically differentiating  $F_{C,NPP,j}$  with respect to each plant carbon pool.







0.0833° resolution (8 km) to 0.05° (5 km). NDVI values from 0.1 (bare ground) to 0.75 (full cover) were linearly rescaled between 0 and 1 to represent vegetation fractional cover. For calibration, we used 2000–2013 data at the locations of the flux sites (Table 1).

### 5 3.2.2 Validation data

For model evaluation, we used predictive empirical models describing the decline of basal area and projected foliage cover with rainfall, developed by Williams et al. (1996) from a data-set of ~ 1000 quadrats (each 20 m × 20 m) lying north of 18° S within the Northern Territory. We also utilized observations reported by Sea et al. (2011) of dry-season (September 2008) tree leaf area index (LAI) based both on digital hemispheric photography (DHP) and the MODIS Collection 5 (MODC5) remote-sensing LAI product. Additionally we used monthly fPAR (as described in *Calibration Data* above) along the entire rainfall gradient.

## 4 Model–data fusion

15 We calibrated HAVANA parameters by optimisation against monthly observations of ET, GPP and fPAR, subject to prior constraints. The search algorithm was the Levenberg–Marquardt method implemented in the PEST software package (Doherty, 2004). The cost function to be minimised was the weighted sum of squared residuals,  $\Phi = \sum_i w_i^2 r_i^2$ , where the residual  $r_i$  can be either the residual between a model  
20 prediction and corresponding observation, or the residual between prior and posterior variables. Relative observation weights ( $w_i$ ) were set such that each observation data type and each prior constraint contributed equally to the prior cost function.

Prior constraints consisted of estimates of leaf and fine-root carbon pools at Howard Springs. We assume prior estimates of time-averaged leaf carbon to be 50 and  
25 100 g C m<sup>-2</sup> for grassy and woody vegetation respectively, and a ratio of time-averaged

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5 fine root mass to leaf mass of 2. Leaf carbon estimates are based on Chen et al. (2003). The ratio of fine root to leaf mass is a very rough estimate, as estimates of peak fine root mass in Northern Australian tropical savannas are divergent: 1800 g C m<sup>-2</sup> (Janos et al., 2008); 50 g C m<sup>-2</sup>; 140 g C m<sup>-2</sup> (claimed to be a factor of 10 too low by Janos et al., 2008).

## 5 Results

### 5.1 Calibration

We assessed the calibrated HAVANA predictions of monthly fluxes of ET and GPP, and monthly mean remotely-sensed fPAR. Time series of the three modelled variables  
10 for each flux site are shown in Fig. 3 as coloured patches, with colour coding to represent the flux-partitioning between transpiration from upper and lower soil and soil evaporation (ET) and between tree and grass components (fPAR and GPP). The observed quantities are also shown along with a benchmark, being a state-of-the-art biogeochemical land surface model (CABLE, as implemented in BIOS2, Haverd et al.,  
15 2013a), forced using LAI derived from the GIMMS-3g fPAR product (Zhu et al., 2013), and calibrated here against GPP and ET from the five flux sites. ET, fPAR and GPP determined from HAVANA-POP increasingly matched observations toward the northern end of the NATT, where a more predictable seasonal cycle was observed than at the southernmost semi-arid site (Fig. 4). Even without being supplied external vegetation cover information, our new HAVANA model performed equally well or better  
20 than the benchmark (BIOS2) for monthly GPP and ET, as illustrated by slightly larger R<sup>2</sup> values and slightly smaller RMSE scores (Fig. 4). There was a tendency in HAVANA and BIOS2 to under-predict ET (slope > 1), whereas the modelled range in GPP closely matched the observed range (Fig. 4). While ET, and to a lesser extent GPP, was under-predicted by BIOS2 at Howard Springs, the bias was not apparent in the  
25 HAVANA results (Fig. 4). Both models over-predict the small values of ET and GPP at

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the Alice Springs site (Fig. 4). HAVANA soil evaporation is a small proportion of ET at all sites.

## 5.2 Evaluation

We evaluated the performance of HAVANA-POP along the entire rainfall gradient (Fig. 5). Each model point represents a spatial average across ~ 65 points lying within a latitude bin of width  $0.57^\circ$ , with error bars representing one standard deviation. The model replicates observed variations with rainfall of GPP, foliage projective cover, tree basal area and dry season tree LAI along the transect. Modelled tree foliage projective cover is higher than the observation-based estimates by about 0.06. This likely reflects a bias between the observation-based estimates, and the satellite-based fPAR that was used for calibration.

## 5.3 HAVANA dynamics along the NATT

Figure 6a and b illustrates the dynamics of key HAVANA variables from north (top row) to south (bottom row) along the NATT. Soil moisture (Fig. 6a(i)) shows strong seasonality in the top layer, which is smoothed out in the lower layer, resulting in respective seasonal and persistent transpiration (root water extraction) from the two layers (Fig. 6a(ii)). This leads to woody vegetation cover persisting throughout the year (Fig. 6a(iii–iv)) and only small seasonal fluctuations in associated GPP (Fig. 6a(v)), compared with grassy vegetation cover, which is completely absent by the late dry season. The decline in fPAR southward along the NATT accords well with satellite observations (Fig. 6a(iv)), as does the interannual variability which is largely absent at the northern end of the NATT, and clearly evident below 970 mm MAP.

Grassy vegetation is characterised by significant temporal shifts in NPP and growth, leading to large changes in the NSC store (Fig. 6b(i)). This ability for growth to draw on NSC reserves is critical for rapid production of resource uptake surfaces (leaves and roots) at the beginning of the wet season (Fig. 6b(iii)). The change in storage flux (rela-

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tive to NPP) increases down the transect as both woody and grassy vegetation become more reliant on the NSC pool for growth in times of stress (Fig. 6b(i, ii)). For grass, root carbon increases with aridity relative to leaf carbon. This is less evident for woody vegetation, because leaf carbon in woody vegetation is also influenced by a gradient in specific leaf area (Eq. 38). Allocation patterns for grass (Fig. 6b(v)) show an increasing fine root component as aridity increases down the transect, with temporal dynamics dictated by whether fine roots or leaves are limiting NPP (Eqs. 30–31). (These are monthly-averaged C-allocation coefficients, which don't necessarily sum to one because allocation coefficients are zero when growth is zero.) For trees (Fig. 6b(vi)), allocation to surface roots occurs in the early wet season, when soil moisture in the upper layer exceeds that in the lower layer. Thus tree and grass roots compete in the surface layer. When soil moisture is plentiful (e.g. 2011), root growth is small and the remainder is partitioned between stems and leaves (Fig. 6b(vi)). Leaf carbon is constrained by sapwood area (Eq. 33), leading to periods of high allocation to stems in wet periods.

## 6 Discussion

There is ongoing debate about the mechanisms governing tree and grass cover and maintaining the stability of savanna ecosystems relative to grassland or closed woody ecosystems (Bond, 2008; Torello-Raventos et al., 2013). While it is widely acknowledged that both resource limitation (especially water) and disturbance (fire and grazing) may control tree cover, their roles differ along environmental gradients and between continents (Africa, Australia, and South America), to the extent that Lehmann et al. (2014) claimed that “a single model cannot adequately represent savanna woody biomass across these regions”. Sankaran et al. (2005) found woody carrying capacity in African savannas to be limited by rainfall, but that savannas were typically held below woody carrying capacity by fire or grazing. Supporting the influential role of disturbance, Bond et al. (2005) used a dynamic vegetation model to infer that fire suppres-

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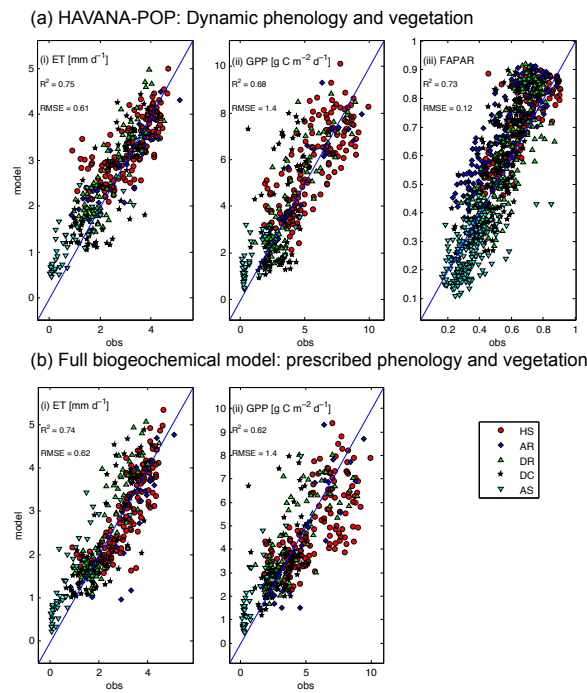






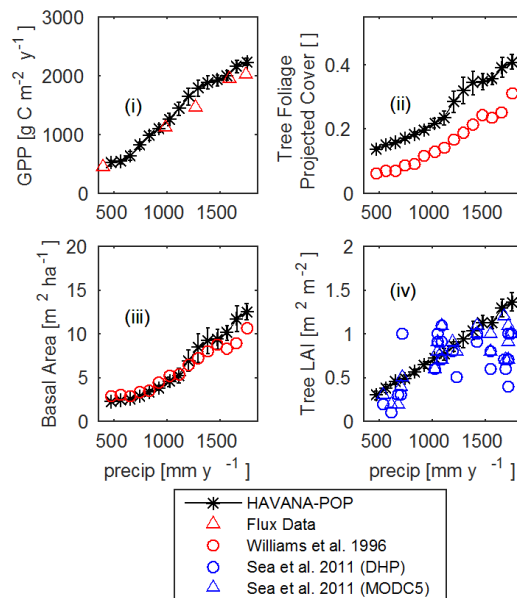






**Figure 4.** Scattergrams of model predictions vs. observations of monthly values at 5 Flux Sites of (i) ET; (ii) GPP; (iii) fPAR. **(a)** HAVANA-POP and **(b)** CABLE in BIOS2, a full biogeochemical model with prescribed phenology and vegetation cover.

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**Figure 5.** Time-averaged (1964–2013) HAVANA-POP output variables: variation with rainfall and comparison with observation-based estimates. (i) Gross primary production (combined tree and grass components) and comparison with mean annual GPP from flux data (averaged over observation period); (ii) Annual average tree foliage projected cover and comparison with Williams et al. (1996); (iii) tree basal area and comparison with Williams et al. [1996]; (iv) Dry season tree LAI (September 2008) and comparison with Sea et al. (2011) estimated from digital hemispheric photography (DHP) and the MODIS Collection 5 product (MODC5).

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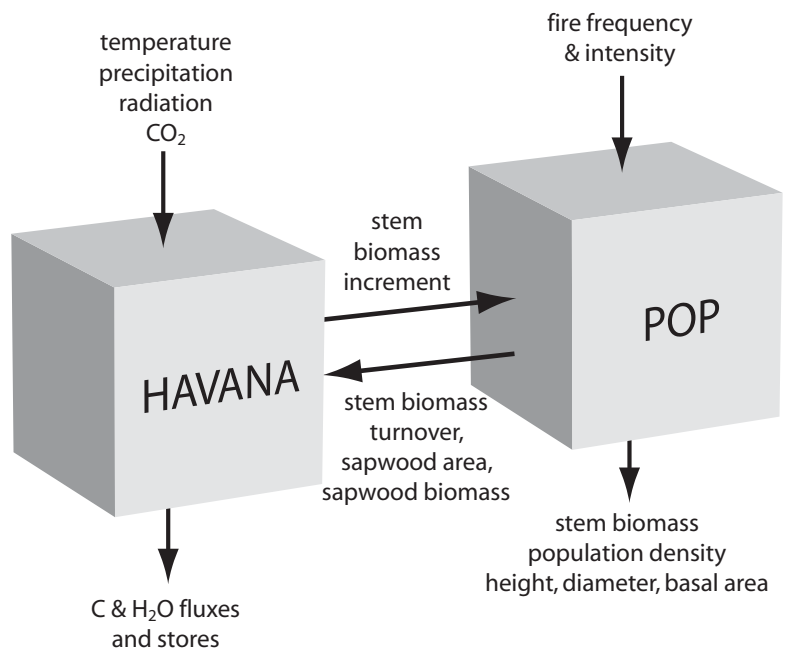


Figure A1. HAVANA-POP coupling.