

Dynamic Pattern Formation in Electron-Beam-Induced Etching

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We report highly ordered topographic patterns that form on the surface of diamond, span multiple length scales, and have a symmetry controlled by the precursor gas species used in electron-beam-induced etching (EBIE). The pattern formation dynamics reveals an etch rate anisotropy and an electron energy transfer pathway that is overlooked by existing EBIE models. We, therefore, modify established theory such that it explains our results and remains universally applicable to EBIE. The patterns can be exploited in controlled wetting, optical structuring, and other emerging applications that require nano- and microscale surface texturing of a wide band-gap material.

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Electron-beam-induced etching (EBIE) [1,2] is a high-resolution, single-step, direct-write nanofabrication technique in which a precursor gas and an electron beam are used to realize etching. To date, EBIE has been used to study electron interactions with solids and adsorbates and to machine a wide range of materials using etch precursors such as oxygen, water, ammonia, nitrogen trifluoride, xenon difluoride, and chlorine. The key advantages of EBIE include site specificity, the absence of staining and severe damage inherent to focused ion beam techniques, and the ability to etch materials such as diamond which are resistant to conventional chemical etch processes. Consequently, EBIE has recently been used to realize practical device components for use in photonics [3], plasmonics [4], and nanofluidics [5].

In this Letter, we report dynamic, highly ordered topographic patterns that form spontaneously on the surface of diamond during EBIE. Pattern formation is a ubiquitous process that provides fundamental insights into the roles of symmetry breaking, anisotropy, and nonlinear interactions in emergent phenomena [6–8]. Here it reveals a chemical etch rate anisotropy that cannot be explained by established EBIE theory. We, therefore, propose a fundamental modification, whereby the critical role of energetic electrons is to transfer energy to surface atoms of the solid rather than to surface-adsorbed precursor molecules. The new EBIE model is confirmed experimentally, explains the observed patterns, and resolves long-standing problems that have been identified in the EBIE literature.

Figure 1(a) is a schematic illustration of EBIE performed using H₂O precursor gas. Figure 1(b) shows images of topographic patterns that form on the surface of single-crystal (001)-oriented diamond during H₂O EBIE performed at room temperature [9]. A movie showing the pattern formation and evolution dynamics is provided as Supplemental Material [9] Video 1. The patterns were

observed over a wide range of electron-beam energy and flux of 2–10 keV and 10¹⁷–10²² cm⁻² s⁻¹, respectively. The etching initiates at scratches and other surface defects, which expand laterally during EBIE, evolving into highly symmetric rhombohedra such as the large pit seen in the top left corner of Fig. 1(b). Similarly, the topography that is normally associated with surface roughness caused by EBIE rapidly evolves into step edges with {110} sidewalls which propagate laterally until they reach the edge of the area scanned by the electron beam. The {111} family of planes is absent from the resulting surface topography, the step sidewalls are comprised of {110} planes, and 90° step corners are formed at the intercepts of the {110} planes. Corner formation requires the (110), ($\bar{1}$ 10), ($\bar{1}$ $\bar{1}$ 0), and (1 $\bar{1}$ 0) planes to etch slower than the (100), (010), (0 $\bar{1}$ 0), and ($\bar{1}$ 00) planes. From these observations, we conclude that H₂O-mediated EBIE removes material from the {100} and {111} planes faster than from the {110} family of planes.

In order to prove conclusively that the proposed anisotropy yields the fourfold symmetry observed in Fig. 1(b), we used a 3D implementation of the level set method (LSM) [33]. LSM is a robust technique for evolving implicit surfaces under anisotropic velocity fields. It can be used to calculate surface shapes produced by anisotropies defined by differences between the etch rates of specific crystal planes. The simulations [9] reveal that the calculated surfaces match the experiment only if the {110} planes that are oriented at 90° with respect to the electron-beam axis etch slower than all other planes. Stable patterns are produced if the etch rate of the slowest etching planes to the remaining planes is at least 1:5. Supplemental Material [9] Video 2 and Fig. 1(d) show the resulting rhombohedral surface features.

Validity of the simulation was confirmed by applying the same etch rate anisotropy rule set to (111)-oriented diamond. The simulation and H₂O EBIE both produced the

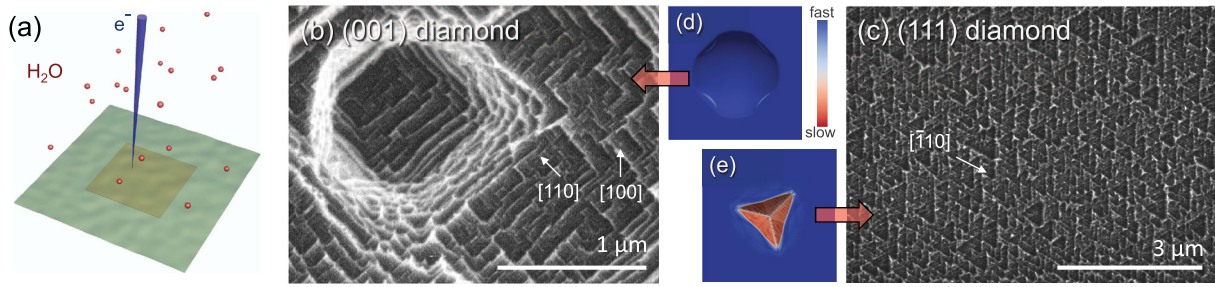
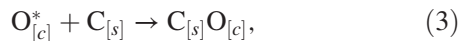
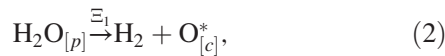


FIG. 1 (color). Topographic patterns formed during H_2O -mediated electron-beam-induced etching of single-crystal diamond performed using a beam energy of 5 keV and a current of 34 nA. (a) Schematic illustration of H_2O EBIE. (b) Expanding rhombohedra formed on the surface of (001)-oriented diamond and (c) trigons on the surface of (111) diamond. (d), (e) Corresponding simulated rhombohedra and trigons (colored by the relative local etch rate) that are expected if the $\{110\}$ planes are the slowest etching planes.

trigons with $\{110\}$ sidewalls shown in Figs. 1(c) and 1(e). The LSM simulations, therefore, support our conclusion that the geometries of patterns observed during H_2O EBIE of (001)- and (111)-oriented diamond is governed primarily by slow etching of specific $\{110\}$ planes. However, this anisotropy cannot be explained by conventional, established EBIE theory which is based on the assumption that the key role of energetic electrons is to dissociate physisorbed precursor molecules (e.g., H_2O) and, thus, generate reactive fragments (O^*) which react with surface atoms (C) to produce volatile molecules (CO) that desorb spontaneously, giving rise to localized chemical etching. In the specific case of H_2O EBIE of diamond, a possible pathway in this framework is the following [1,2]:



where the subscripts $[v]$, $[s]$, $[p]$, and $[c]$ signify vapor phase, solid phase, physisorbed, and chemisorbed species, respectively. Reactions (1)–(4) represent adsorption of H_2O precursor molecules from the gas phase, dissociation of the adsorbates into fragments, bonding of oxygen fragments to the diamond surface, and desorption of CO, respectively (desorption of H_2 is not shown). Ξ_1 represents the energy barrier for dissociation of H_2O , and Ξ_2 is the binding energy of the reaction product. According to the standard EBIE model, Ξ_1 and Ξ_2 are overcome by a transfer of kinetic energy from the electrons that drive EBIE and thermal energy of the substrate (kT), respectively. This model has been used to explain a wide range of experiments such as dependences of etch rates on time, beam current density, and pressure of the precursor gas [2,5,34–44]. However, the model cannot explain the etch rate anisotropy

seen in Fig. 1, unless different crystal planes give rise to significant variations in the electron dissociation cross section of H_2O adsorbates, the secondary electron emission yield, or the local coverage of precursor molecule adsorbates. None of these are plausible since the precursor is H_2O , the patterns form at room temperature (and at elevated temperatures, as is discussed below), and the slowest etching planes are not consistently dark in secondary electron images.

To resolve the above issues, we propose a new mechanism, which proceeds through reactions (1)–(4), but electrons provide the energy Ξ_2 in reaction (4). Hence, the critical role of electrons is not to dissociate physisorbed precursor molecules but to break bonds that bind surface atoms to the substrate and, thus, enable the desorption of the reaction products. During etching, reaction (2) can reasonably be expected to proceed spontaneously since active (i.e., unterminated) surface sites are generated continuously during EBIE, and the interaction of H_2O molecules with a bare diamond surface results in spontaneous decomposition of H_2O [45] and formation of oxygen terminated sites. In this framework, the etch rate anisotropy needed to produce the patterns seen in Fig. 1 is not surprising since Ξ_2 (i.e., the C—C bond properties and the corresponding cross section for scission by electrons) is expected to vary with the crystal plane.

To confirm the proposed EBIE mechanism, we performed an experiment based on the fact [46] that the C—C bonds are modified by hydrogen which reconstructs and stabilizes the $\{111\}$ surface. We, therefore, performed H_2O EBIE of (001)- and (111)-oriented diamond in the presence of NH_3 gas, where the role of the NH_3 is to supply an excess of hydrogen radicals to terminate the (111) planes. Figure 2 shows that the corresponding surface patterns consist of inverted pyramids and trigons, respectively and that these geometries are indeed expected from LSM simulations in which the $\{111\}$ planes are the slowest etching planes.

We performed one more experiment to further test the proposed EBIE mechanism. A consequence of the conventional EBIE model is that the etch rate should be directly

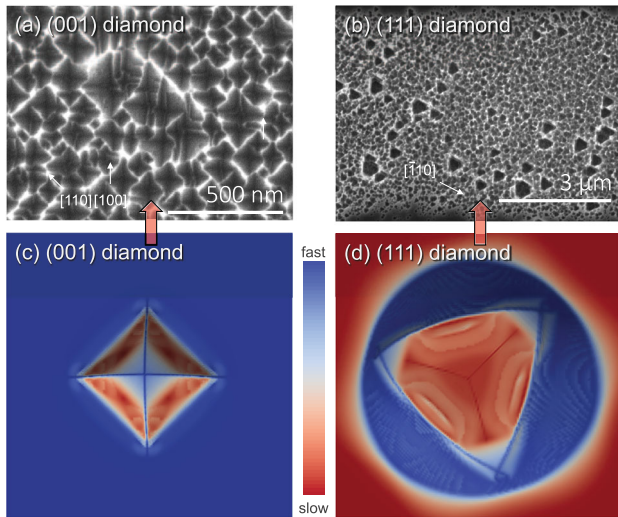


FIG. 2 (color). Topographic patterns formed during electron-beam-induced etching of single-crystal diamond in the presence of NH_3 (the electron-beam parameters were the same as in Fig. 1). (a) Expanding inverting pyramids formed on the surface of (001)-oriented diamond and (b) trigons on the surface of (111) diamond. (c), (d) Corresponding simulated pyramids and trigons (colored by the relative local etch rate) that are expected if the $\{111\}$ planes are the slowest etching planes.

proportional to the coverage of H_2O [1,2] which is $\sim 4 \times 10^{-1}$ and 6×10^{-3} monolayers at 298 and 400 K, respectively, due to the temperature dependence of the thermal desorption rate of H_2O . Hence, the etch rate of diamond is expected to be negligible at ~ 400 K, as is shown in Fig. 3 (solid curves calculated using the rate equation model presented in the Supplemental Material [9]). However, the measured etch rate is approximately independent of temperature up to at least 600 K where it is over 3 orders of magnitude higher than that predicted by the conventional EBIE model, irrespective of the electron flux used in the simulations (the simulated flux was varied over 5 orders of magnitude because it affects adsorbate depletion and, hence, the predicted temperature dependence of EBIE [1,34]). The measurement is clearly inconsistent with the conventional model, but it is expected from the new model in which the etch rate is proportional to the concentration of chemisorbed oxygen. The lack of a temperature dependence, therefore, serves as direct evidence for the new EBIE model. Furthermore, the topographic patterns were observed at all temperatures that were investigated, as is illustrated by the image shown in the inset of Fig. 3. The abrupt step edges in the patterns generated at ~ 600 K are inconsistent with any model that attempts to explain the etch rate anisotropy by spatial variations in the coverage of physisorbed adsorbates.

We note that the new EBIE model is consistent with all results in the literature that were explained successfully by the conventional EBIE model [1,2,5,34–44,47]. The scaling of the etch rate with beam energy is the same because the

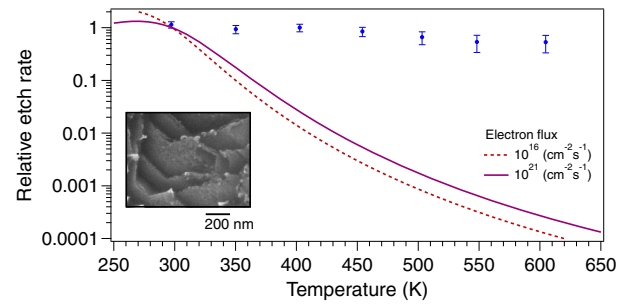


FIG. 3 (color online). Temperature dependence of the rate of EBIE measured experimentally (points) and calculated using the established EBIE model [9] (lines) using a wide range of electron fluxes. The etch rates are normalized to the EBIE rate at room temperature where the measured etch rate is $\sim 10^{-3} \mu\text{m}^3 \text{s}^{-1}$. The inset shows an image of surface topography generated by H_2O EBIE at ~ 600 K. EBIE experiments were performed using a beam energy of 5 keV and an electron flux of $\sim 8 \times 10^{17} \text{cm}^{-2} \text{s}^{-1}$.

secondary electron yield is proportional to the energy transferred from the beam to the surface atoms of the substrate. The beam current density and pressure play the same roles in the two models because both the physisorbed, and chemisorbed adsorbates are consumed in EBIE and replenished through the same mechanisms (namely, adsorption from the gas phase and surface diffusion). Electron-induced desorption of adsorbates plays the same role in each model [9,34], and electron dose and time dependences of the etch rate are governed by the kinetics of the respective adsorbate concentrations. However, the new model provides a more compelling explanation for EBIE observed at cryogenic temperatures [35] since it does not require thermal desorption of the reaction products. Moreover, the new model is unique in being consistent with reports of UV-laser-induced etching of diamond that is believed to proceed through a two-photon C—C bond scission mechanism [8]. The new model also provides a satisfactory explanation for the fact that single-crystal diamond can be etched by EBIE in the first place. The energy barrier of reaction (4) in diamond is known to be significant [48], and, therefore, the etching observed at room temperature or any temperature below the onset of defect generation and graphitization cannot be accounted for in the standard model.

Finally, we note that anisotropic wet etching of diamond proceeds through a graphitization pathway, and the etch rate is limited by the anisotropic graphitization rate. However, the topographic patterns reported here cannot be explained by analogous damage generation mechanisms or those encountered in conventional dry etch processes [49,50] for a number of reasons. First, the EBIE rate anisotropy was modified significantly by the presence of NH_3 gas, which should not change the subsurface damage generation rate. Second, pattern formation was either modified or suppressed entirely if residual hydrocarbon contaminants were present on the etched surface. Such

contaminants are common in electron microscopes, alter the surface termination during EBIE, and give rise to a competing process of electron-beam-induced deposition of carbon [1]. The contaminants likely account for the fact that patterns have not been reported in prior EBIE literature (here, we suppressed contamination using the sample cleaning procedure detailed in the Supplemental Material [9]). Third, prior studies of EBIE of single-crystal diamond have failed to produce any evidence of damage by photoluminescence and Raman spectroscopy [3,43,51,52]. Fourth, the generation rate of damage produced by a 5 keV electron beam scales with the local energy density deposited into the substrate throughout the electron interaction volume [47]. The damage generation rate is, therefore, isotropic, except for special cases where the electron-beam axis is parallel to a channeling axis, which should produce a strong dependence of the patterns on sample tilt, which was not observed in our experiments. We, therefore, conclude that subsurface damage generation does not play a role in the observed etching and pattern formation behavior.

To summarize, we showed several novel dynamic pattern formations on the surface of single-crystal diamond. We proposed an amended model for the EBIE process that is based on interactions of electrons with the substrate rather than the precursor molecule adsorbates. Our results can be leveraged to engineer surface patterns controlled by electron-beam irradiation conditions.

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