

# Condition assessment of timber utility poles based on a hierarchical data fusion model

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**Abstract:** This paper proposes a novel hierarchical data fusion technique for the non-destructive testing (NDT) and condition assessment of timber utility poles. The new method analyses stress wave data from multi-sensor multi-excitation guided wave testing using a hierarchical data fusion model consisting of feature extraction, data compression, pattern recognition and decision fusion algorithms. The proposed technique is validated on guided waves at a set of in-situ timber poles. The actual health states of these poles are known from autopsies conducted after the testing, forming a ground-truth for supervised classification. In the proposed method, a data fusion level extracts the main features from the sampled stress wave signals using power spectrum density (PSD) estimation, wavelet packet transform (WPT) and empirical mode decomposition (EMD). These features are then compiled to a feature vector via real-number encoding and sent to the next level for further processing. Principal component analysis (PCA) is also adopted for feature compression and to minimise information redundancy and noise interference. In the feature fusion level, two classifiers based on support vector machine (SVM) are applied to sensor separated data of the two excitation types and the pole condition is identified. In the decision making fusion level, the D-S evidence theory is employed to integrate the results from the individual sensors obtaining a final decision. The results of the in-situ timber pole testing show that the proposed hierarchical data fusion model was able to distinguish between healthy and faulty poles demonstrating the effectiveness of the new method.

**Author Keywords:** Condition assessment, timber poles, hierarchical fusion, support vector machine, D-S evidence theory, non-destructive testing

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## Introduction

Timber utility poles are used all over the world for power and communication distribution due to their low cost and practicality. In Australia, an estimated number of more than seven million timber poles form part of the country's infrastructure (Nguyen et al. 2004). Among these, about five million poles are used for communication and power supply and are worth more than \$10 billion. For pole management and maintenance, the Australian government spends every year approximately \$50 million to ensure reliability of the network and to avoid potentially disastrous pole failures. The conventional methods for pole assessment are sounding, visual inspection and core drilling (Tansasoiu et al. 2002). These methods, however, are subjective techniques, which highly depend on the experience and skills of the inspector. More importantly, none of these methods are able to provide reliable assessment of the underground sections of the poles, which are indeed the most critical and vulnerable in terms of structural safety. These drawbacks severely compromise the inspection and maintenance management of timber poles. According to (Nguyen et al. 2004), around 30,000 electricity poles are annually substituted in the Eastern States of Australia, although more than 80% of the substituted poles still maintain in a healthy condition, resulting in a large waste of natural resources and money. In addition, research studies have shown that while the present averaged serviceable lifespan of timber utility poles is around 35 years, the life expectancy can be prolonged to more than 75 years if appropriate maintenance and inspection techniques are adopted (Stewart 1996).

In the last two decades, various NDT techniques have been developed to evaluate the integrity and condition of pile structures such as deep foundation piling. Among these techniques, stress wave methods based on guided wave testing such as the impulse response (IR) method (Davis and Dunn 1974), the sonic echo (SE) method (Paquet 1968; Steinbach and Vey 1975; Lin et al. 1991; Van and Middendorp 1980) and the bending wave (BW) method (White and Ross 2014; Qian and Mita 2005) are well established in the pile testing industry. For these tests, an excitation force is applied and the structural responses are measured using a sensor installed on the top of pile structure. By analysing the reflexogenic signals, the health condition of the pile including the underground section can be evaluated. Although some of these stress wave methods have been adopted for the condition assessment of timber poles, most of this work is research-based and many

challenges still have to be overcome before accurate and reliable assessment can be achieved (Dackermann et al. 2014a; Krause et al. 2014; Li et al. 2012; Subhani et al. 2013). These challenges include complicated wave propagation in timber, related to the complexity of the timber material with anisotropic characteristics and uncertainties from natural defects and deterioration, as well as unknown soil conditions and environmental factors such as temperature and moisture fluctuations influencing the wave propagation. As a result, traditional and newly developed signal processing methods often fail to fully interpret wave patterns and to produce accurate and reliable condition assessment. Challenges further stem from practical field testing conditions, where sensor measurements are influenced by noise submerging the actual wave propagation information. Furthermore, if testing data originates only from one source, it is non-inclusive and may be subject to errors from operators and environmental factors. Hence, to achieve comprehensive and reliable pole assessment, multiple types of signals should be recorded and analysed. Furthermore, using a multi-sensor system instead of only a single sensor or device can facilitate the higher identification accuracy. In such case, however, sensors installed at different positions of the pole may result in conflicting assessment results, making a final decision difficult.

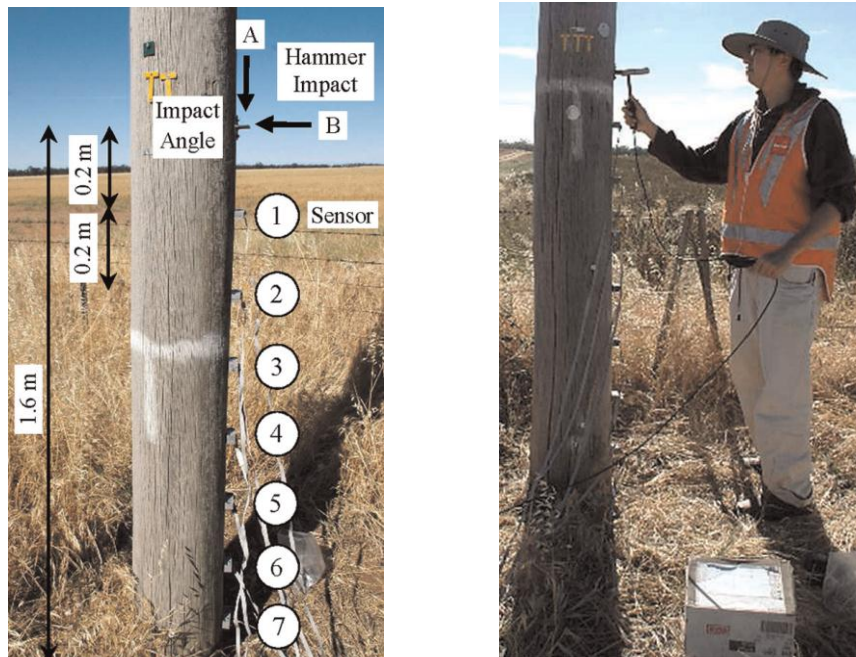
Aiming at solving some of the challenges above, this paper proposes a novel hierarchical data fusion model, combined with multi-sensor and multi-excitation guided wave testing, to analyse stress wave signals for the condition assessment of timber poles. In the data analysis level, power spectrum density (PSD) estimation, wavelet packet transform (WPT) and empirical mode decomposition (EMD) are used to extract signal features from the stress wave data. Next, a feature vector is formed, which is fed into a support vector machine (SVM) classifier for pattern recognition. In order to enhance the classification accuracy and prevent a slow convergence rate, a genetic algorithm (GA) is employed to optimize the classifier parameters. Furthermore, the sigmoid function is adopted to transform the standard outputs of SVM into the confidence probability, realizing the objective assignments of basic probability assignment function. In the decision level, the D-S evidence theory is adopted to fuse the initial identification results from different sensors in the testing system and to make a final decision. In-situ field testing data is used to verify the feasibility and performance of the proposed hierarchical model.

The remainder of this paper is organized as follows: the second section gives background information on the field testing and the hierarchical data fusion model; in the third section, the related data analysis algorithms are described in detailed together with feature analysis and model setup of the stress wave signals. The fourth section presents the performance results of the proposed model for condition assessment of timber poles using the experimental field data. Finally, a conclusion is drawn in the last section.

## **Guided wave testing and hierarchical data fusion model**

### ***Guided wave testing***

To validate the proposed method, guided wave testing was conducted on eight in-situ timber poles that were scheduled for decommissioning. After the testing, the poles were dismembered to determine their actual health states. For the guided wave testing, an impact hammer, seven accelerometers and a data acquisition system were employed. The experimental field setup is depicted in Fig. 1. For the testing, a hammer impact was induced at a height of 1.6 m in either longitudinal direction (using an impact angle) to generate primarily longitudinal waves or in transverse direction to generate bending waves. The impact hammer used was a PCB model HP 086C05 of sensitivity 0.24mV/N. The responses of the pole were captured by an array of sensors, which were installed on the side of the pole with a uniform spacing of 0.2 m as illustrated in Fig.1 (a). The sensors were low cost dual-axis piezoresistive accelerometers of model ADXL320, with a sensitivity range between 154 and 194 mV/g and a frequency bandwidth from 0.5 to 2.5 kHz. All the sensors were embedded within the plastic cases, which were drilled to the tested poles. The data acquisition system was a mid-range 8 channel system with 13-bit 4M sample/second per channel of model NI PCI-6133. For the testing, the sampling frequency was set to 1 Hz with 0.2 s sampling time. Each test was repeated five tests, i.e. for each pole five hammer strikes were executed in longitudinal direction and five in transverse direction. More details on the conducted experimental setup and testing can be found in (Dackermann et al. 2014b).



(a) Experimental field setup (b) Testing execution

Fig. 1. Experimental field setup and guided wave testing execution

### ***Hierarchical data fusion model***

The proposed hierarchical data fusion model is shown schematically in Fig.2. This model is divided into three analysis levels, i.e. a data level, a feature level and a decision level. In the first level, dominate signal features are extracted minimising information redundancies and disturbances such as environmental noise and wave dispersion. In this level, three different signal processing methods (PSD, WPT and EMD) and PCA are employed to isolate information sensitive to the health condition of the pole structure. In the second level, a state-of-the-art SVM classifier is constructed to intelligently analyse these feature parameters, facilitating the initial evaluation of the pole condition. In the third level, influences from different sensor locations, excitation types and training samples on the condition assessment are addressed. Here, according to the probability outputs of the SVM, the basic probability assignment (BPA) of each proposition of the pole condition discernment frame is obtained. The initial recognition result can be regarded as independent evidence and all results including conflicting evidences are combined using evidence combination rule, solving the problem of conflicting and inaccurate identification of the pole condition using only one SVM

classifier. The entire model employs a hierarchical structure, in which the results from the former level are used as the inputs for the next level. Accordingly, this method can separately realize multiple levels of information processing, guaranteeing the robustness and accuracy of assessment results.

## Methodology

### Data level fusion based on multi-feature extraction

Stress-wave-based condition assessment of timber poles is essentially a pattern recognition problem. Hence, signal feature extraction is a key element in the data processing and its performance is closely related to the accuracy of the final assessment results. While there are many feature extraction methods available, each approach has its limitations. Therefore, in the proposed method, three different analytical methods are employed in parallel to extract key features of the stress wave signals, i.e. PSD (Gangopadhyay et al. 1989), WPT (Sun and Chang 2002) and EMD (Huang et al. 1998).

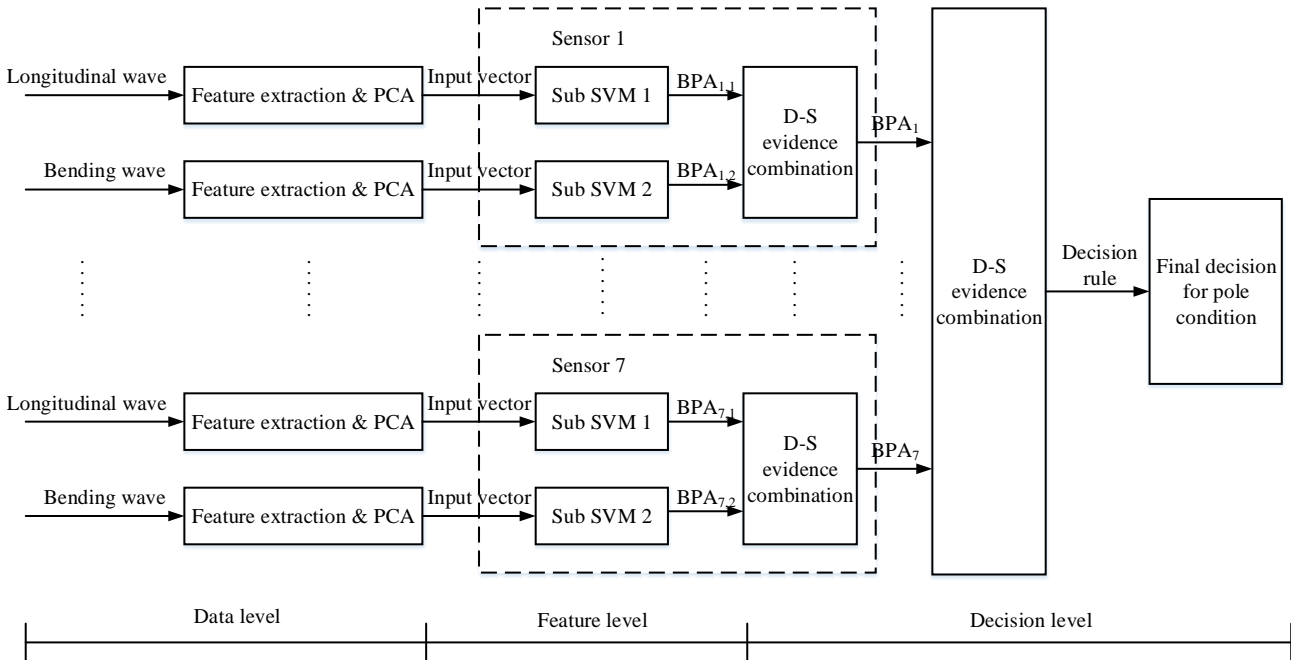


Fig. 2. Hierarchical data fusion model for pole condition assessment

142 Power spectrum density (PSD) feature extraction

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144 Typical stress wave signals captured from guided wave testing have nonlinear and random characteristics  
145 and are polluted with noise. These characteristics can be seen in Fig. 3, which displays stress wave signals of  
146 one intact pole from sensor 1 with longitudinal and bending wave excitations. Generally, PSD estimation is  
147 an effective way to analyse this type of signals. Up to present, various signal PSD estimation techniques have  
148 been reported including parametric and nonparametric methods. Compared with nonparametric methods,  
149 parametric ones are apt to provide better results especially when the analysed signal length is relatively short,  
150 which is always regarded as short quasi-stationary sequence. In this work, a parametric approach using  
151 autoregressive (AR) coefficient estimation is utilised to transform the time-series stress wave signals into a  
152 series of real-valued variables based on the assumption that signals can be obtained from a time-series model  
153 of a random process. As well, AR model is able to model stress wave signals as the output of a linear m-  
154 order AR model combined with zero-mean Gaussian white noise and its specific expression is given by  
155 (Fugate et al. 2001):

156 
$$y(n) = -\sum_{i=1}^m a(i)y(n-i) + e(n) \quad (1)$$

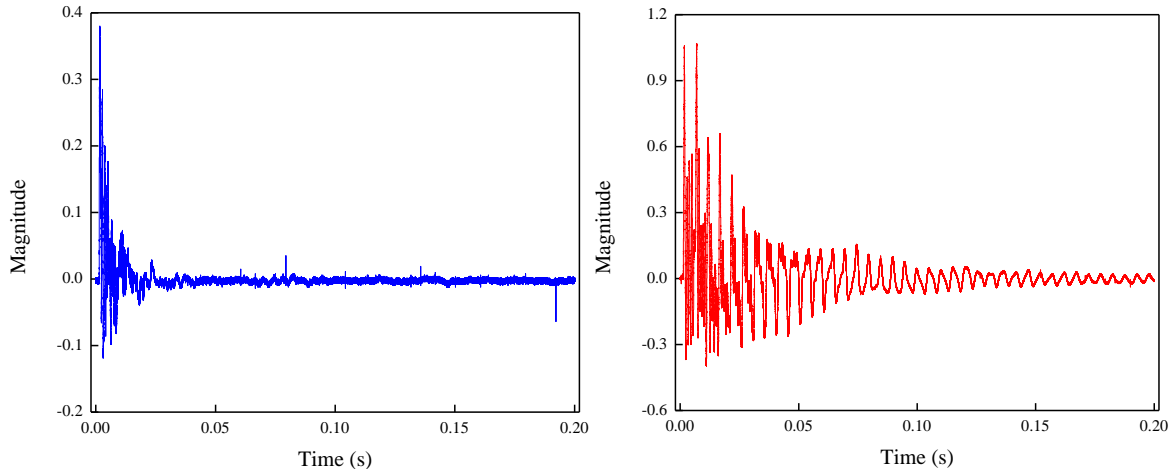
157 where  $y(n)$  is the discrete time-history response that model the stress-wave signals,  $a(i)$  is an AR coefficient  
158 and  $e(n)$  is the time-series sequence of a Gaussian white noise process.

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160 The Burg method is utilized here to estimate the AR parameters of the signals, which is mainly based on  
161 Levinson-Durbin recursion and least square criterion. The order  $m$  in the AR model is an important  
162 parameter to be identified from the signals and describes a trade-off relationship between adding resolution  
163 and declining model accuracy. Here, the trial-and-error method is used to identify the optimal model order  
164 via minimizing the Akaike information criterion (AIC) function (Marple 1987):

165 
$$\min \quad AIC[m] = N \cdot \ln(\tau) + 2m \quad (2)$$

166 where  $m$  denotes the model order of the AR system,  $N$  denotes the total number of sampling points, and  $\tau$   
167 denotes the variance estimation of the white noise input to the AR model for order  $m$ .

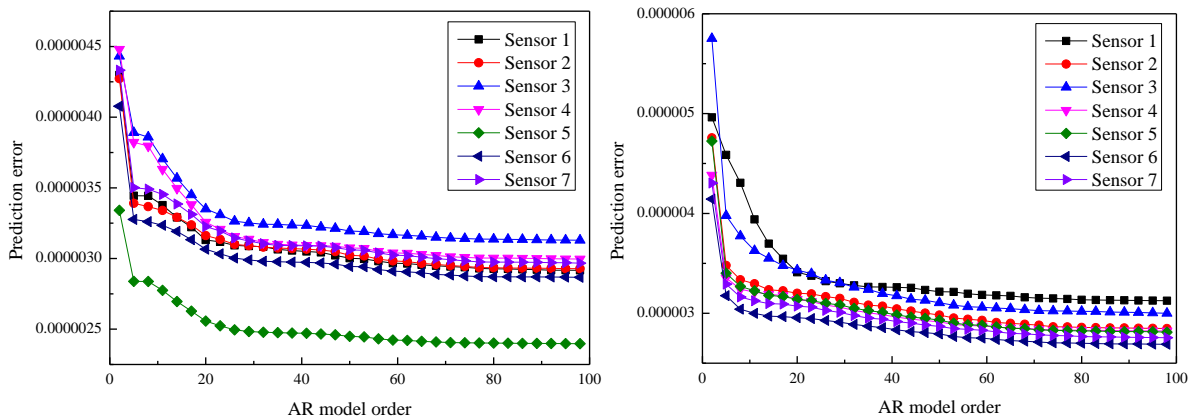


(a) Longitudinal wave excitation

(b) Bending wave excitation

Fig. 3. Typical stress wave signals of an intact pole from sensor 1.

Fig. 4 shows the relationship between variance estimation and AR model order for both longitudinal and bending waves obtained from the sensor array. It can clearly be observed that the variance estimation shows a decreasing trend with an increasing model order. This decreasing trend reduces once the order exceeds the knee points. In general, a higher order will lead to a high-dimensional feature vector which may influence the classification accuracy of the SVM. Therefore, the knee points of AIC curves are selected as the optimal order in this work, i.e.  $m=20$  for longitudinal wave and  $m=17$  for bending wave excitation.

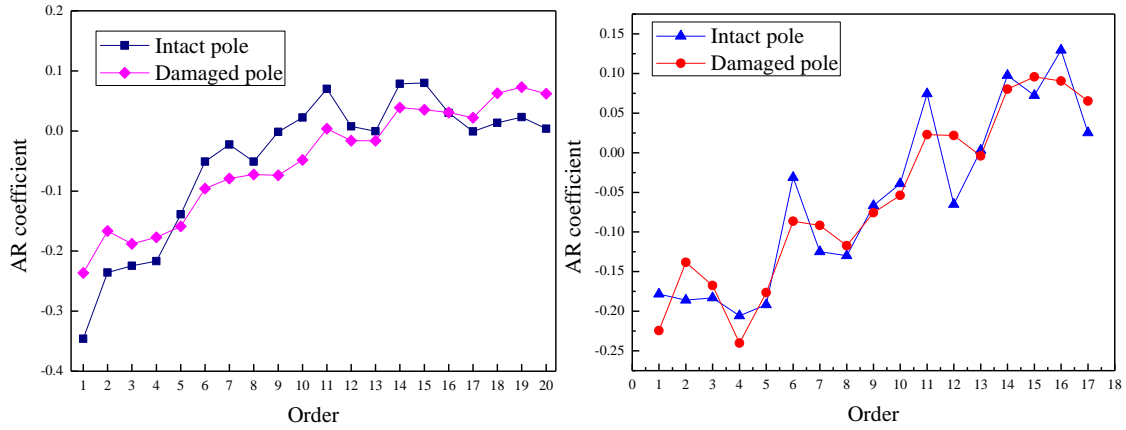


(a) Longitudinal wave data (b) Bending wave data

Fig. 4. Mean AIC responses



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(a) Longitudinal wave data

(b) Bending wave data

Fig. 5. AR coefficients for both intact and damaged poles

Fig. 5 shows a typical case of the resulting AR coefficients calculated using the parametric method for longitudinal and bending wave signals for an intact and a damaged timber pole. These results show that only tiny AR coefficient differences can be found between intact and damaged poles, which verifies the importance and necessity of multi-sensor extraction for condition assessment of timber poles.

#### Wavelet packet transform (WPT) feature extraction

The second feature extraction method employed is WPT, which is a further development of the wavelet transform and can provide a broader scope of probabilities for the analysis of the sampling signals (Sun and Chang 2002). In WPT, both low frequency and high frequency elements are separated based on successive time fixation of frequency sub-bands produced by a tree structure of high-pass and low-pass filtering operation. The process of WPT is schematically depicted in Fig. 6, in which an original time series signal  $S_{0,0}(n)$  with length  $N$  in the first level is split into a low frequency and a high frequency signal as follows (Sun and Chang 2002):

$$S_{1,0}(n) = \sum_{i=0}^{N-1} g(i) S_{0,0}(n-i) \quad (3)$$

$$S_{1,1}(n) = \sum_{i=0}^{N-1} h(i)S_{0,0}(n-i) \quad (4)$$

where  $S_{1,1}(i)$  and  $S_{1,0}(i)$  denote the details and approximations in the first level, and  $h(i)$  and  $g(i)$  denote the response functions of high-pass and low-pass filters, which are dependent on the selection of the wavelet function. To guarantee the time fixation of every frequency band and improve the frequency resolution, the outputs of the filters are reduced to half of the signal length in the upper level at the end of every filtering phase (Yen and Lin 2000).

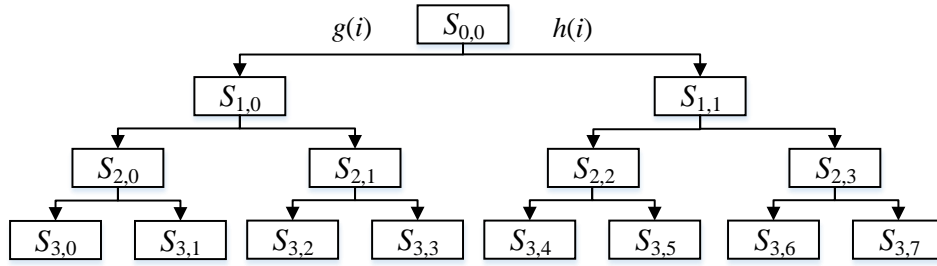


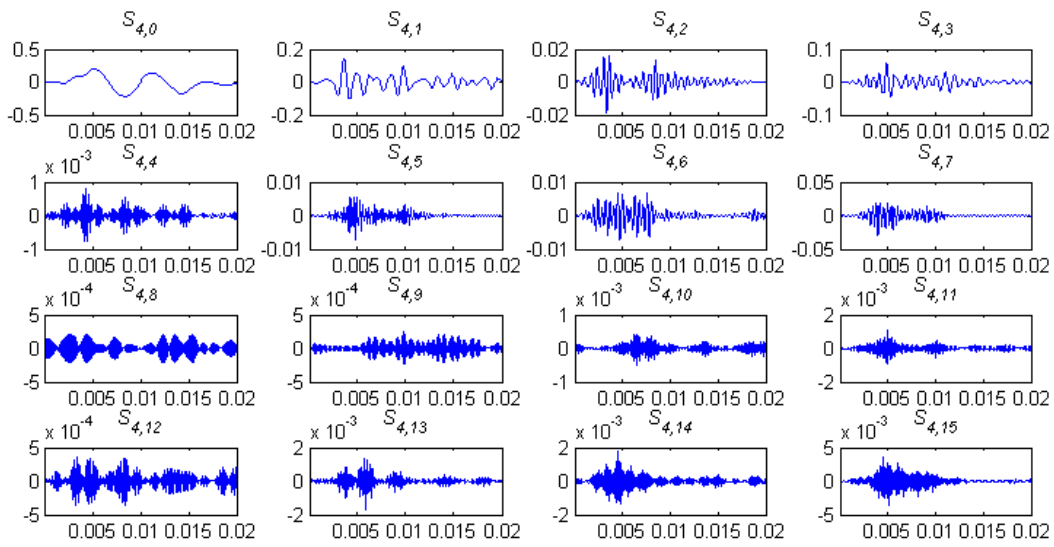
Fig. 6. Tree structure of WPT

Previous studies have shown that very good classification results can be achieved if the BiorSplines 6.8 wavelet function is selected. This is mainly due to its good orthogonality and symmetry together with high vanishing moments. Fig.7 shows the WPT reconstructed bending wave signals of the first 16 frequency bands after 10 layers of decomposition. It is noticed that in the first 2 bands there is no remarkable amplitude difference between intact and damaged poles. However, starting from the third frequency band, clear differences are present between the stress wave signal frequency compositions of the different transform scales. This characteristic is mainly reflected in energy and can be expressed by:

$$E_{k,j} = \sum_{i=1}^N [S_{k,j}(i)]^2 \quad (5)$$

where  $j=3, \dots, 16$ , and  $N$  is the length of reconstructed signal. Fig. 8 shows the sectional energy features of WPT signals from intact and damaged poles. It is noticeable that the signal energy of the fourth frequency band from the intact pole is clearly higher than that of the damaged pole. Hence, these energy features of WPT scale space can be used as feature parameters for timber pole condition assessment.

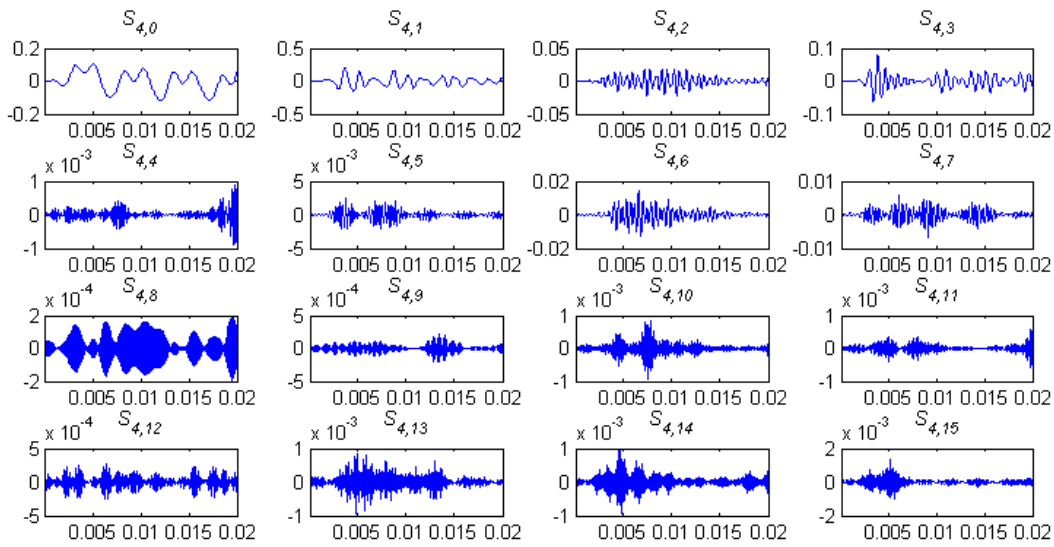
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(a) Intact pole



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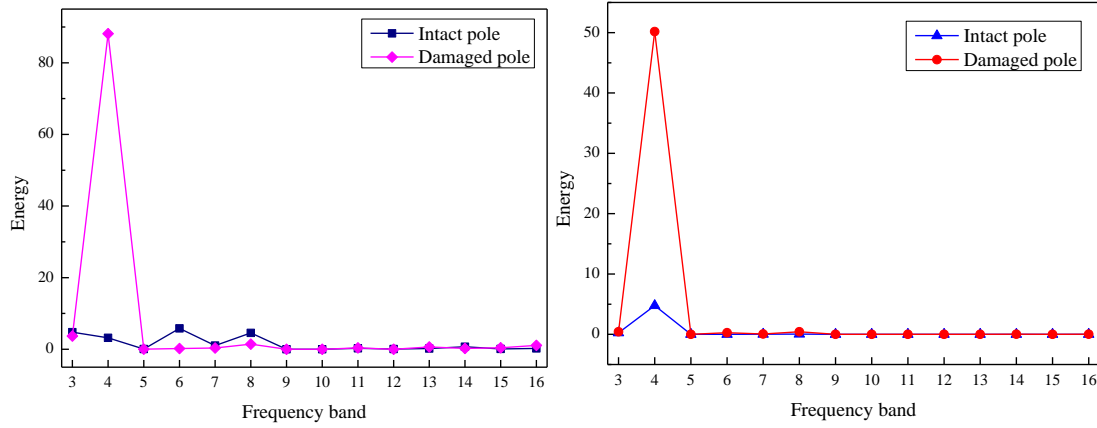
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(b) Damaged pole

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Fig. 7. WPTof bending wave signals



(a) Longitudinal wavedata (b) Bending wave data

Fig. 8. Comparison of WPT signal energy features between intact and damaged pole

#### Empirical mode decomposition (EMD) feature extraction

EMD is an effective and adaptive method for analysing non-stationary and nonlinear signals and was first proposed by Huang (1998). Using this method, a complex signal can be decomposed into a collection of intrinsic mode functions (IMFs) and a residue. Since the decomposition of the signal is mainly dependent on the information contained in the signal, the IMF number is always limited and its components gained via decomposition are steady (Reddy et al. 2015; Rezaei and Taheri 2010; Yang and Tavner 2009). The IMFs generally satisfy two conditions: 1) in the entire signal sequence, the number of extreme points and crossing through zero points should be the same or the difference no more than 1; 2) at any time point, the averaged value of the envelop constructed by the local maximum and minimum points is 0. The procedure of EMD can be described as follows. First, identify all extreme points of the signal  $x(t)$  and interpolate these minimum and maximum points into the lower and upper envelop of the signal using the cubic spline method. Second, calculate the averaged value of the lower and upper envelop, which is denoted as  $m_1(t)$ , thus the detail  $d_1(t)$  can be extracted by (Huang 1998):

$$d_1(t) = x(t) - m_1(t) \quad (6)$$

If  $d_1(t)$  dissatisfies the conditions of IMF, it will be regarded as a new signal and all the steps are repeated until the condition is satisfied. At this point, the detail  $d_1(t)$  is an effective IMF, denoted as  $c_1(t)$  that is the

highest frequency component in the original signal. Third, the difference  $r_1(t)$  is obtained by subtracting  $c_1(t)$  from  $x(t)$  (Huang 1998):

$$r_1(t) = x(t) - c_1(t) \quad (7)$$

Then take  $r_1(t)$  as a new signal and repeat all the steps to obtain  $c_2(t), c_3(t), \dots, c_n(t)$  and  $r_2(t), r_3(t), \dots, r_n(t)$ . If  $r_n(t)$  or  $c_n(t)$  meets the pre-set stopping criterion, and  $r_n(t)$  becomes a monotone function, the cycle is terminated. Finally, the following expression is obtained (Huang 1998):

$$x(t) = \sum_{i=1}^n c_i(t) + r_n(t) \quad (8)$$

where  $c_i(t)$  is the  $i$ th IMF and  $r_n(t)$  is the residue.  $c_1(t)$  contains the highest frequency while  $c_n(t)$  has the lowest frequency, representing the tendency of  $x(t)$ .

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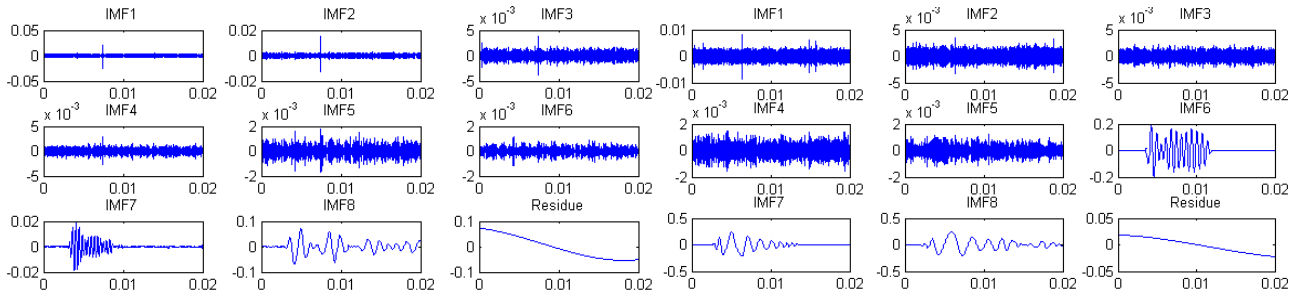
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(a) Intact pole

(b) Damaged pole

Fig. 9. EMD of bending wave signals

After EMD decomposition, the obtained IMFs represent a group of steady signals on the feature scale and every IMF has its own unique energy information. Moreover, it has been found that the signal energy mainly focuses on the first eight layers, which means that the first eight IMFs can completely portray the signal energy feature. Fig.9 shows the first eight layers and the residue of EMD decomposition of bending wave signals for an intact and a damaged timber pole. Based on these results, the energy features of the EMD decomposition are obtained and the energy coefficient of each IMF is given by:

$$Q_i = \frac{E_i}{\sum_{i=1}^8 E_i} \quad (9)$$

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$$E_i = \sum_{n=1}^N [c_i(n)]^2 \quad (10)$$

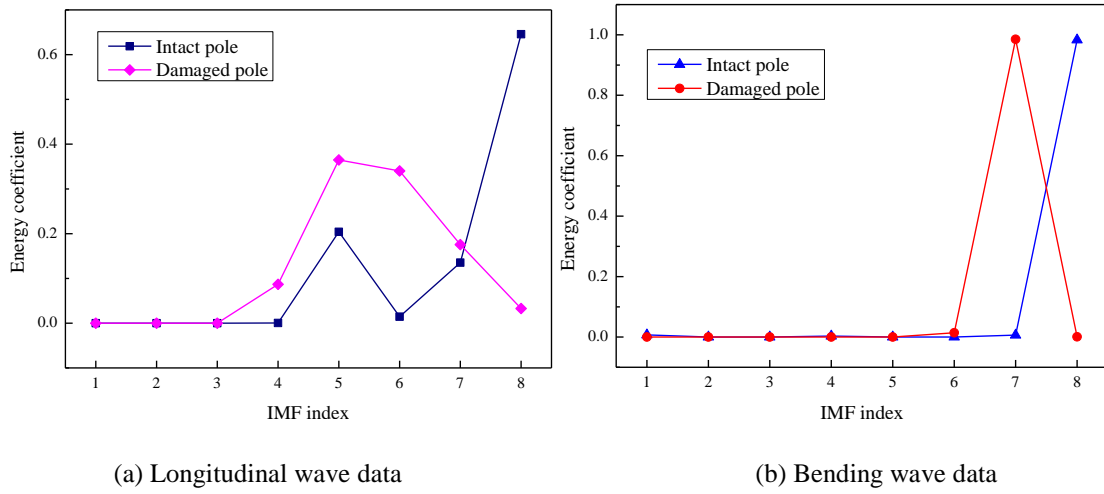
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#### 284 Construction of feature vector

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Fig. 10. Comparison of energy coefficients of IMFs between intact and damaged poles

After feature extraction of the stress wave signals, the final step in the data level involves the construction of a single vector containing the signal state information to be used as input for the SVM for classification learning and testing. Here, three types of signal features (AR model coefficients, energy values of WPT and energy coefficients of EMD) are combined together with a class label by real-number encoding. Fig. 11 shows the specific encoding process. According to the analysis above, there is a total of 44 indicators in the vector for longitudinal wave signals and 41 indicators for bending wave signals.

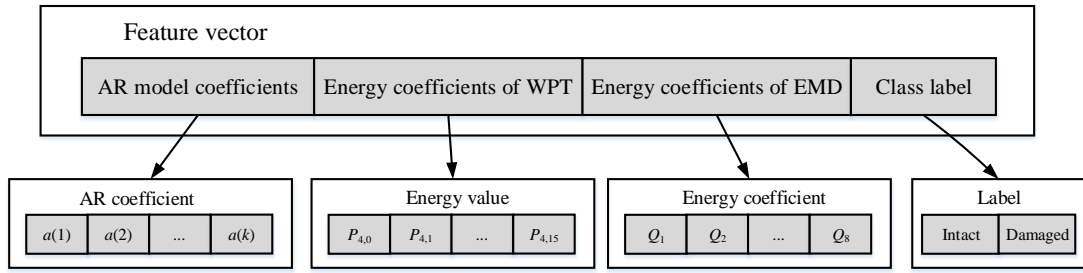


Fig. 11. Encoding for single feature vector

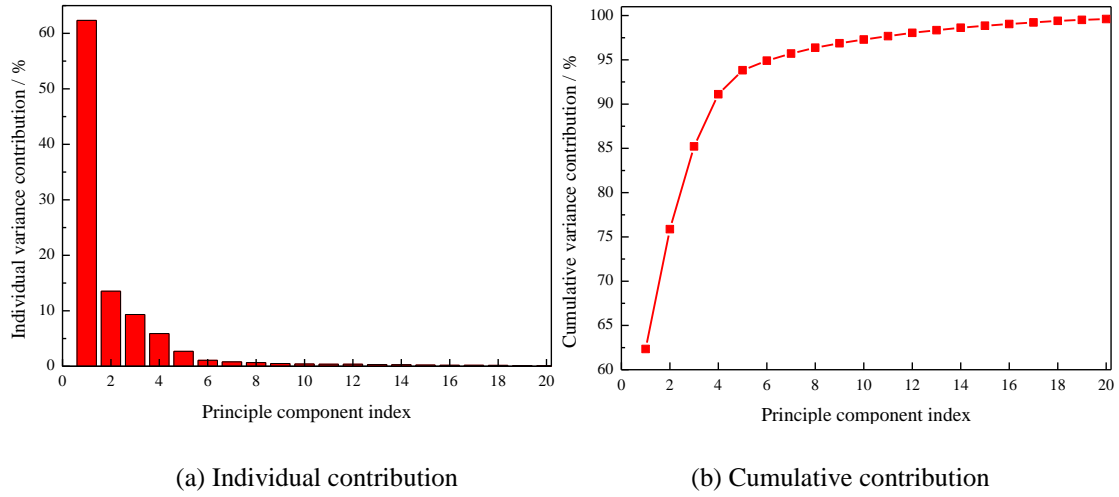
Although multiple feature extraction is able to provide comprehensive information on the signal features, some of these features may be redundant or polluted with noise. If the full feature vector is directly used as input for the SVM classifier, the classification accuracy and generalization capacity will be greatly affected. As a result, the number of indicators should be reduced to obtain an optimal classification model.

In this work, before being used for training in the SVM classifier, the extracted feature vector is pre-processed adopting principal component analysis (PCA), which is considered as an effective statistical multi-variable data processing method for reducing feature dimensionality. This method is based on the linear transformation of the original data set into a new data set with fewer components, which are termed principal components (PCs) (Kuzniar and Waszczyszyn 2006). Every PC is a linear combination of the components in the original data set, and all are orthogonal to each other, thus setting up an orthogonal basis of data space. By disregarding PCs of small contribution, the dimension of the feature vector is decreased without remarkably influencing the signal information.

In this case, there are a total of 44 components in the vector for longitudinal wave signals and 41 components for bending wave signals, corresponding to 44 and 41 SVM input nodes, respectively. However, such large number of input nodes can cause problems in calculation efficiency and training convergence. Hence, PCA is employed to reduce the dimension size. Here, for each sensor in the array, there are 40 samples of longitudinal wave signals and 30 samples of bending wave signals. As presented above, after projection, there are 44 and 41 PCs corresponding to longitudinal and bending wave signals, respectively. Fig.12 shows the individual and cumulative contributions of the first 20 PCs of the feature vector of sensor 1 of

317 bending wave signals. It can be seen that the first 8 PCs make up more than 95% contribution of the original  
 318 information (first 15 PCs for longitudinal wave data). So with a 5% loss of information, the vector  
 319 dimensions can be significantly reduced, which is greatly beneficial to SVM training. The resulting input  
 320 vector dimensions for the SVMs for the remaining sensors are listed in Table 1.

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Fig. 12. PCA results of bending wave signals from sensor 1

Table 1. Feature vector dimensions of other six sensors

Signal type	Feature vector dimension					
	Sensor 2	Sensor 3	Sensor 4	Sensor 5	Sensor 6	Sensor 7
Longitudinal wave	14	16	17	15	12	15
Bending wave	10	5	7	8	12	7

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### 328 *Feature level fusion based on SVM*

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#### 330 Theoretical background

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332 SVM is a machine learning algorithm, which is based on the principle of structural risk minimization and  
 333 kernel-based method (Qu et al. 2013; Ao et al. 2014). SVM utilizes a finite number of samples to train the  
 334 model to explore the optimal compromise between generalization performance and classification accuracy,  
 335 and reveals the distinct benefits in dealing with problems of nonlinearity, small samples and high dimension.  
 336 Hence it is considered as one of the most effective machine learning algorithms. The principle of SVM for



337 classification is to seek an optimal line or hyperplane between two groups of data with maximum margin. For  
 338 a given training set  $\{(x_i, y_i)_{i=1}^l\}$ , where  $x_i$  denotes the input vector and  $y_i$  is the class label, the characteristic  
 339 space of SVM is represented by (Vapnik 1998):

$$340 \quad f(x) = \omega \cdot x + b \quad (11)$$

341 where  $\omega$  is the vector of connecting weight and  $b$  is a bias. The optimal classifier can be obtained by  
 342 calculating the following minimization optimization problem (Vapnik 1998):

$$343 \quad \begin{aligned} & \text{Minimize} \quad \frac{1}{2} \|\omega\|^2 + C \sum_{i=1}^l \xi_i \\ & \text{s.t.} \quad y_i(\omega \cdot x_i + b) \geq 1 - \xi_i, \quad \xi_i \geq 0 \text{ and } i = 1, 2, \dots, l \end{aligned} \quad (12)$$

344 where  $C$  represents the penalty factor to adjust the balance between the classifier complexity and to minimize  
 345 the training error, and  $\xi_i$  denotes the classification errors. By incorporating a Lagrange function, the above  
 346 optimization problem can be written as a dual optimization problem, expressed by (Vapnik 1998):

$$347 \quad \begin{aligned} & \text{Maximize} \quad \sum_{i=1}^l \alpha_i - \frac{1}{2} \sum_{i,j=1}^l \alpha_i \alpha_j y_i y_j (x_i \cdot x_j) \\ & \text{s.t.} \quad \sum_{i=1}^l \alpha_i y_i = 0, \quad 0 \leq \alpha_i \leq C \text{ and } i = 1, 2, \dots, l \end{aligned} \quad (13)$$

349 Therefore, the optimal nonlinear decision function can be obtained by solving the above problem, which is  
 350 expressed by:

$$351 \quad f(x) = \text{sgn} \left[ \sum_{i=1}^l \alpha_i y_i K(x_i, x) + b \right] \quad (14)$$

352 where  $K(x_i, x)$  is the kernel function, which is used in SVM for nonlinear classification. In this paper, the  
 353 radial basis function (RBF) is employed as the kernel function due to its excellent performance on nonlinear  
 354 classification. The expression of RBF is

$$355 \quad K(x_i, x) = \exp \left( -\frac{\|x_i - x\|^2}{2\sigma^2} \right) \quad (15)$$

356 where  $\sigma$  is the width of RBF.

357 Construction of SVM classifier

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359 To identify the health condition of the timber poles from the extracted feature vector, fourteen sub SVM  
360 classifiers, corresponding to the two signal types (longitudinal and bending waves) and seven sensors, are  
361 built. The PCs selected from the feature vector in Section 3.1.4 are used as the inputs of the SVM classifier  
362 while the output of the model is the pole condition. There are two condition types denoted as 0 and 1, where  
363 0 means ‘damaged’ and 1 represents ‘intact’. The classifier parameters are also selected, which are related to  
364 the model generalization performance and classification accuracy. Here, the genetic algorithm (GA) is  
365 adopted to optimize the penalty factor  $C$  and the kernel function parameter  $\sigma$  in the classifier model. The  
366 classification accuracy is evaluated by leave-one-out cross-validation using the fitness function for parameter  
367 optimization. The optimization process can be regarded as solving the following maximization optimization  
368 problem:

$$\begin{aligned} & \underset{C, \sigma^2}{\text{Maximize}} && R_{cv}(C, \sigma^2) \\ & \text{s.t.} && C_{\min} \leq C \leq C_{\max} \\ & && \sigma_{\min}^2 \leq \sigma^2 \leq \sigma_{\max}^2 \end{aligned} \quad (16)$$

370 where  $R_{cv}(C, \sigma^2)$  denotes the ratio between correct classification samples and the total samples. For each sub  
371 SVM classifier, the optimization process can be divided into the following steps:

372 **Step 1.** Initialize the chromosome number  $N$ , maximal iteration number  $T$ , search range of parameter  $(C, \sigma^2)$ ,  
373 crossover probability  $P_c$  and the mutation probability  $P_m$ . In this case,  $N=20$ ,  $T=100$ ,  $C_{\min}=0$ ,  
374  $C_{\max}=100$ ,  $\sigma_{\min}^2=0$ ,  $\sigma_{\max}^2=100$ ,  $P_c=0.7$  and  $P_m=0.01$ .

375 **Step 2.** Chromosome encoding for parameter  $(C, \sigma^2)$ . Randomly generate initial chromosome and set initial  
376 iteration  $t=0$ .

377 **Step 3.** Calculate the individual fitness, i.e.  $R_{cv}(C, \sigma^2)$ .

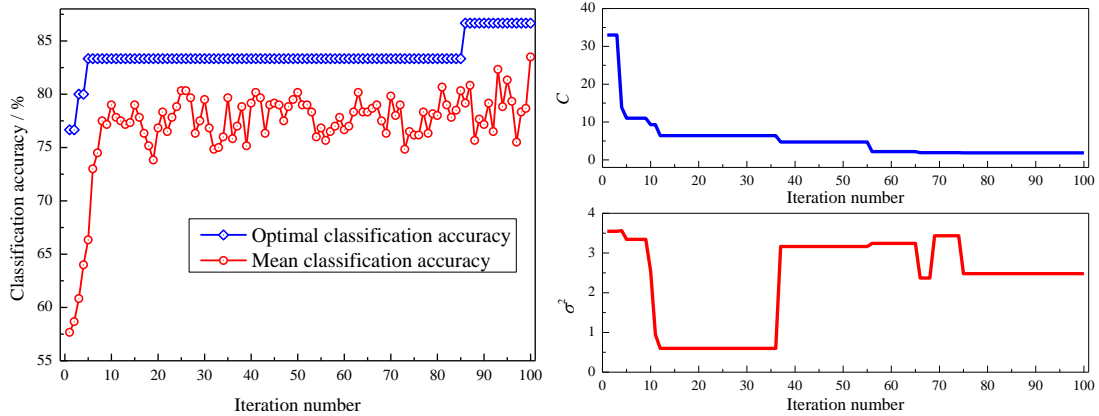
378 **Step 4.** Select the part of the chromosome to produce the new chromosome by roulette wheel strategy.

379 **Step 5.** Carry out the crossover and mutation operation to generate the new chromosome.

380 **Step 6.** If the termination rule is not satisfied and  $t \leq T$ , go to Step 2.

381

Fig.13 shows the parameter optimization process of sub SVM of bending wave signals from sensor 1. Fig. 13(a) shows the algorithm convergence during the iteration while Fig. 13(b) gives the variance trend of each parameter. It is apparent that the best fitness gradually increases with the addition of iteration number though some fluctuations still exists in the average fitness (classification accuracy). Moreover, it is found that the parameter  $C$  can quickly arrive at its optimum compared with  $\sigma^2$ , which requires more iteration. Table 2 gives the classification results for both wave types of all sub SVMs using leave-one-out cross-validation. It is observed that the classification accuracies of sub SVMs based on bending wave data are higher than those of longitudinal wave data. This may be due to two reasons: 1) due to the shorter wavelength in the induced frequency band, the bending wave is more susceptible to smaller damage compared to the longitudinal wave; 2) the bending wave has more prominent radial and longitudinal displacement components on the surface of the tested pole. Therefore, the bending wave is able to reflect the damage scenarios more accurately compared to the longitudinal wave since the radial component is more susceptible to the real damages.



(a) Convergence rate

(b) Parameter optimization

Fig. 13. Parameter optimization process of sub SVM of bending wave from Sensor 1

Table 2. Classification results of all sub SVMs using leave-one-out cross-validation

Sensor Number	Classification accuracy		
	Longitudinal wave	Bending wave	Mean
Sensor 1	80% (32/40)	86.67% (26/30)	82.86% (58/70)
Sensor 2	87.5% (35/40)	90% (27/30)	88.57% (62/70)
Sensor 3	87.5% (35/40)	96.67% (29/30)	91.43% (64/70)
Sensor 4	77.5% (31/40)	83.33% (25/30)	80% (56/70)
Sensor 5	62.5% (25/40)	80% (24/30)	70% (49/70)
Sensor 6	92.5% (37/40)	93.33% (28/30)	92.86% (65/70)

Sensor 7	82.5% (33/40)	86.67% (26/30)	84.29%(59/70)
Mean	81.43% (228/280)	88.1% (185/210)	

Probability output of SVM classifier

The standard outputs of SVM classifiers are based on hard decision and are dependent on avoting method. However, for practical engineering applicationswith nonlinear classification problems, a soft decision with probability outputs is required to provide an objective evaluation with different categories. In this work, the sigmoid function is adopted to map the outputs of SVM to the range of [0, 1] to obtain posterior probability outputs. The specific expression is given by:

$$p(x) = \frac{1}{1 + \exp[Af(x) + B]} \quad (17)$$

where  $A$  and  $B$  are two factors to adjust the flexibility of the sigmoid function and their optimal values can be obtained by solving the following minimization problem:

$$\min - \sum_{i=1}^l [t_i \ln(p_i) + (1 - t_i) \ln(1 - p_i)] \quad (18)$$

where  $p_i = \frac{1}{1 + \exp[Af(\mathbf{x}_i) + B]}$  and  $t_i = \frac{y_i + 1}{2}$ ,  $y_i$  is the classification label of sample  $i$ .

### ***Decision level fusion based on D-S evidence theory***

The evidence theory is usedto manipulate and model incomplete, inaccurate, uncertain and even conflicting information. It was first presented by Dempsterbased on the notion of upper and lower probabilities, and then consummated by Shafer (Dampster 1967; Shafer 1976). This method has been successfully applied in many application fields such as data fusion, image analysis, pattern recognition and decision making (Talon et al. 2014). For probability estimation, the evidence theory adopts a belief function, which is built usingevent probability and constraint expression withthe novel percept notions, i.e. unknown or uncertainty.

Frame of discernment

424

425 In the evidence theory, a non-null set, which contains  $N$  exhaustive and exclusive hypotheses, is defined as  
 426 the frame of discernment. The power set is denoted by  $2^\theta$ . In this work, the frame of discernment for pole  
 427 condition assessment is  $\theta = \{A_1, A_2\}$ , where  $A_1$  and  $A_2$  represent the damaged and intact conditions,  
 428 respectively.

429

#### 430 Basic Probability Assignment

431

432 The basic probability assignment function (BPA) of the proposition  $A$  is a mapping from  $2^\theta$  to the interval  $[0,$   
 433  $1]$ , which meets the following relationship (Dampster 1967; Shafer 1976):

$$434 \quad \begin{cases} m(\Phi) = 0 \\ \sum_{A \subseteq \theta} m(A) = 1 \end{cases} \quad (19)$$

435 where  $m(A)$  is called the BPA of event  $A$ , which denotes a certain piece of evidence. Generally, the  
 436 probability output of sub SVM classifier can be regarded as the BPAs, which means that  $p(x)$  denotes the  
 437 BPA value of the damaged condition,  $1-p(x)$  denotes the BPA value of the intact condition. Also, how to  
 438 assign the uncertainty is an important issue to be solved. Here, the error upper bound of SVM classification  
 439 identification is introduced and adopted: if a group of training samples are able to be separated by an optimal  
 440 hyperplane, the classification error upper bound of testing samples is the ratio of mean number of support  
 441 vectors in the training set to the total training sample number:

$$442 \quad E(P_{error}) = \frac{N_{sv}}{N_t - 1} \quad (20)$$

443 where  $N_t$  and  $N_{sv}$  denote the total training sample number and mean number of support vectors, respectively.  
 444 The above expression represents the sample uncertainty by SVM classification, corresponding to the  
 445 uncertainty degree  $\theta$  in the frame of discernment  $\theta$ . In order to satisfy the requirement that the summation  
 446 of BPAs equals to 1, the probability outputs of two categories (damaged and intact) should be multiplied by  
 447 the coefficient  $1-E(P_{error})$ . Accordingly, the mathematical expression of BPAs by SVM classifier is given as  
 448 follows:

449

$$\begin{cases} m(A_1) = p(x)(1 - \frac{N_{sv}}{N_t - 1}) \\ m(A_2) = [1 - p(x)](1 - \frac{N_{sv}}{N_t - 1}) \\ m(\Theta) = \frac{N_{sv}}{N_t - 1} \end{cases} \quad (21)$$

450

451 Evidence combination rule

452

453 Suppose  $m_1$  and  $m_2$  are BPA functions from different evidence sources in the same frame of discernment, and  
 454 its focal elements are  $B_i$  and  $C_j$ . The rule of combination of  $B_i$  and  $C_j$  is given as follows (Dampster 1967;  
 455 Shafer 1976):

456

$$\begin{cases} m(A) = 0, & A = \emptyset \\ m(A) = m_1 \oplus m_2 = \frac{\sum_{B_i \cap C_j = A} m_1(B_i)m_2(C_j)}{1 - K} \end{cases} \quad (22)$$

457 where  $K = \sum_{B_i \cap C_j = \emptyset} m_1(B_i)m_2(C_j)$  denotes the conflict degree among different information sources. Generally,

458 the combination result of  $n$ BPA functions  $(m_1, \dots, m_n)$  in the same frame of discernment is given by  
 459 (Dampster 1967; Shafer 1976):

460

$$m = m_1 \oplus m_2 \oplus \dots \oplus m_n \quad (23)$$

461

462 Decision making

463

464 In this paper, the maximum trust degree approach is used to make a final decision in accordance with the  
 465 evidence combination results:

466  $\exists A_1$  and  $A_2 \subset \Theta$ ,  $m(A_2) = \max\{m(A_k), A_k \subset \Theta \text{ and } A_k \neq A_1\}$ . If the following expression is satisfied:

467

$$\begin{cases} m(A_1) - m(A_2) > \delta_1 \\ m(\Theta) < \delta_2 \\ m(A_1) > m(\Theta) \end{cases} \quad (24)$$

468

$A_1$  is the final result, where  $\delta_1$  and  $\delta_2$  denote the thresholds. In this work,  $\delta_1=0.3$  and  $\delta_2=0.3$ .

469

470 **Case study**

471

472 To evaluate the performance of the hierarchical data fusion model on the condition assessment of timber  
 473 utility poles, all cases of timber poles are utilized to testing the model using leave one pole out method, in  
 474 which five cases related to the same pole are taken out in turn as the unknown validation samples and the rest  
 475 are used as the training set. Tables 3 and 4 show the initial estimations of all sub SVM classifiers of the two  
 476 randomly selected cases. According to the description in 3.3.4, when  $m(A_1) - m(A_2) > 0.3$ ,  $m(\Theta) < 0.3$  and  
 477  $m(A_1) > m(\Theta)$ , the assessment result is  $A_1$ ; when  $m(A_2) - m(A_1) > 0.3$ ,  $m(\Theta) < 0.3$  and  $m(A_2) > m(\Theta)$ , the  
 478 assessment result is  $A_2$ . Otherwise, there is no recognition result from the system. Consequently, it can be  
 479 seen that for the damaged pole case, the assessment results from the sensors 2, 4, 5, 6 and 7 dissatisfy the  
 480 decision rule. The same problem exists for the sensors 1, 3 and 5 for the intact pole case. It is believed that  
 481 there are two possible reasons contributing to this phenomenon. One reason may be linked to noise  
 482 sensitivity, sensor or measurement errors, which cause uncertainties in the input feature vectors of the sub  
 483 SVM classifiers. The other reason is that the training samples are so limited that they are not able to include  
 484 all the possible conditions, which may lead to the identification errors in sub SVM classifiers.

485

486 Tables 5 and 6 give the first-layer evidence combination results of two sub SVM classifiers of the same  
 487 sensor for the two cases. For the damaged pole case, the support probability of the proposition  $A_1$  (damaged  
 488 condition) has increased to 0.8491 at sensor 1 while the support probability of  $A_2$  (intact condition) and  
 489 uncertainty degree declined to 0.0372 and 0.1137, respectively. This result meets the decision rule, which  
 490 means that the assessment result of sensor 1 is  $A_1$  ‘damaged pole’. Similarly, the other six sensors have the  
 491 same assessment results. Therefore, after first-layer evidence combination, all the sensors in the testing  
 492 system give the same result for  $A_1$ , which conforms to the practical condition of the pole. However, for the

506 intact pole, because  $m_1(A_1) > m_1(A_2)$  and  $m_3(A_1) > m_3(A_2)$ , the assessment results from sensors 1 and 3 are still  
 507 in contradiction with that of the other five sensors. Therefore, it is difficult for the system to make a final  
 508 decision.  
 509

Table 3. Initial recognition result by SVM classifiers for the damaged pole case

BPA	$A_1$	$A_2$	$\Theta$
$m_{1,1}$	0.5734	0.1702	0.2564
$m_{1,2}$	0.6911	0.1020	0.2069
$m_{2,1}$	0.2940	0.4624	0.2436
$m_{2,2}$	0.7708	0.0395	0.1897
$m_{3,1}$	0.5858	0.1578	0.2564
$m_{3,2}$	0.7696	0.0063	0.2241
$m_{4,1}$	0.4170	0.3138	0.2692
$m_{4,2}$	0.7860	0.0243	0.1897
$m_{5,1}$	0.2747	0.4689	0.2564
$m_{5,2}$	0.6806	0.1125	0.2069
$m_{6,1}$	0.2770	0.4666	0.2564
$m_{6,2}$	0.7886	0.0217	0.1897
$m_{7,1}$	0.3245	0.4319	0.2436
$m_{7,2}$	0.7491	0.0440	0.2069

Table 4. Initial recognition result by SVM classifiers for the intact pole case

BPA	$A_1$	$A_2$	$\Theta$
$m_{1,1}$	0.4836	0.2600	0.2564
$m_{1,2}$	0.5158	0.2773	0.2069
$m_{2,1}$	0.0203	0.7361	0.2436
$m_{2,2}$	0.0241	0.7862	0.1897
$m_{3,1}$	0.1292	0.6144	0.2564
$m_{3,2}$	0.7225	0.0534	0.2241
$m_{4,1}$	0.1816	0.5492	0.2692
$m_{4,2}$	0.0506	0.7597	0.1897
$m_{5,1}$	0.4625	0.2811	0.2564
$m_{5,2}$	0.0437	0.7494	0.2069
$m_{6,1}$	0.2144	0.5292	0.2564
$m_{6,2}$	0.0033	0.8070	0.1897
$m_{7,1}$	0.0646	0.6918	0.2436
$m_{7,2}$	0.0191	0.7740	0.2069

510  
 511 Tables 7 and 8 show the second-layer evidence combination results of all seven sensors for the two cases.  
 512 From the tables it can be seen that after the second-layer combination, the uncertainty degree declines to 0  
 513 and the support probabilities of the propositions as the final decisions for the two cases ascend to 100%,  
 514 which is in agreement with the practical conditions of the cases. The results verify that compared to  
 515 the results from the single SVM classifier, the confidence probability of the final decision is greatly improved  
 516 through the two-layer evidence combination.  
 517

Table 5. First-layer evidence combination for the damaged pole case

BPA	$A_1$	$A_2$	$\Theta$
$m_1$	0.8491	0.0372	0.1137
$m_2$	0.7785	0.0627	0.1588
$m_3$	0.8852	0.0020	0.1128
$m_4$	0.8481	0.0198	0.1321
$m_5$	0.6386	0.1802	0.1812
$m_6$	0.7880	0.0365	0.1755
$m_7$	0.7779	0.0608	0.1613

Table 6. First-layer evidence combination for the intact pole case

BPA	$A_1$	$A_2$	$\Theta$
$m_1$	0.6659	0.1925	0.1416
$m_2$	0.0008	0.9253	0.0739
$m_3$	0.5084	0.1787	0.3129
$m_4$	0.0192	0.8738	0.1070
$m_5$	0.0712	0.7420	0.1868
$m_6$	0.0015	0.8964	0.1021
$m_7$	0.0022	0.9120	0.0858



Table 7. Second-layer evidence combination for the damaged pole case

BPA	$A_1$	$A_2$	$\Theta$
$m$	1.0000	0	0

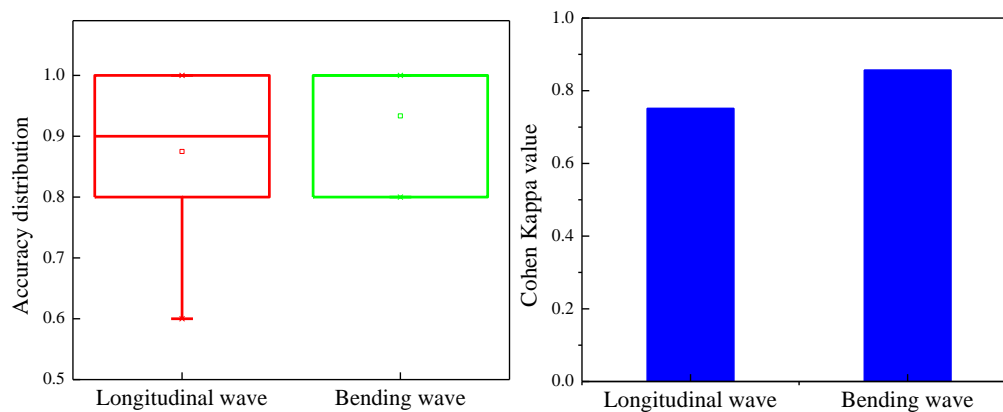
Table 8. Second-layer evidence combination for the intact pole case

BPA	$A_1$	$A_2$	$\Theta$
$m$	0	1.0000	0

537

538 Fig. 14 gives the statistical accuracy analysis results of the proposed model for timber poles with longitudinal  
 539 and bending wave excitations. Fig. 14 (a) displays the classification accuracy distributions for two excitation  
 540 cases. The results clearly illustrate that bending wave excitation outperforms longitudinal wave in the respect  
 541 of classification accuracy with average value of 93.33% although the latter also could arrive at 87.5%. Fig.  
 542 14 (b) shows the related Cohen Kappa values of the data fusion model with different excitation types.  
 543 Generally, Kappa value is used to estimate the distribution of the forecast labels, which could not be  
 544 expressed by the classification accuracy. Kappa value always changes between 0 and 1 with the maximal  
 545 value representing the best forecast with all values located at the diagonal line in the confusion matrix  
 546 (Witten et al. 2011). Similar to results in Fig. 14 (a), Fig. 14 (b) also verifies that bending wave cases also  
 547 present a better result than the longitudinal wave cases, which accords with the previous analysis that  
 548 captured signal features from bending wave are more sensitive to the damage scenario than that of  
 549 longitudinal wave.

550



551

552

(a) Classification accuracy distribution (b) Cohen Kappa value

553

Fig. 14. Statistical indicators of the proposed model with different wave signal excitations

554

## Conclusion

This paper presented a novel method for the health condition assessment of in-situ timber utility poles based on a hierarchical data fusion model. In the proposed method, first, stress wave signals were recorded in a sensor array using two types of wave excitation (longitudinal and bending wave). Second, for each sensor, the stress wave data was analysed using AR coefficients, wavelet packet energies and energy coefficients of IMFs. The derived parameters were then used to form a feature vector and PCA was applied for data compression. Third, for each sensor, two sub SVM classifiers were built up for initial estimation of the pole condition. Fourth, to improve the identification accuracy of the classifier and to obtain a final decision, GA was employed to optimize the two main parameters in the model. The experimental results from in-situ timber pole testing demonstrated that the proposed hierarchical model is able to greatly improve the identification accuracy. The support probability of right proposition was increased from 0.7886 to 1. This prevents the problem of difficult decision making and satisfies the requirement of condition assessment of timber utility poles in engineering application and management. In this work, the SVM model is set up based on the off-line learning, which is not suitable for real-time structural health monitoring of timber poles. In the future work, the model will be realised in the on-line way to update the model in real-time for the higher accuracy. Furthermore, except the application in the pole condition assessment, the proposed hierarchical model can also be developed for leakage detection of pipeline networks, fault diagnosis of machines and damage detection of bridge and building structures, in which the multi-sensor system is essential for capturing multi-source data information to implement the monitoring tasks. Moreover, sometimes the information provided by only one-type sensor may be incomplete or inaccurate due to the self-deficiency and environmental factors. Therefore, multi-type-sensor system and multi-source information fusion algorithm will be also investigated to realise their application in civil engineering in future.

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553

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