

The Dynamic Performance and Economic Benefit of a Blended Braking System in a Multi-Speed Battery Electric Vehicle

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Abstract

As motor-supplied braking torque is applied to the wheels in an entirely different way to hydraulic friction braking systems and it is usually only connected to one axle complicated effects such as wheel slip and locking, vehicle body bounce and braking distance variation will inevitably impact on the performance and safety of braking. The potential for braking energy recovery in typical driving cycles is presented to show its benefit in this study. A general predictive model is designed to analysis the economic and dynamic performance of blended braking systems, satisfying the relevant regulations/laws and critical limitations. Braking strategies for different purposes are proposed to achieve a balance between braking performance, driving comfort and energy recovery rate. Special measures are taken to avoid any effects of motor failure. All strategies are analyzed in detail for various braking events. Advanced driver assistance systems (ADAS), such as ABS and EBD, are properly integrated to work with the regenerative braking system (RBS) harmoniously. Different switching plans during braking are discussed. The braking energy recovery rates and brake force distribution details for different driving cycles are simulated. Results for two of the cycles in an 'Eco' mode are measured on a drive train test rig and found to agree with the simulated results to within approximately 10%. Reliable conclusions can thus be gained on the economic benefit and dynamic braking performance. The strategies proposed in this paper are shown to not only achieve comfortable and safe braking during all driving conditions, but also to significantly reduce cost in both the short and long term.

Keywords: Regenerative braking; Blended braking system; Strategy; Cost; Driving cycles.

1. Introduction

The benefit of regenerative braking by blended braking systems, combining electric and friction brakes, has been theoretically and experimentally validated in many kinds of electric vehicle (EV), e.g. battery electric vehicle (BEV) [1,2], fuel cell electric vehicle (FEV) [3], and hybrid electric vehicle (HEV) [4]. A plethora of similar papers can be found which focus on braking energy recovery improvement by optimizing strategies and studying the performance of braking system itself. Nian, et al used PID control and fuzzy logic in a brushless DC motor to realize regenerative braking and prolong driving range, ensuring the braking quality at the same time [5]. A vehicle lateral motion state based adaptive control strategy was proposed by Han and Park to guarantee the vehicle controllability and stability [6]. Electromechanical brake was

37 integrated into regenerative braking to ensure braking force distribution ratio follow an optimal
38 curve, instead of a linear line [7]. According to the results from Gao, et al, blended braking
39 system structure plays an important role in energy recovery rate [8]. Zhang developed a
40 regenerative braking system by utilizing as much as possible mature components, integrating
41 cooperative regeneration with Anti-lock Braking System (ABS)/Traction Control System (TCS)
42 functions, which provided system reliability, low development cost and risk at the same time
43 [9]. Battery current balance during regenerative braking was investigated in [10] by
44 experimental analysis in both used-defined and FTP-75 driving cycles.

45 However, the frequently mentioned energy recovering ability and braking performance, in the
46 above studies, are just two of the key factors in blended braking system design, and are not
47 mutually independent. The safety issues introduced by the addition of a brake-by-wire system,
48 the braking performance affected by a combination strategy, the potential economic benefits,
49 and the relationship of economic benefit and braking performance need to be considered as
50 well. Specially testing maneuvers for blended braking system, which are often neglected by
51 many studies, are required to validate the braking performance in all conditions [11,12]. The
52 problems became more complicated when a multi-speed gearbox became popular on EVs, such
53 as an Automatic Transmission (AT), Automated Manual Transmission (AMT) or Continuously
54 Variable Transmission (CVT) is added to improve the dynamic performance and driving range,
55 then additional problems of response delay and torque interruption are introduced [13–15].
56 These problems are of particular concern for the simplified two-speed Dual Clutch Transmission
57 (DCT), which has been proven to be extremely suitable for EVs [16,17]. Additionally, safety-
58 oriented driver assistance system, such as the Anti-lock Braking System (ABS) and Electronic
59 Brake Force Distribution (EBD), should also be integrated into blended braking strategies
60 properly to ensure their effectiveness [18,19]. At last, for any of these complicated powertrain
61 architectures, specially designed braking algorithms are needed to ensure safe braking, while
62 recapturing as much kinetic energy as possible.

63 In this paper, an optimized blended braking strategy with a manual/automatic switch over
64 function is proposed to achieve the balance between braking performance and energy recovery
65 ability. This demonstrates the energy recovering improvement based economic benefit. A
66 comprehensive investigation of the energy recovery, safety issues, braking dynamic
67 performance, and economic benefit of a multi-speed transmission based blended braking
68 system is clearly addressed.

69 Based on the achievement and limitations of previous papers, a brief breakdown of the
70 comprehensive researching work, regarding to the dynamic performance and economic benefit
71 of braking energy recovering on multi-speed BEV, is presented in following parts:

- 72 1. The energy lost in conventional friction braking is reported to indicate the maximum
73 potential gains from regenerative braking,
- 74 2. The strengths and weaknesses of blended braking in a two-speed DCT based front-drive
75 BEV are discussed.

- 76 3. The advantage of load transfer to the motor-connected front axle during braking is
77 examined, while the torque interruption in gear shifting presents a disadvantage.
78 4. Different strategies are designed to either recapture maximum braking energy, or
79 achieve the best braking performance, or to compromise between energy recovery and
80 braking performance.
81 5. A simulation model is established to analyse the details of braking force distribution,
82 wheel slip, and kinetic energy recovery rates in various test conditions.
83 6. One of the strategies is validated experimentally on an electric powertrain test bench for
84 city and highway driving cycles.
85 7. Finally, the economic benefit of blended braking systems with different strategies is
86 evaluated, in terms of fuel cost, initial manufacturing cost and maintenance cost.
87 8. Superior dynamic performance and economic benefit are obtained than for the
88 strategies used in another recent study [20].

89 Some of the above content has been presented in paper [21] by a subset of the authors.
90 That content is included here for completeness, but the content is restructured and
91 rewritten, and extended with the new results on the brake force distribution, dynamic
92 performance and economic benefit analysis of energy recovering.

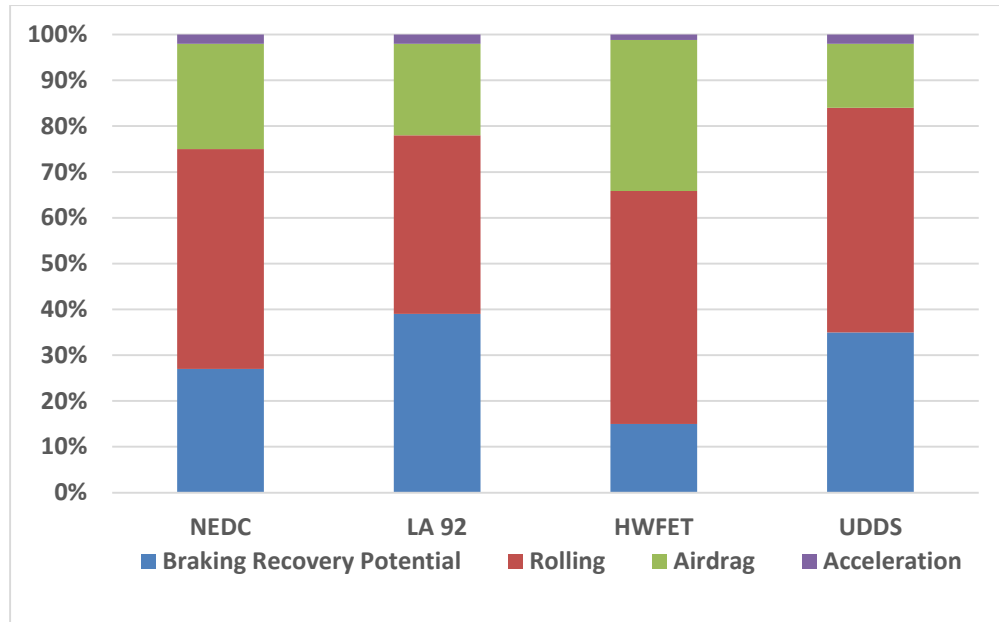
93 **2. Maximum Kinetic Energy Recovery**

94 In EVs, regenerative braking captures the drop in the vehicle's kinetic energy, which in
95 traditional Internal Combustion Engine (ICE) vehicles is lost as heat in friction brakes. However,
96 the different working principles and the potential safety risks have been barriers to large-scale
97 commercialization. To assess whether it is worth the extra cost of additional equipment and
98 R&D to achieve a blended braking system for EVs, one must know the potential gain, i.e. how
99 much energy is consumed by braking.

100 Fig.1 shows the distributions of energy consumption in several typical driving cycles for a
101 medium size passenger Battery Electric Vehicle (BEV), without regenerative braking. The results
102 are based on the integral of driving energy consumption and energy lost in friction braking with
103 respect to time. The dynamic energy consumption in driving of specification Table 1A, i.e.
104 rolling, aerodynamic drag and acceleration, is calculated by Eq.1, which is the product of vehicle
105 dynamic resistance and travel distance per computational step size. According to the target
106 speed profile of cycles, the dynamic friction braking force is achieved in Simulink model, shown
107 in Fig.2. For city or hybrid cycles, the energy wasted in braking is very high, e.g. 39% in the
108 California Unified Cycle (LA92) and 35% in Urban Driving Dynamometer Schedules (UDDS). In
109 fact, the energy wasted can easily go over 50% during peak commuting times in congested
110 cities. Even in the highway cycle Highway Fuel Economy Testing (HWFET), with less acceleration
111 and deceleration events, the braking loss is still a considerable 15%. Though not all of the
112 energy can be recaptured, these figures show the significant potential for a regenerative braking
113 system (RBS) to extend driving range, thus saving energy use cost.

$$\Delta E_{driving} = (mgC_R \cos \varphi + mg \sin \varphi + C_D A u^2 / 21.15 + \delta m d_u / d_t) \times \Delta x \quad (1)$$

114 where C_R is the rolling resistance coefficient, φ represents the slop degree, C_D is the
 115 aerodynamic drag coefficient, A is the front area, u is vehicle velocity in km/h, δm is the
 116 equivalent mass in acceleration including the rotational components. Δx represents the travel
 117 distance per computational step size in Simulink model.

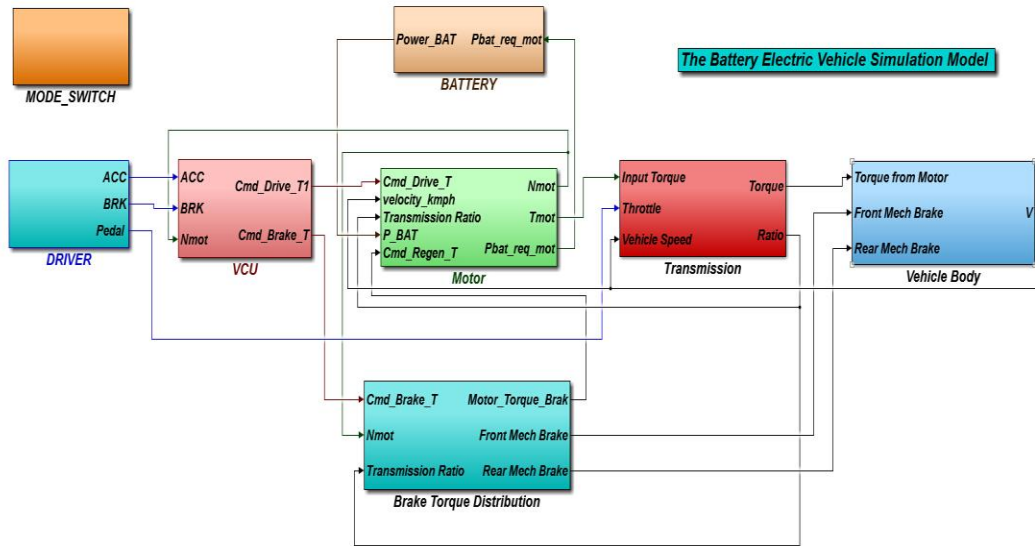


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119 Figure 1: Energy consumption distribution in driving cycles, with the energy lost in braking
 120 shown in blue.

121 3. Powertrain Topology

122 The simulation model shown in Fig. 2 has been created to evaluate the safety and energy
 123 recovery performance of a blended braking system. It is a backward-facing model in which the
 124 desired driving cycle speed profile is assigned. For the given speed profile, the Vehicle Control
 125 Unit (VCU) calculates the required driving and braking torques and the power from the battery.
 126 The total required braking torque is apportioned in the 'Brake Torque Distribution' block into
 127 three command paths, to the front (axle) motor brake, the front friction brake, and the rear
 128 friction brake, according to the selected strategy. The regenerative braking torque is limited by
 129 the motor's maximum torque ability, which is a function of speed, and by the maximum
 130 charging current capability of the battery, which is a function of its state of charge. The motor
 131 torque goes through a stepped transmission, before being applied on the driven front axle. In
 132 the alternate torque command path, mechanical friction braking is directly applied to the
 133 wheels, front or rear, via a hydraulic system.



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Figure 2: Two-speed DCT based BEV Simulink® model

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The advantages and details of a two-speed DCT-based BEV have been introduced in Ref [22]. Here, only topics relating to braking in this new DCT structure are examined. Fig.3a depicts the two-speed DCT-based powertrain topology, and Fig.3b shows the powertrain's installation on the test bench used in this study. The test rig incorporates a high rotational inertia provided by four railway wheels to mimic the linear inertia of a moving vehicle.

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The benefits of using front wheel drive in traditional ICE vehicles carry over to BEVs, such as lower cost, simpler design, control and manufacture, and greater boot space. Furthermore, for BEVs there is the additional advantage that regenerative braking has greater energy recovery potential on the front axle compared to the rear axle due to load transfer. The dynamic added weight on the front axle when braking or on the rear axle when accelerating is expressed:

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$$\Delta Weight = amh_g/w \quad (2)$$

146

where a is the vehicle longitudinal acceleration, h_g is the height of the centre of mass, w is the wheelbase length and m is the total vehicle mass [23]. Fig.4 gives the ratio of the normal forces on the front and rear wheels at different deceleration rates of specification Table 1A. The ratio increases from 1.15 at constant speed to approximately 1.54 at 1 g (9.81 ms^{-2}) deceleration. The normal wheel load determines the maximum available friction force given the friction coefficient μ between a specific road and tyre, according to:

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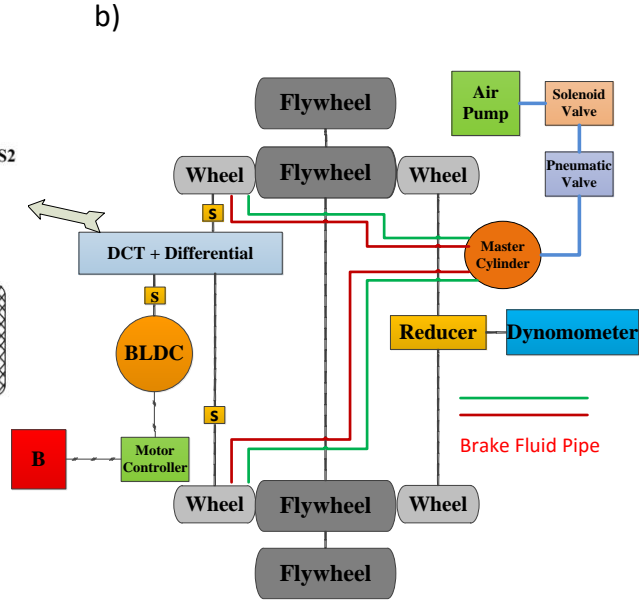
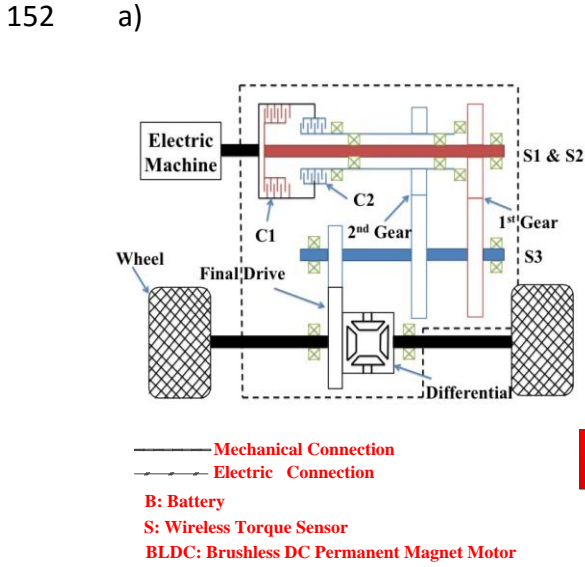
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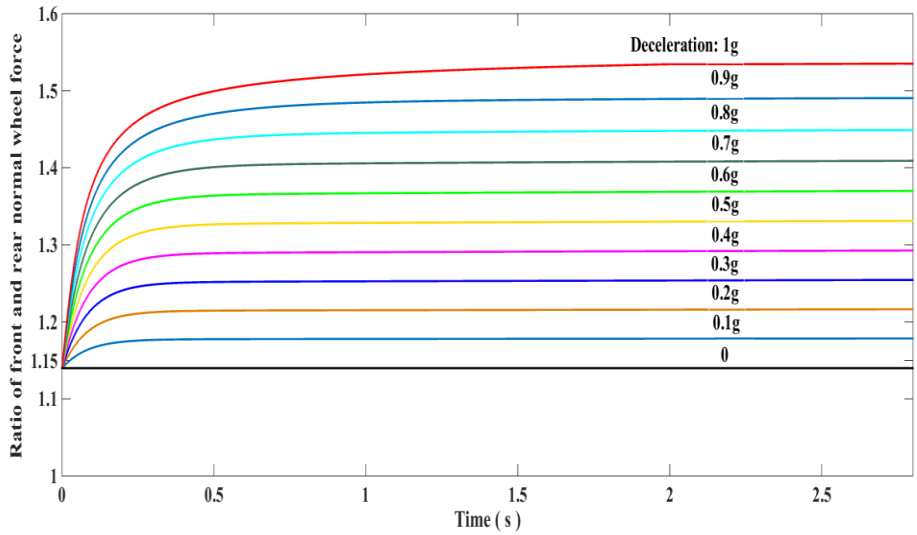
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$$F_{friction} = \mu F_{normal} \quad (3)$$



154 Figure 3: Schematic diagrams of: a) the Two-Speed DCT-based BEV powertrain topology; and b)
 155 the test bench.

156 Thus, the additional normal load on the front axle during braking enables greater regenerative
 157 braking from a front-mounted motor.



159 Figure 4: Ratio of the normal loads on the front and rear wheels during braking for a typical city
 160 vehicle chassis

161 **4. Braking Regulations and Proposed Testing Maneuvers**

162 In addition to the braking stability and performance testing procedures implemented in
163 conventional vehicles, BEV which is equipped with a non-hydraulic RBS need specialized testing
164 to isolate any potential system failures. For example, with the regenerated energy typically
165 being deposited in the battery, any effect on the RBS from the battery being full charged must
166 be tested.

167 In Europe, general safety requirements for new vehicles are legislated in Regulation (EC) No
168 661/2009 [24]. Specific requirements for braking systems are legislated by one or other of the
169 following UNECE Regulations depending on the vehicle type and mass, the first Regulation
170 applying to cars (category M1 being passenger vehicles of up to 8 passenger seats with
171 maximum laden mass less than 3.5 tonnes):

- 172 • ECE Regulation 13H for light passenger vehicles (M1) and optionally light goods vehicles
173 (N1) [25]
- 174 • ECE Regulation 13 for virtually all other vehicles [26]

175 ECE 13H and 13 divide the types of regenerative braking systems into three categories and
176 describe the testing procedures in great detail [25],[27]:

- 177 • Category A: The electric regenerative system is not part of the (“service” or main)
178 braking system. Typically, the function and the braking feeling reflected to the driver are
179 similar to engine braking in ICE vehicles.
- 180 • Category B Non-Phased: The electric regenerative system is part of the braking system
181 and regeneration commences or is increased when the brake is applied. The electric
182 regenerative force starts to be developed at the same time as or slightly after the
183 conventional friction brakes. This is also described as a parallel blended braking system.
- 184 • Category B Phased: The electric regenerative system is part of the braking system and
185 the regenerative force can be developed ahead of any braking from the conventional
186 friction brakes. This is also known as a serial blended braking system. This system allows
187 the maximum amount of regenerative energy to be recovered.

188 Whichever the type of regenerative braking system, ECE 13H and 13 have the compulsory
189 requirement of granting any Anti-Lock Braking System (ABS) an override priority to control
190 braking. Similar procedures are presented in the United States National Highway Traffic Safety
191 Administration [28].

192 To demonstrate compliance of the aforementioned regulations, the following specially designed
193 maneuvers [27] and typical driving cycles are selected to test blended braking systems on BEV:

- 194 • Single straight line braking with piecewise braking force;
- 195 • The cooperation of ABS, Electronic Braking Force Distribution (EBD) and RBS;

- 196 • Load varying braking;
- 197 • Gear shift during braking;
- 198 • NEDC, UDDS, HWFET, LA92 and JP1015 [29–33];

199 5. Braking Strategies

200 5.1 Regenerative braking capability

201 Compared to hydraulic braking systems (HBS), the available regenerative braking torque is
 202 restricted by many factors, including the maximum available motor torque (which is a function
 203 of motor speed), the transmission gear ratios, and the maximum acceptable battery current.
 204 Therefore, the HBS must be ready to automatically compensate for any unexpected electric
 205 braking absence or diminishment, at any time. Furthermore, the HBS must be ready to adjust its
 206 braking output torque to an appropriate level to meet the driver’s deceleration demand when
 207 the driving conditions change, for example if the vehicle hits a patch of ice.

208 The available regenerative braking on the front wheels is restricted by the motor peak output
 209 torque, the speed and the gear ratio. As we can see from Eq.5, the maximum braking force from
 210 the motor of specification Table 1A is limited to approximately 5 kN when the vehicle runs in 2nd
 211 gear. Even when the vehicle runs in 1st gear with a bigger torque amplification ratio, shown in
 212 Eq.4, the available maximum motor braking force is only 8 kN. Because the peak motor torque
 213 can only be supplied up to a certain speed, namely 2500 rpm for the motor of the specification
 214 of Table 1A, These maximum torques are only available during the starting period until each
 215 gear’s ‘turning point’, given by Eq.6 and Eq.7, above which the maximum available braking
 216 torque drops as shown by the top operating boundary curves of Fig.5. For this reason,
 217 mechanical braking is still necessary for BEVs, in addition to the safety concerns.

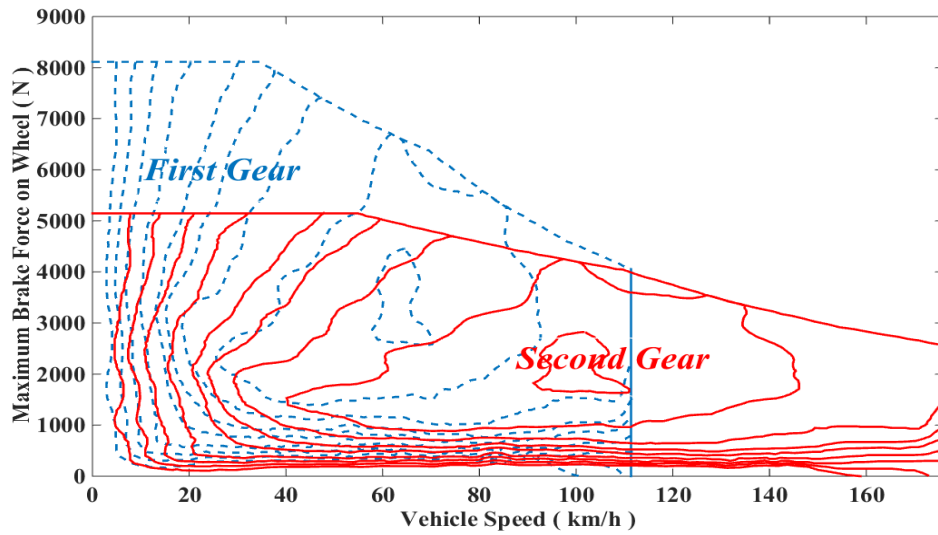
218 For mild or moderate braking in the normal speed range, the required braking force can be
 219 supplied by the motor alone. However, under heavy braking or for the vehicle cruising at high
 220 speed, the motor has to cooperate with mechanical friction braking to stop the vehicle jointly.

$$Brake_{max_1}: T_{max}i_1/r = 300 \times 8.45/0.3125 N = 8112 N \quad (4)$$

$$Brake_{max_2}: T_{max}i_2/r = 300 \times 5.36/0.3125 N = 5146 N \quad (5)$$

$$Turning\ point\ vehicle\ speed\ in\ 1^{st}\ gear: \frac{2500 \times 2 \times \pi \times 0.3125 \times 3.6}{8.45 \times 60} = 35\ km \quad (6)$$

$$Turning\ point\ vehicle\ speed\ in\ 2^{nd}\ gear: \frac{2500 \times 2 \times \pi \times 0.3125 \times 3.6}{5.36 \times 60} = 55\ km \quad (7)$$



221

222 Figure 5: Available operating region of the motor braking force on the front wheels in different
 223 gears, also showing contours of motor efficiency.

224 5.2 Stability and controllability in braking

225 Backward-sloping colored lines in Fig.6 are the lines of constant total braking force,
 226 corresponding to the indicated deceleration values (as multiples of g). Eq.8 and Eq.9 give the
 227 maximum available friction force for front and rear tyres as a function of the road-tire friction
 228 coefficient.

$$F_{bf} = \mu mg(L_b + zh_g)/L \quad (8)$$

$$F_{br} = \mu mg(L_a - zh_g)/L \quad (9)$$

229 where F_{bf} and F_{br} are the dynamic maximum friction force on front and rear wheels during
 230 decelerating based on load transfer. L_a and L_b are the distance from wheel centre to the CoM.
 231 The total maximum friction force is

$$\text{Maximum } (F_{bf} + F_{br}) = \mu mg \quad (10)$$

232 The vertical and horizontal black dash-dot lines represent the maximum available friction force
 233 based on different friction factors μ and the vehicle specification in Table.1A (see the Appendix).
 234 In other words, if the braking force applied to the wheels exceeds the critical threshold on a
 235 particular μ road, the wheel will lock. Generally, μ is less than 1.2, which means the maximum
 236 deceleration should be lower than 1.2g to avoid wheel locking, although the deceleration can
 237 go over 3g by improving vehicle aerodynamics structure and driving on a specially designed
 238 road, e.g. as is the case in Formula 1 racing. In this paper, considering the various road
 239 conditions and tire types used by the majority of passenger vehicles, which together determine

240 the friction factor, the maximum μ is set to 0.9 for safety at the cost of wasting some braking
241 capability. The two red dash-dot bolt lines in Fig.6 are the braking force limitations of front and
242 rear wheels in this paper. For some special low μ road conditions such as wet and snow, the
243 wheel locking risk generated by hard braking will be handled by ABS.

244 Solid blue line I joins the operating points of maximum total force for varying friction coefficient.
245 If the front/rear wheel braking force distribution ratios always follow this blue curve, known as
246 'Ideal' braking force distribution ratio, vehicle will make the maximum utilization of road-tyre
247 friction force and ensure the most stability and controllability in braking. For all load conditions,
248 UNECE Regulations demand that the adhesion coefficient utilization curve of the rear axle must
249 not be higher than the curve for the front axle [34,35]. With reference to Fig.6, this means that
250 the force distribution curve should always be lower than the ideal curve.

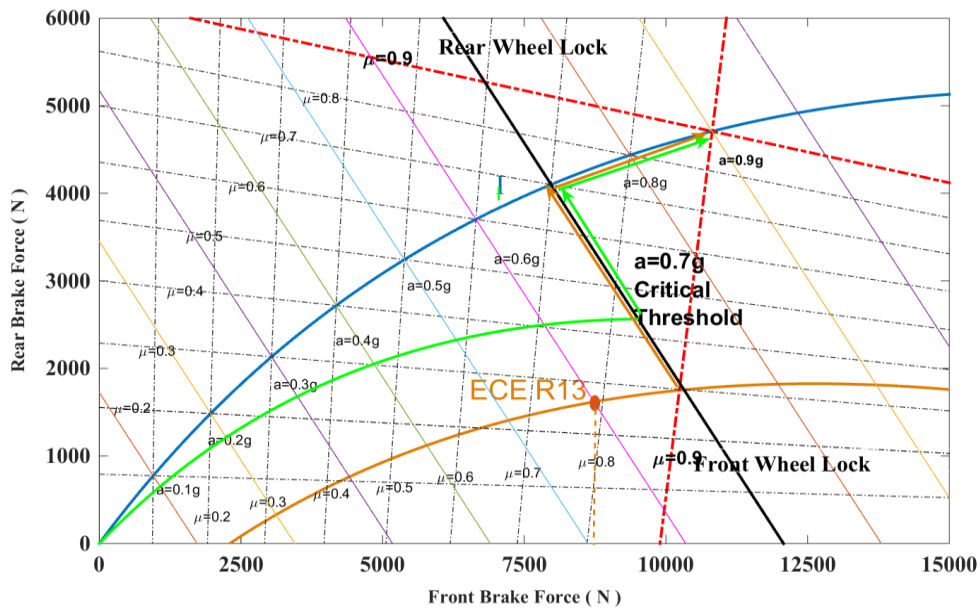
251 There are lots of braking related regulations and directives from worldwide governments and
252 organizations, but regulations in most countries are very similar to ensure that road vehicles are
253 designed and constructed to decelerate safely and efficiently under all conditions of operation.
254 The European UN Regulation 13-H is recognized as a valid type-approval standard in all EU and
255 many non-EU countries, with members of the 1958 Agreement including Japan, USA, Canada,
256 Australia, Korea, China, India, and Malaysia. It requires that, for all states of loading, two-axle
257 vehicles that are not equipped with ABS, the rate of braking must meet the requirement of
258 Eq.11

$$z = a/g > 0.1 + 0.85(\mu - 0.2) \quad (11)$$

259 Although for the weight of the vehicle assumed in the specification of Table 1.A, UN Regulation
260 13-H actually applies, in which the 0.85 factor in Eq.11 is replaced by 0.70, we will adopt the
261 more demanding 0.85 factor of Regulation 13 assuming a greater margin of safety is desired.
262 The distribution of braking forces is given by Eq.12 and Eq.13, which is shown by the golden
263 curve in Fig.6.

$$F_{bf} = (L_b + zh_g)(z + 0.07)g/0.85L \quad (12)$$

$$F_{br} = mgz - F_{bf} \quad (13)$$



264

265 Figure 6: Braking force distribution on front and rear wheels for the vehicle of specification

266 In summary, the area, restricted by solid blue 'Ideal braking force distribution' curve, red dash-dot 'maximum available friction braking force on front wheels' curve, golden ECE R13-H
 267 regulation curve, and horizontal axis, indicates the range of available braking force distribution
 268 ratios of front and rear wheels.
 269

270 **5.3 Safety (Motor Priority) Strategy**

271 Braking safety, including stopping distance, stability and controllability, is always the top priority
 272 and is likely to be tested by bad weather and road conditions. The motion of a wheel in a
 273 normal driving vehicle consists of two parts, namely rolling and sliding, which causes a
 274 difference between the speeds of the vehicle and the wheel. In the longitudinal direction, if the
 275 force applied to the wheel by brake calipers exceeds the maximum available friction force
 276 between the tires and ground, then the relative motion between the tires and road will change
 277 from a mix of sliding and rolling to pure sliding (Eq.3). This phenomenon is known as 'wheel
 278 lock'. Specific to the blended braking system, it occurs when the total braking force from the
 279 motor and calipers exceeds the friction force from the ground:

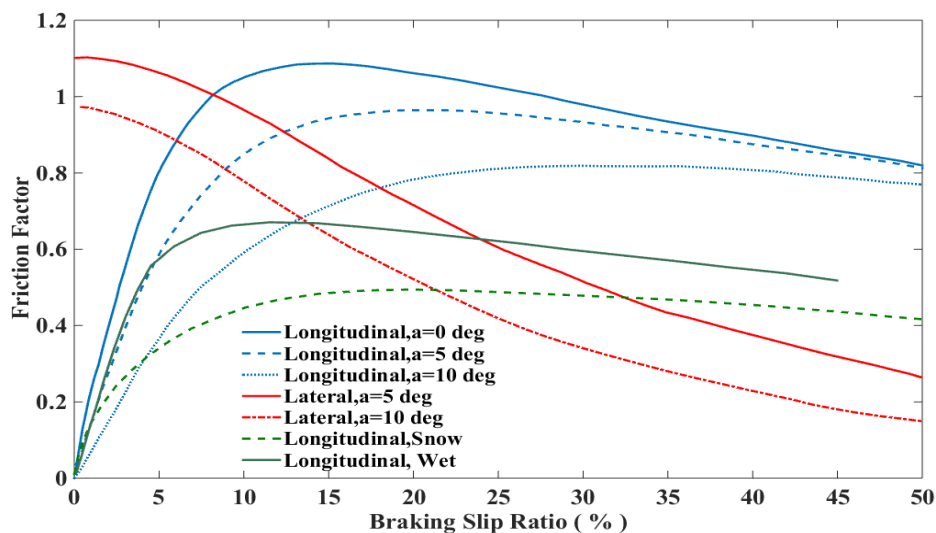
$$f_{regen} + f_{caliper} > f_{brake_friction} = mg\mu \quad (14)$$

280 The wheel slip ratio is defined as the ratio of difference between the rotational speed of the
 281 wheel and the translational velocity of the wheel center:

$$\lambda = \Delta v/v = (\omega r_{dyn} - v)/v \quad (15)$$

282 ω is the wheel rotation speed and r_{dyn} represents the dynamic radius of the wheel, which is
 283 determined indirectly by measuring the travel distance per rotation circle. λ is a value from 0 to
 284 1 representing the motion of wheel from freely rolling to lock. The solid blue curve in Fig.7
 285 shows the dependence of the friction factor μ on the longitudinal slip ratio λ on dry asphalt
 286 pavement. The μ drops significantly when the vehicle is travelling on a wet or snow-covered
 287 road, which are presented by solid and dashed green curves. Moreover, a steering angle causes
 288 the friction factor to fall as well.

289 The force in the lateral direction of the road-tire contact surface directly affects the direction
 290 controllability of the vehicle. A locked wheel cannot generate lateral force to offset the sideslip
 291 trend, when cornering or unintentionally steering during an emergency brake, resulting in
 292 unnecessary under-steering and uncontrollable over-steering. As shown in Fig.7, the lateral
 293 friction factor falls dramatically with increased longitudinal braking slip ratio. For example, for a
 294 wheel with 5° steering angle and 20% longitudinal slip ratio, the lateral friction factor only
 295 equals half that of pure straight driving. When the longitudinal slip ratio hits 100% (wheel lock),
 296 steering input has no result on yaw motion because the front tires are saturated, and no lateral
 297 force can be generated. If it happens to the front wheel, the vehicle will lose steering ability.
 298 However, there is no directional instability because whenever the lateral movement of the front
 299 wheels occurs, a self-correcting moment due to the inertial force of the vehicle about the yaw
 300 center of the rear axle will be developed [36]. Consequently, it tends to bring the vehicle back to
 301 a straight line path. In contrast, if the rear wheels are locked, they lose their capability to
 302 generate the required side forces and the rear end might start to slide sideways, losing
 303 directional stability. The omitted red arrows on the rear wheel and front wheels, in the ‘Over-
 304 steering’ and ‘Under-steering’ Fig.6 schematics, indicate the locked wheels and lost lateral force.
 305 The black arrows show the potential movement directions.



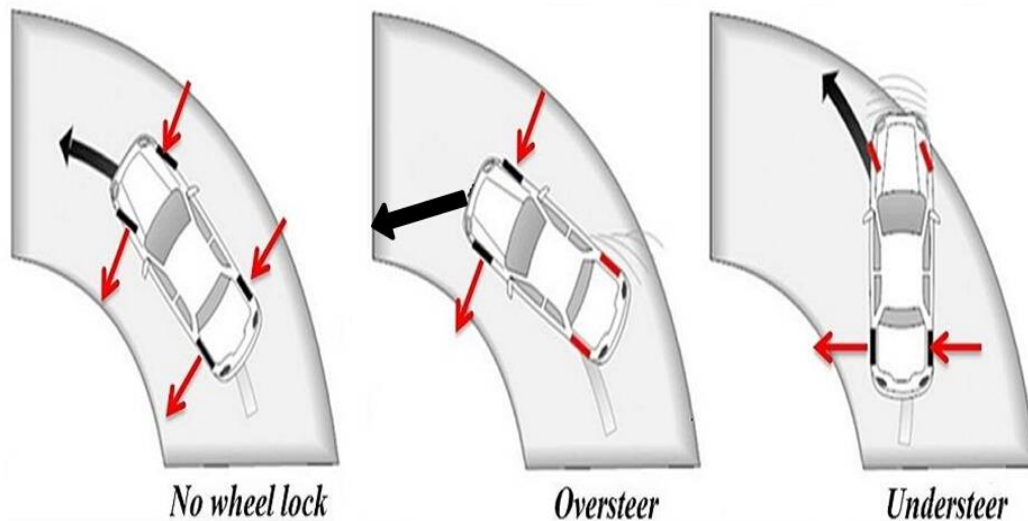
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307 Figure 7: The influence of slip ratio, steering angle (“a” in degrees) and road condition on
 308 friction factor [37]

309 The most 'Safety' strategy should properly distribute braking force to each wheel, keeping their
310 operating points below the maximum front and rear road friction curves (Red dash-dot bolt
311 lines in Fig.6). Use this strategy at maximum braking all wheels lock simultaneously.

312 The critical threshold of deceleration rate in an emergency brake, also known as ABS activation
313 threshold, is set as 0.7g in this paper. It is worth noting that the thresholds vary according to
314 wet or dry road conditions. Wet road conditions trigger ABS activation when deceleration
315 exceeds 0.65g, whereas dry road conditions trigger ABS activation when deceleration exceeds
316 0.90g [38]. ABS is assumed to activate if adjustable maximum deceleration thresholds are
317 exceeded. There are two main reasons why the method used in the model to determine ABS
318 activation was employed. For the ABS Activation condition and for emergency braking
319 conditions that use ABS activation as triggering criteria, is simply set as 0.7g. First, this threshold
320 is widely used in a lot of applications, testing procedures and researching reports [39–
321 42]. Second, the incidence of braking events with peak decelerations above 0.7g is relatively
322 rare, occurring, on average, approximately once every 4800 [38].

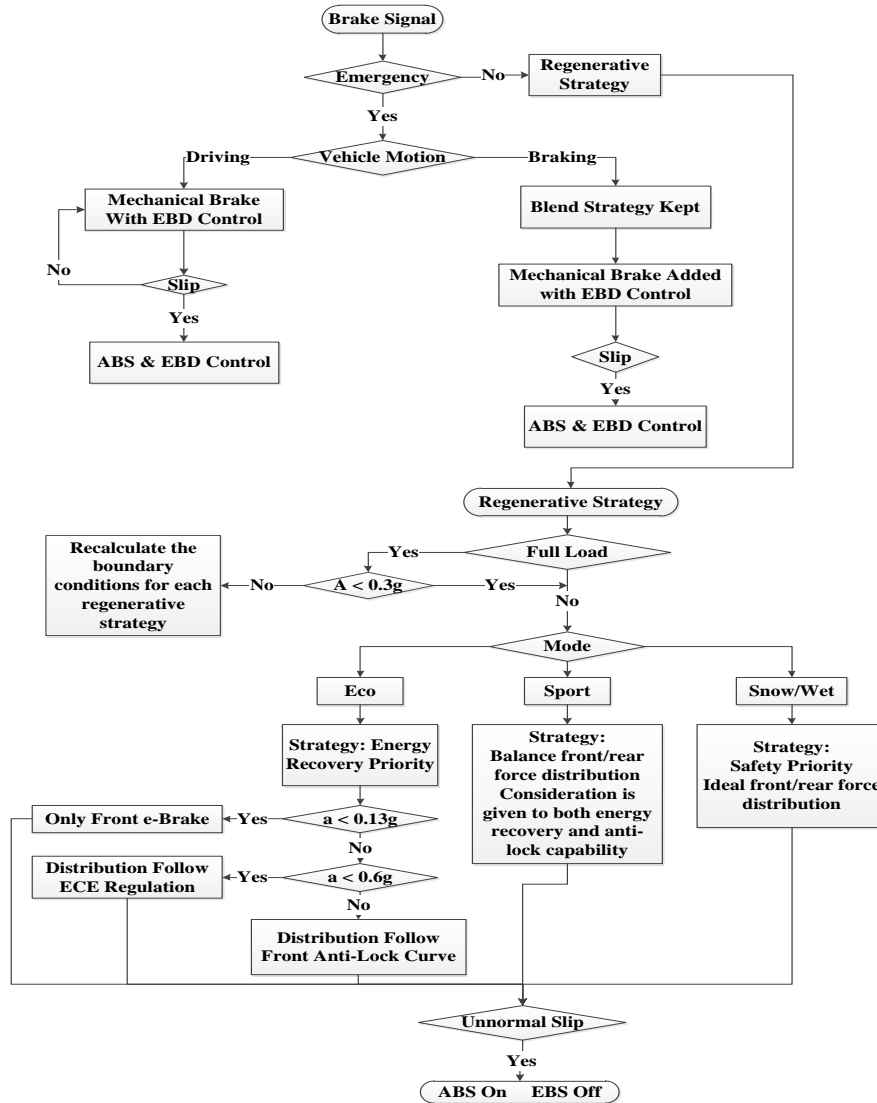
323 Therefore, if the strategy is manually set to 'Safety', or if the deceleration rate goes over this
324 threshold value in other strategies, then the braking force must be ideally distributed to the
325 front and rear wheels, i.e. on the blue curve I in Fig.6, To recapture as much braking energy as
326 possible, 'Safety (Motor Priority)' strategy is proposed, in which the motor takes responsibility
327 for supplying the required front torque until reaching its maximum ability. The principal and
328 details of this strategy are presented in Fig.9. Of course, any wheel lock occurrence would be
329 detected and avoided by ABS. Non-ideal braking force distribution strategies result in
330 asynchronous wheel locking time, which can cause over-steering or under-steering.



332 Figure 8: Schematic over-steering and under-steering when wheels lock, shown in red. Red
333 arrows show lateral forces on unlocked wheels.

334 **5.4 Eco Strategy**

335 To maximize the recovery of braking energy, only the front electric brake is utilized while
 336 deceleration remains below the critical intersection point, which is determined by the
 337 horizontal axis and ECE R13-H regulation curve. After that, the ratio of front and rear axle
 338 braking force follows the ECE regulation curve, the golden one in Fig.6, until the deceleration
 339 triggers the emergency situation-0.7g. Then, the distribution strategy jumps to the 'Safety
 340 (Motor Priority)'.



341

342

Figure 9: The Cooperation of RBS, EBD and ABS

343 **5.5 Sport Strategy**

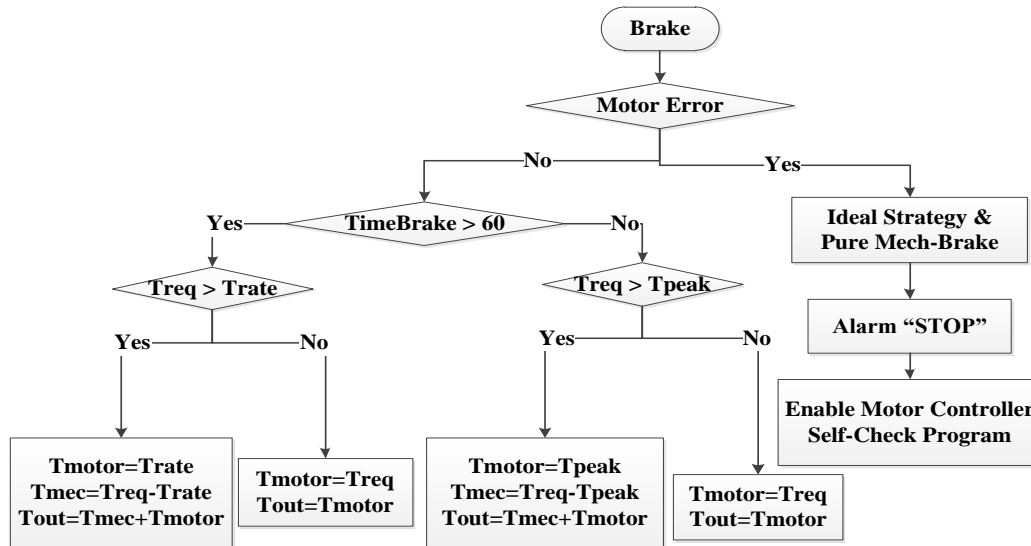
344 Aggressive driving is desired when the driver intentionally selects this strategy. High
345 acceleration and deceleration and more frequent start-stops may increase the possibility of
346 motor failure. Therefore, any motor failure caused by the frequent and fast changed torque
347 requirements should be avoided. This requires that the demanded motor torque never exceeds
348 the motor ability, regardless of the motor speed and gear ratio. Because the available electric
349 brake varies according to the motor speed and gear ratio for a full pedal brake. The minimum
350 available electric force in a full pedal brake ($Regen_{min}$) appears at the highest motor speed with
351 the minimum gear ratio, which are 8000 rpm and 5.36 respectively in the specification of
352 Table.1A. To ensure this critical value is always lower than the required electric brake, the ratio
353 of minimum full pedal electric brake force and the theoretical maximum brake force (mu equals
354 1) is defined as the ratio of regenerative/total required brake:

$$\frac{Regen_{min}}{Friction_{max}} = \frac{T_{min} \times i_{g2}}{m \times g \times \mu} = \frac{150 \times 5.36}{0.3125 \times 1500 \times 9.81 \times 0.9} = 19.4\% \quad (16)$$

355 Compared to the Eco strategy when electric braking has the priority and mechanical braking
356 works as a supplement, the mechanical braking torque and the motor supplied braking torque
357 act jointly all the time in Sport strategy. Based on the braking force distribution in Safety
358 strategy, additional 15.8% of total required braking force is applied to the front axle, comes from
359 motor. Consequently, if motor works well, the friction and electric braking force will increase
360 continuously and smoothly without any braking source alternation, at a fixed ratio. If motor out
361 of order, the mechanical braking will work alone with an 'Ideal' front/rear distribution ratio to
362 guarantee a stable and controllable deceleration.

363 **5.6 Motor Fault Insurance Strategy**

364 Generally, electromagnetic equipment is considered to be not as robust as a hydraulic system.
365 Specific to the blended braking system, motor downtime is a very dangerous situation, whether
366 caused by IGBT failure or temperature protection. Especially during long continuous downhill
367 braking, high current may cause motor overheating and trigger a protection mechanism,
368 especially if the cooling system is out of order. It is not common, but is a serious event. A fail-
369 safe provision of hydraulic braking should be activated immediately when electric braking
370 torque is limited or a 'torque error' is detected. Including consideration of motor overload and
371 error redundancy, a fail-safe mechanism for the motor is presented in Fig.10.



372

373

Figure 10: Motor control & fail-safe strategy

374 6. Brake Performance Analysis

375 The goal of automotive braking system design, whether for conventional or blended systems, is
 376 to achieve a comfortable and reliable deceleration at the request of the driver. In addition, the
 377 vehicle must be brought to a stop as soon as possible in an emergency situation, while
 378 maintaining dynamic stability and controllability.

379 6.1 Single straight line braking

380 In this testing profile, the vehicle begins to decelerate from 100 km/h to 92.8 km/h in 2 seconds,
 381 then, slows down to 60.4 in 3 seconds, and finally brakes to a full stop in the next 2 seconds.
 382 The deceleration increases from 0.1g (Mild Braking) to 0.3g (Moderate Braking) to 0.9g
 383 (Emergency Braking) in three stages. Fig. 9 shows the braking forces and wheel slip versus time
 384 for the different strategies introduced in Sec. 5 and Fig. 11 plots the trajectory of the
 385 distribution of braking forces to the axles for each strategy.

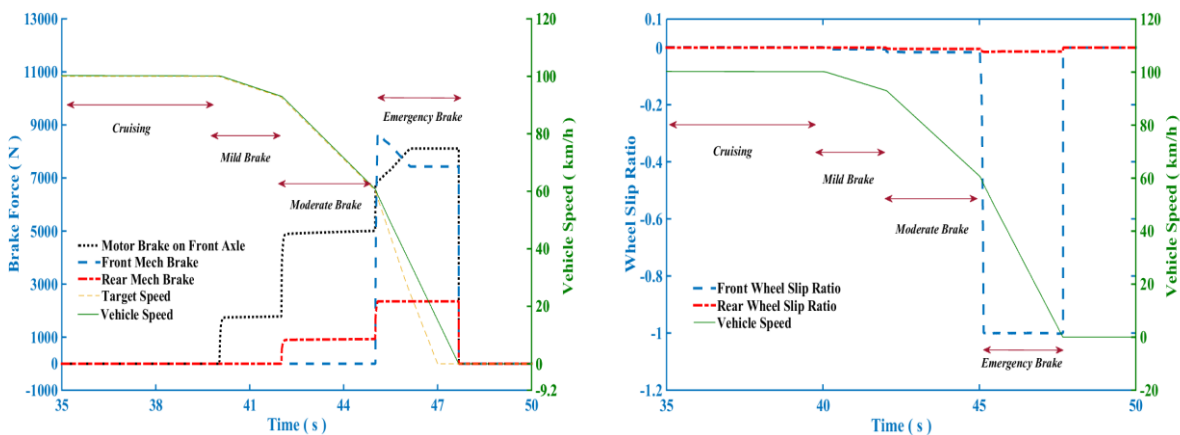
386 As shown in Fig.11 (a) and (b), the Eco strategy distributes the required braking force to the
 387 front axle as much as possible under the limitation of laws and regulations. Most of the front
 388 braking force is supplied by the motor, which is represented by the black dotted curve. During
 389 mild braking, all the required braking force is supplied by the front-wheel regenerative brake.
 390 During moderate braking, front electric braking and rear friction braking, which is represented
 391 by the red dash-dot curve, share the increased braking force demand. Finally, during emergency
 392 braking, front friction braking (blue dash curve) increases sharply to compensate for the
 393 insufficient front braking force, due to the output torque limitation of the motor. It is apparent
 394 from Fig.12 that the purple curve strategy should be switched to the safety strategy, red

395 hexagram curve, to avoid any wheel locking when the front or rear braking force goes over the
 396 'wheel lock' line.

397 Therefore, if the strategy is not already chosen as 'Safety', the strategy should be automatically
 398 switched to 'Safety' when emergency braking occurs. The braking force distribution ratios of
 399 'Eco' and 'Sport', represented by star and triangle curves in Fig.12, are automatically switched to
 400 'safety' when deceleration gets close to 0.7g. As a result, both of them have satisfactory braking
 401 performance, as demonstrated by the actual speed following the target speed in Fig.11 (c) and
 402 (e). No braking force comes from the front friction brake in the 'Eco & Safety' strategy before
 403 emergency braking arises, after which the distribution ratio is switched to the 'Sport & Safety'
 404 strategy.

405 There is no difference between the 'Safety' and 'Safety (Motor Priority)' strategies with regard
 406 to the front/rear braking force ratio. Nevertheless, the 'Safety (Motor Priority)' strategy differs
 407 from the 'Safety' strategy by introducing braking force in series mode. Firstly, the electric brake
 408 supplies braking torque as much as possible until reaching its limitation, then, compensation is
 409 made by hydraulic friction braking on the front wheels to meet the driver's deceleration
 410 demand.

411 Comparing these four strategies, the safety performance of 'Eco' (no switching) strategy is the
 412 worst. It cannot stop the vehicle in a satisfied distance in an emergency case due to the wheel
 413 locking, although it can recover the most kinetic energy. Because the 'Safety (Motor Priority)'
 414 strategy always guarantees front and rear wheels lock simultaneously, it has the best safety
 415 performance and doesn't need to take the risk of strategy switching failure, like 'Eco & Safety' or
 416 'Sport & Safety'. Furthermore, it has a higher utilization rate of electric braking than 'Sport &
 417 Safety', because the electric brake is strictly restricted to a certain level. The 'Eco & Safety'
 418 strategy has the highest energy recovery rate and an excellent decelerating stability. However,
 419 the potential risk of failure switching between two strategies demands extra attention.



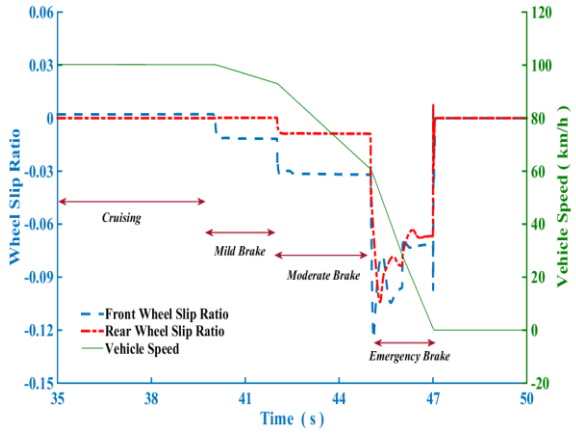
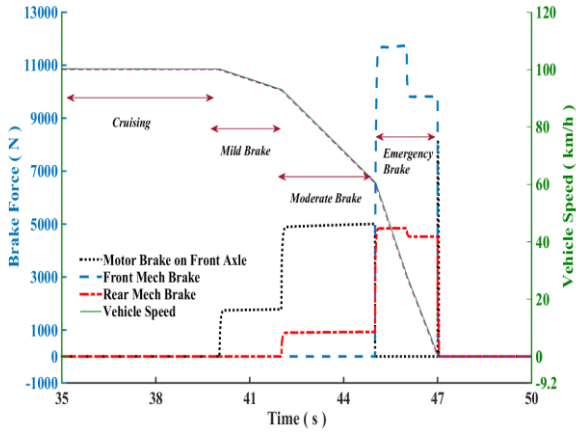
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421

(a) Braking force distribution in Eco strategy

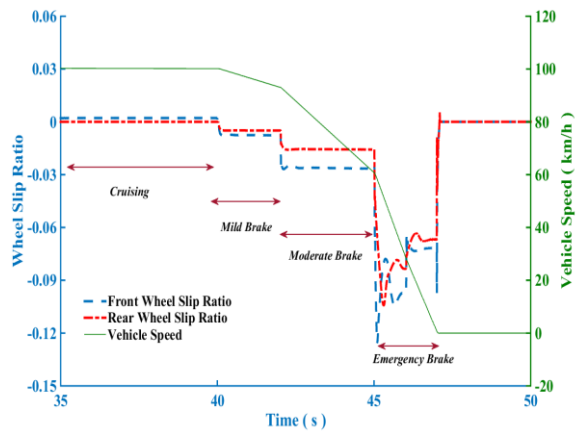
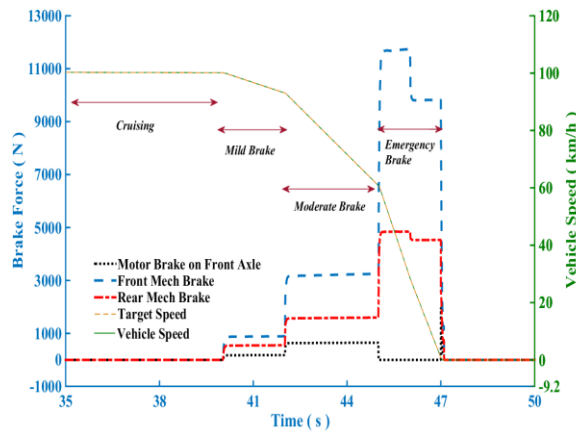
(b) Slip ratio in front & rear wheels for (a)

422



423 (c) Braking force distribution in Eco & Safety strategy (d) Slip ratio in front & rear wheels for (c)

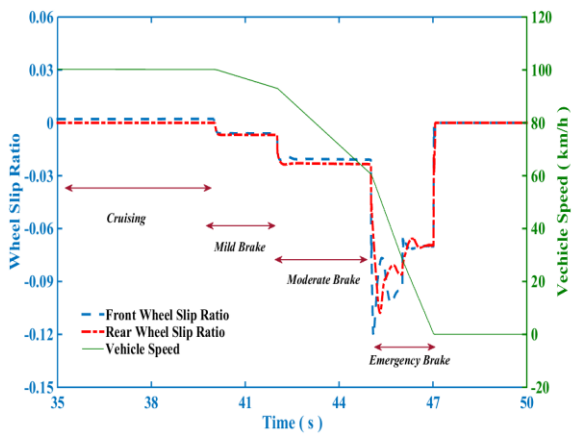
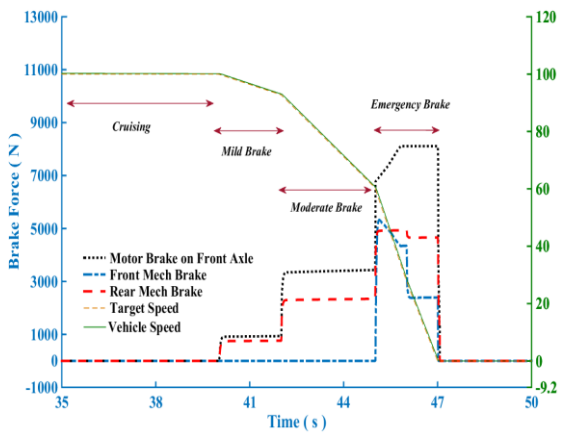
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425 (e) Braking force distribution in Sport & Safety strategy (f) Slip ratio in front & rear wheels for (e)

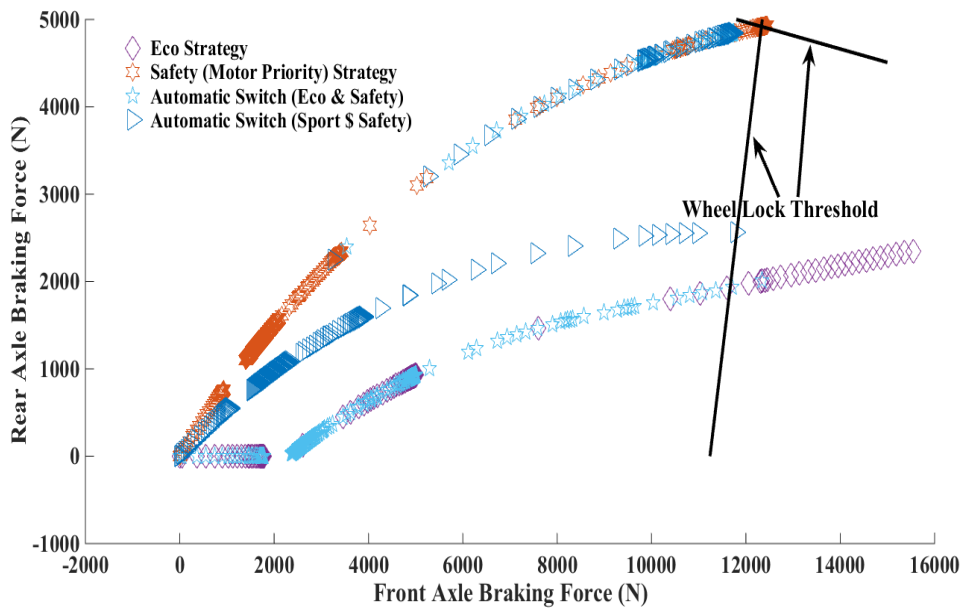
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428 (g) Braking force distribution in Safety (Motor Priority) strategy (h) Slip ratio in front & rear
429 wheels for (g)

430 Figure 11: Straight line braking force distribution and wheel slip ratios for: (a) and (b) Eco
431 strategy; (c) and (d) Eco & Safety strategy; (e) and (f) Sport & Safety strategy; and (g) and (h)
432 Safety strategy.



433
434 Figure 12: Front/Rear braking force distribution ratios for different strategies

435 **6.2 The cooperation of ABS, EBD and RBS**

436 In traditional ICE vehicles, to ensure the maximum braking force is available and to avoid wheel
437 slipping, driver assistance systems are integrated into the vehicle such as ABS and EBD. The
438 implementation relies on the hydraulic accumulators and actuators to work corporately with a
439 complex relationship. In brief, the EBD supplies appropriate forces to help vehicle running on
440 the initial intended path, while the ABS stands by ready to prevent any wheel lock. However,
441 with an RBS seeking braking energy recovery, the strategies and intervention time of hydraulic
442 brake systems may change.

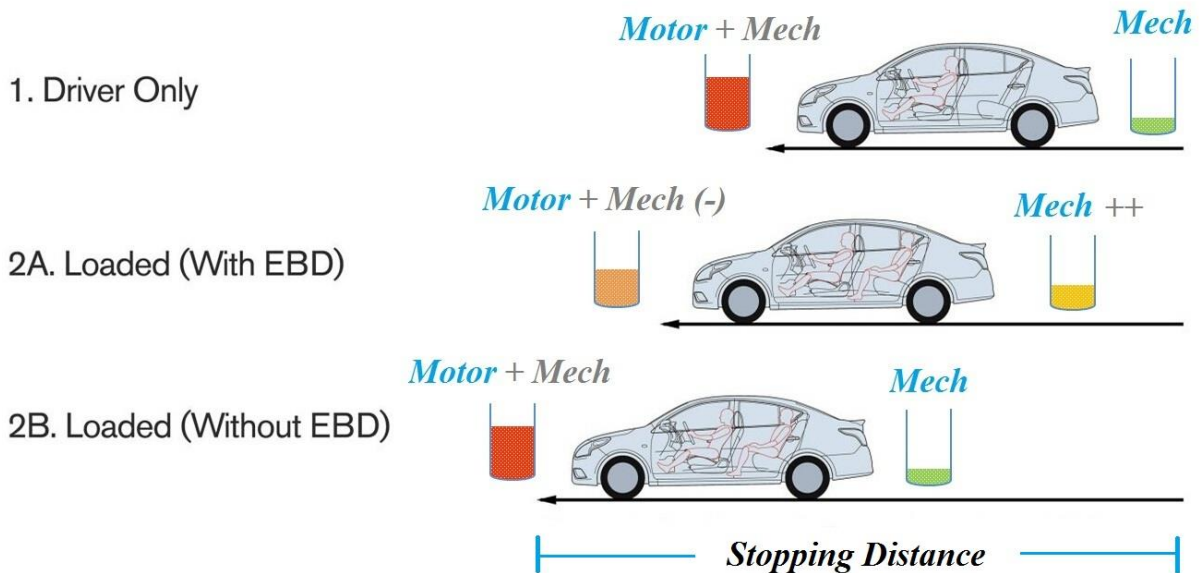
443 Deceleration rates varying braking and Split Mu braking shows big challenges for blended
444 braking strategy design. In this paper, the safety-oriented cooperation of RBS, ABS and EBD is
445 analyzed and proposed, without going into the details of ABS or EBD.

446 **6.2.1 RBS with EBD**

447 When the deceleration intention is detected from the brake pedal in RBS, the motor begins to
448 apply braking torque on the front wheels; meanwhile, pressure is established in the rear

449 hydraulic actuator to decelerate the rear wheels. The braking force variation on the front and
450 rear wheels, which is usually implemented by tuning the hydraulic accumulator and actuators,
451 now can be provided by the motor from the viewpoint of energy recovery.

452 Fig.13 shows how the additional load affects braking performance and how a shorter stopping
453 distance is achieved by RBS & EBD acting jointly. The variations of braking force distribution for
454 normal load and added load with/without EBD are demonstrated by bar indicators. According to
455 Fig.4, EBD should distribute more braking force on the front wheel to offset the load transfer
456 and avoid rear wheels locking. In contrast, when the vehicle is loaded with passengers or goods
457 in back rows, EBD automatically detects and redistributes more braking force on the rear wheels
458 to utilize the increased available friction force, as demonstrated in Fig.13-2A. However, the real
459 distribution ratio is kept as the previous one from the viewpoint of energy recovery, instead of
460 increasing rear braking force and reducing front braking force immediately, at the cost of a
461 longer stop distance (Fig.13-2B). However, this only happens in mild braking ($a < 0.3g$). Stopping
462 distance becomes the top concern when braking intention is detected stronger ($a > 0.3g$). The
463 braking force distribution is rebalanced to take full advantage of load transfer. Rear mechanical
464 braking force is increased, at the same time, reducing front mechanical braking and keeping
465 motor braking, or reducing motor braking if there is no mechanical brake on the front wheels.
466 The rebalance and detection procedures are described in the flowchart (Fig.9).



467

468

Figure 13: RBS Cooperate with EBD

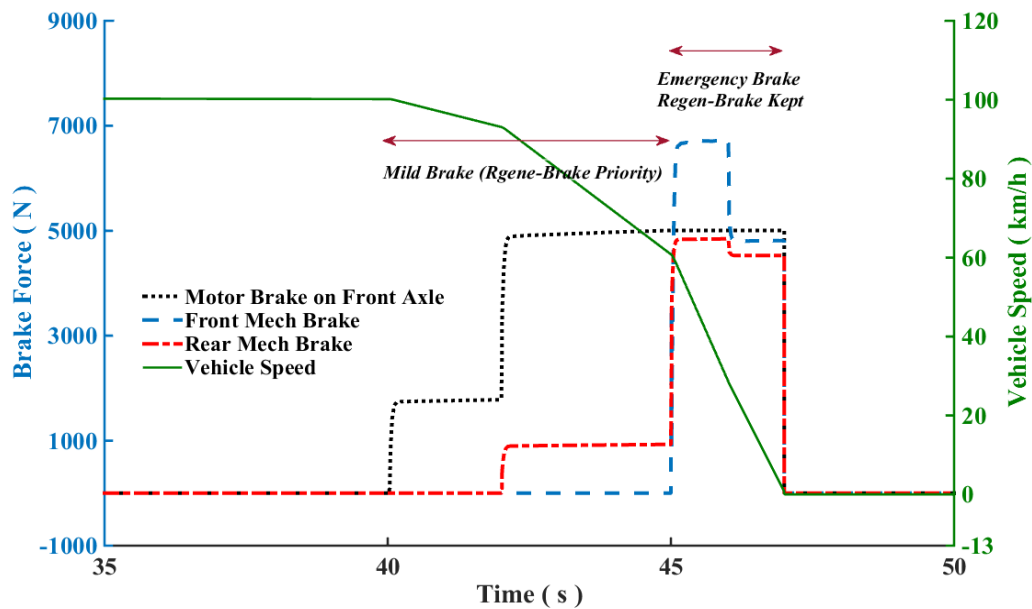
469 **6.2.2 RBS with ABS**

470 ABS becomes involved when emergency braking is activated. ABS reduces the pressure in the
471 hydraulic brake actuator of the wheel that is tending to lock. However, there are two different
472 preconditions for the blended braking system when ABS operates:

- 473 1. Emergency braking starts from driving
- 474 2. Emergency braking starts from an existing braking event

475 In case 1, emergency braking usually needs a great deal of force. Using RBS alone would
476 generate high instantaneous current in the motor, which can't be taken by the battery. Given
477 HBS has higher reliability, hydraulic ABS is given the highest priority, which means motor braking
478 does not participate in emergency braking in this situation.

479 In case 2, there is already some level of regenerative braking before the braking turns to strong.
480 With respect to safety, keeping the existed regenerative braking and using mechanical braking
481 to supply the rest of required braking force is the best choice. The detail of this strategy and the
482 testing result is included in Fig.9 and Fig.14.



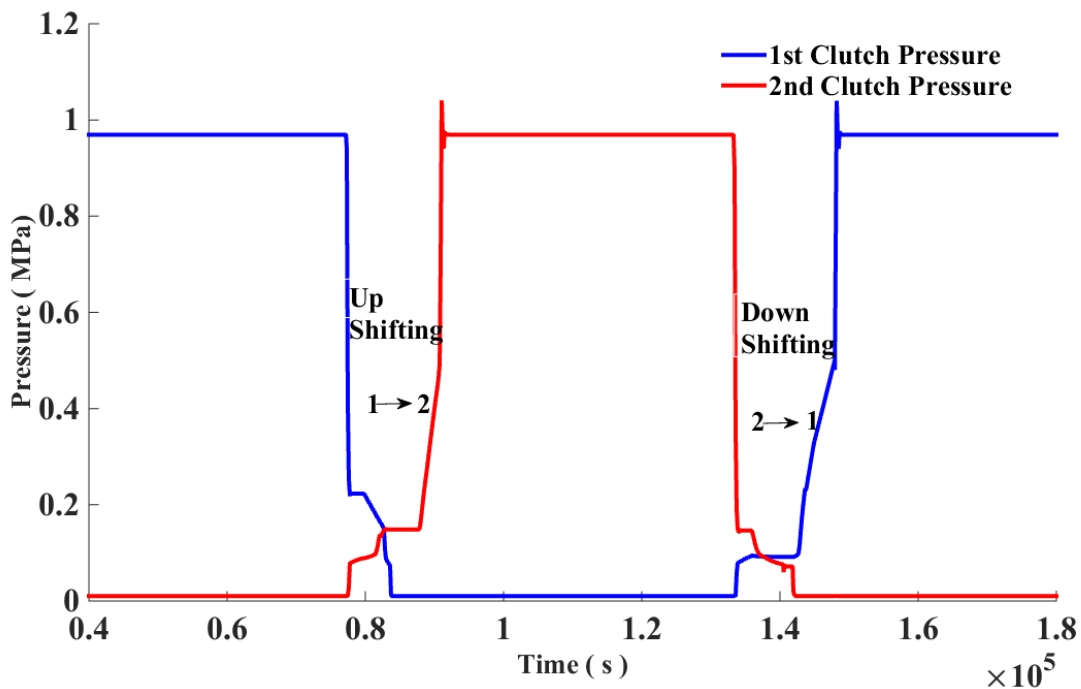
483
484 Figure 14: Emergency braking force distribution when motor torque is kept

485 **6.3 Gear Shift during Braking**

486 Unlike the conventional HBS, in which the braking force goes from the brake pedal to master
487 cylinder, hydraulic actuator, and calipers, then, directly to the wheels, electric braking goes
488 through transmissions and differentials, then acts on the driven half shafts, which are
489 connected to each wheel. On the one hand, regenerative braking from the motor may be

490 insufficient when the vehicle is running at high speed with smaller gear ratio, as shown in Fig.5.
 491 On the other hand, the torque interruption introduced by gear shifting can result in a serious
 492 potential safety issue, especially for emergency braking. Although the interruption, also known
 493 as ‘shifting torque hole’ (Fig.15), is very short in DCT, it can still be felt and can send the wrong
 494 message to the drivers, which may cause them to take unnecessary corrective measures.
 495 Theoretically, there are two potential solutions:

- 496 1) Lock out the shifting function and use the mechanical brake to supply the rest of the
 497 required braking force;
- 498 2) Use mechanical braking to supply the reduced torque during shifting, but reinstate the
 499 motor braking torque after shifting.



500
 501

Figure 15: Clutch pressure variation during shifting

502 Obviously, the second solution can recapture more braking energy by giving regenerative
 503 braking more opportunities to participate. However, it also needs a more complicated control
 504 algorithm and a higher precision in monitoring of HBS and RBS. When the shifting requirement
 505 occurs in emergency braking, considering the safety risk and energy recovery potential from
 506 emergency braking over a short period, solution 1 is the favored choice for market products.
 507 However, when the shifting requirement occurs in long-downhill road with a moderate braking,
 508 a downshifting should be allowed to increase the energy recovery rate.

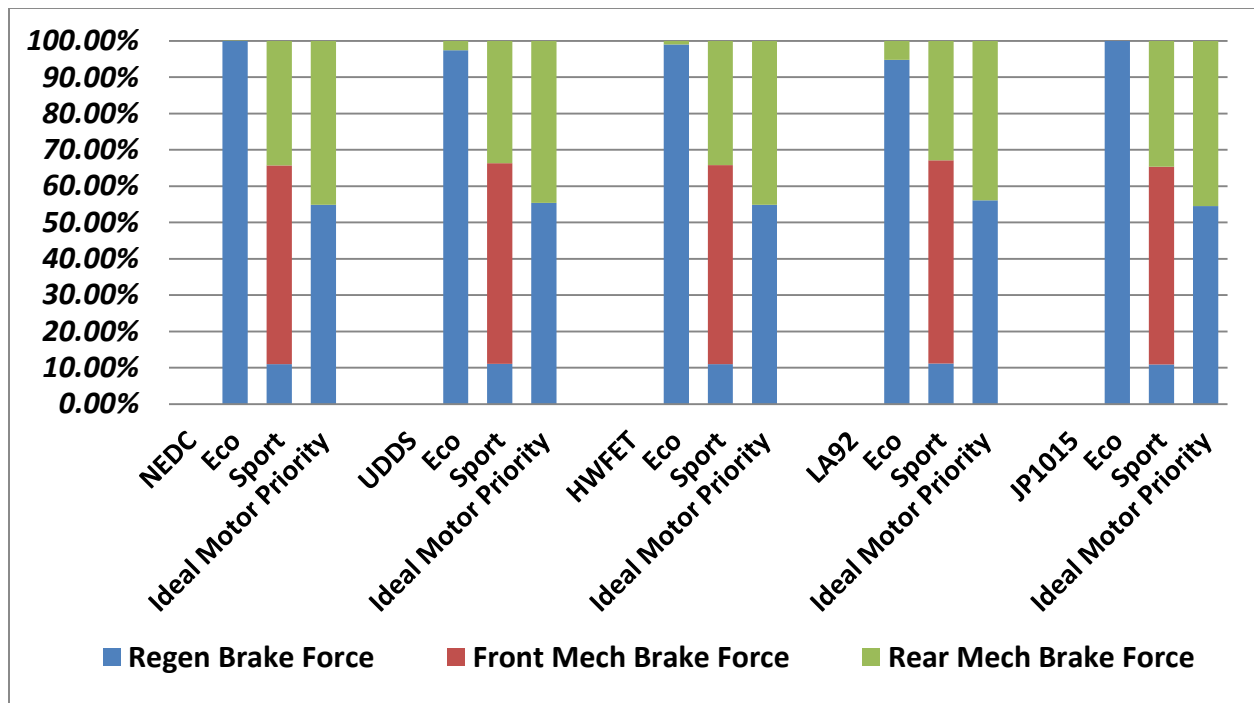
509 **6.4 Braking in Typical Cycles**

510 The following chart, Fig.16, demonstrates the braking force distribution on the front (friction &
 511 regenerative braking) and rear wheels in different strategies. The various distribution ratios
 512 result in some fluctuations of total braking force for strategies in each driving cycle.

513 For the ‘Eco’ strategy, the required braking force in NEDC, HWFET and JP1015 never exceeds the
 514 threshold of ECE R-13 regulation, so all the braking force is supplied by the motor. The two US
 515 city cycles, UDDS and LA-92, have a more aggressive braking event, and both need rear friction
 516 braking to meet the requirement of ECE R-13.

517 The ‘Sport’ strategy deliberately limits the motor’s braking ability to a safe and low level, as
 518 described in Sec 5.4. Consequently, the front and rear mechanical friction braking accounts for
 519 most of the braking, rather than regenerative braking, in all driving cycles.

520 The motor has the priority and sufficient ability in the ‘Safety (Motor Priority)’ strategy to meet
 521 the front axle braking force requirement, causing a higher utilization rate of regenerative
 522 braking. Meanwhile, the lowest likelihood of wheel locking is guaranteed by the ‘Ideal’ braking
 523 force distribution ratio. Friction braking on the front wheels plays no role in typical driving cycle
 524 deceleration in this strategy. Because motor has the sufficient ability to meet the total front axle
 525 braking force requirement.

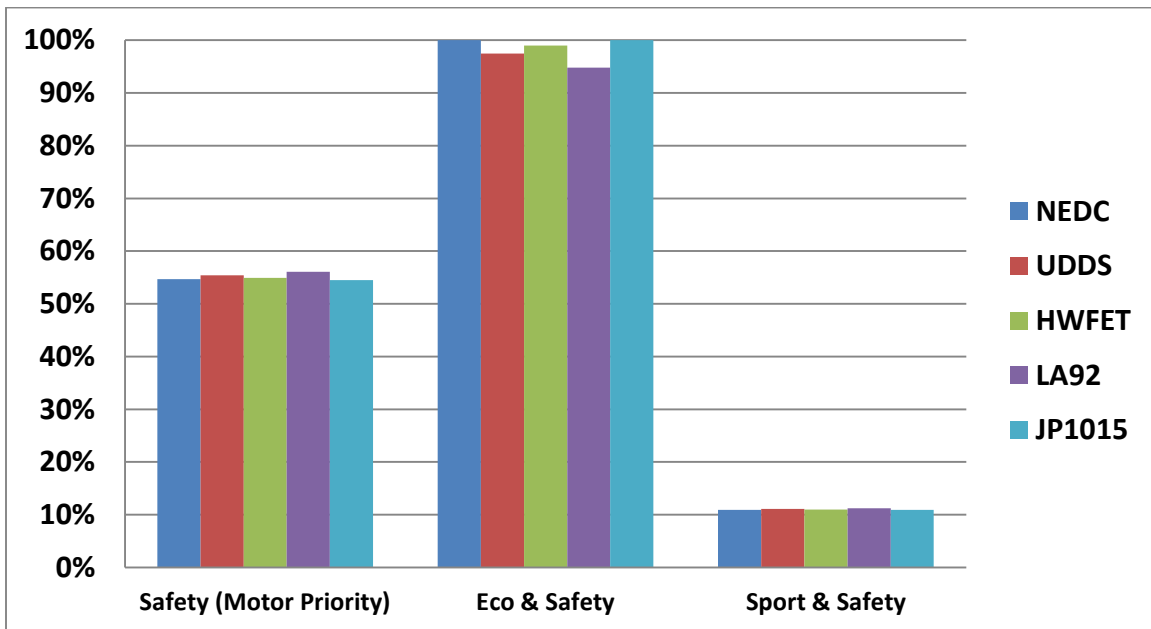


526

527 Figure 16: Braking force distribution for strategies in driving cycles

528 Eq.17 is used to evaluate the the braking energy recovery potential of strategies. The
 529 comparison of potential braking energy recovery rates in driving cycles is present in Fig.17.
 530 Thanks to the bigger capacity of motor and battery in BEV, comparing to HEV, and the moderate
 531 driving cycles, most of braking requirements can be covered by motor alone in ‘Eco & Safety’
 532 strategy. Consequently, the energy recovery rates in this strategy are almost 100%, except some
 533 higher deceleration braking events in UDDS, LA92, and HWFET needing a complementary
 534 friction braking. Subject to the distribution ratio of front and rear braking force in ‘Safety (Motor
 535 Priority)’ strategy, energy recovery rates of different cycles are all around 55%. Regarding to
 536 Fig.16, motor supplies all the required braking force on front axle. ‘Sport & Safety’ strategy
 537 achieves the highest motor failure tolerance at the cost of lowest energy recovery rates, 10% for
 538 all the cycles.

$$Energy\ Recovery\ Rate = \frac{Regenerative\ Braking\ Energy}{Total\ Braking\ Energy} \quad (17)$$



539

540 Figure 17: Braking energy recovery potential of strategies in each cycle

541 In the industry, battery energy recovery rate is widely accepted as the evaluation criterion of the
 542 regenerative braking system. The rate is defined as the ratio of the battery input energy from
 543 braking and the battery output energy for driving:

$$Q_{re} = \frac{E_{bat_{IN}}}{E_{bat_{OUT}}} \quad (18)$$

544 Table 1 shows a comparison of energy recovery rates for different driving cycles. Comparing the
 545 driving cycles, in columns, one observes that more energy can be recaptured in aggressive city
 546 cycles, UDDS and LA92, than others. The reason JP1015 has the highest recovery rate is that the
 547 required driving energy is bigger, compared to the recovered energy from braking. On the
 548 contrary, the recovery rate of HWFET is the lowest one.

549 Table 1: Energy recovery rates in term of driving cycles, plus motor failure tolerance, with +
 550 indicating a higher tolerance

Energy Recovery Rates	NEDC	UDDS	HWFET	LA92	JP1015	Controllability Lost Risk
Safety (Motor Priority)	12.4%	16.4%	8.6%	15.0%	17.8%	0
Eco & Safety	25.3%	30.4%	16.0%	24.6%	32.9%	0
Sport & Safety	2.4%	3.1%	1.8%	3.6%	3.6%	++

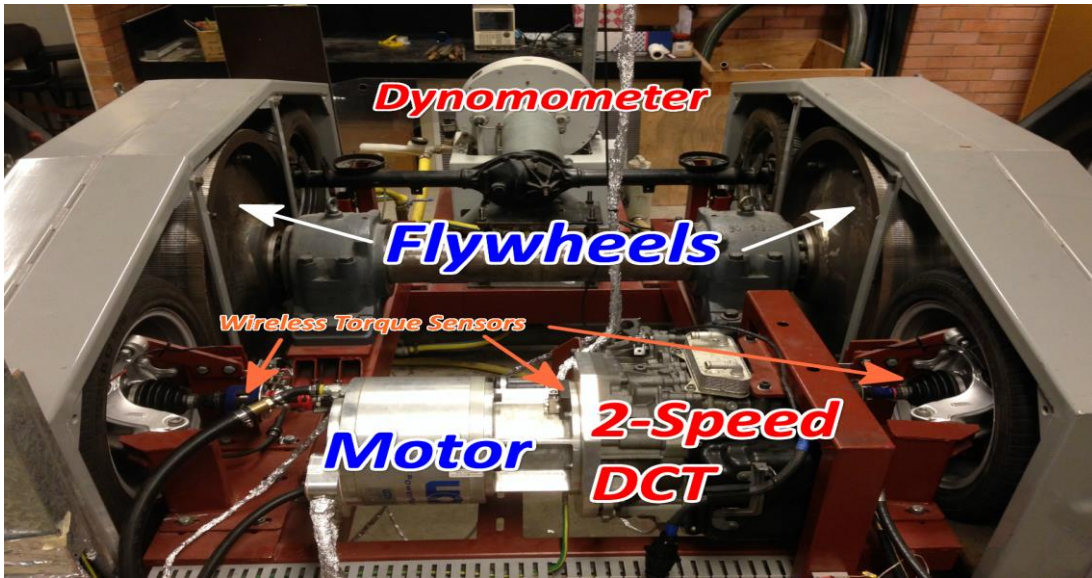
551 Comparing the strategies, in rows, safety risk is included to demonstrate a general evaluation of
 552 wheel locking possibility. ‘Safety (Motor Priority)’ is the baseline and has the highest avoidance
 553 of wheels lock. The highest energy recovery rate is achieved in ‘Eco’ because the required
 554 braking force rarely reaches the threshold of ECE R-13(H) regulation in all testing cycles, in other
 555 words, braking is supplied by the motor alone for most of the time. However, as more braking
 556 force is distributed to the front axle, the front wheels’ locking point will arise earlier. Safety-
 557 oriented Sports strategy results in much lower energy recovery rate, all under 4%, due to the
 558 fixed ratio of front friction and regenerative braking.

559 Summarizing the strategies’ performance, ‘Eco’ is the winner for energy recovery, although it
 560 has an earlier wheel lock threshold and higher risk of insufficient motor braking torque. ‘Sport’
 561 mode can keep the vehicle decelerating as demanded, no matter what the motor speed and
 562 gear number, or even a motor fault happens. However, the braking energy recovery rate is the
 563 lowest. ‘Safety (Motor Priority)’ has an excellent braking performance in terms of wheel locking,
 564 and at the same time, has a satisfactory energy recovery rate.

565 7. Experimental Results

566 The integrated powertrain-testing rig incorporates a BLDC motor and controller, a differential
 567 included two-speed DCT, wheels, flywheels and a dynamometer, as shown in Fig.18. The motor
 568 is a UNIQ UQM_PowerPhase125 with ratings as given in Table 1.A in the Appendix. The UNIQ
 569 UQM_PowerPhase125 motor controller is supplied by a custom-built 380 V DC supply, which is
 570 bidirectional, i.e. can supply or absorb power. A 380 V, 72 Ah battery bank is to be also installed
 571 [43]. Its energy capacity of 20 kWh can be considered typical of a BEV. The vehicle inertia is

572 supplied by four flywheels in the testing rig to simulate a 1500kg whole vehicle mass. This
 573 inertia stores kinetic energy in the flywheels, simulating a road vehicle driving at some linear
 574 speed. By using these flywheels the dynamic behavior of the vehicle can be simulated
 575 accurately in a controlled laboratory. Additional external resistance force, such as dynamic
 576 aerodynamic drag and roll resistances in the driving cycles, is generated by an eddy current
 577 dynamometer. HWFET and NEDC cycles are selected in this study to consist of a combined
 578 driving cycle to simulate consumers' daily driving conditions.



579

580

Figure 18: Vehicle powertrain testing rig

581 The maximum decelerations in different driving cycles are presented in Table 2. The highest
 582 deceleration, $2.2 \text{ m/s}^2 = 0.22g$ appearing in the LA-92 cycle, is far from the wheel-lock
 583 deceleration thresholds, represented by the two red dotted curves in Fig.6. Therefore, RBS can
 584 theoretically meet all the braking force requirements. Aiming at studying the energy recovery
 585 maximum potential and testing the motor braking safety performance, 'Eco' strategies are
 586 selected in these two cycles to be experimentally validated.

587

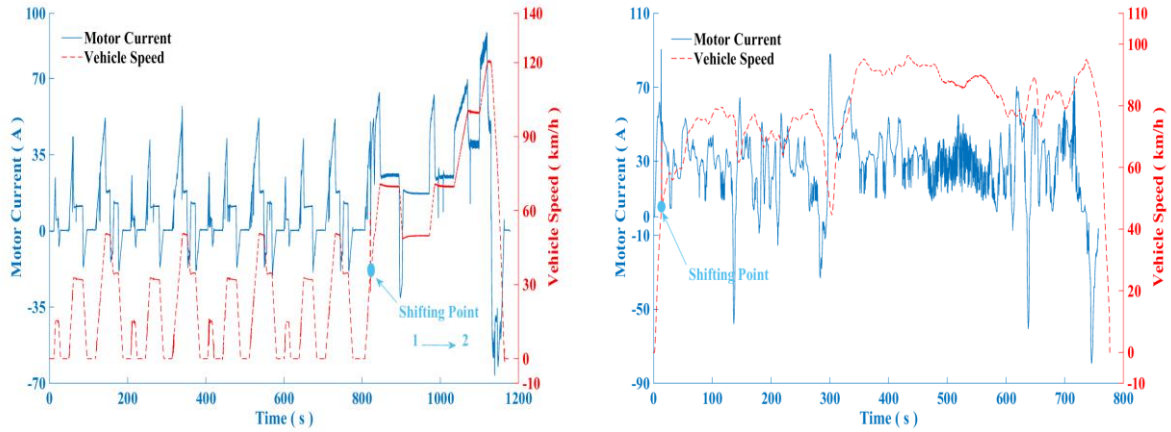
Table 2: Maximum deceleration in typical driving cycles

	NEDC	UDDS	JP-1015	HWFET	LA 92
Max Deceleration (g)	0.1	0.093	0.067	0.14	0.22

588 As shown in Fig.19, the vehicle can be decelerated and stopped as required by regenerative
 589 motor braking alone in both cycles. The negative current generated by the motor (acting as a
 590 generator) never exceeds 90 Amps. Therefore, according to the specifications of 72 Ah battery

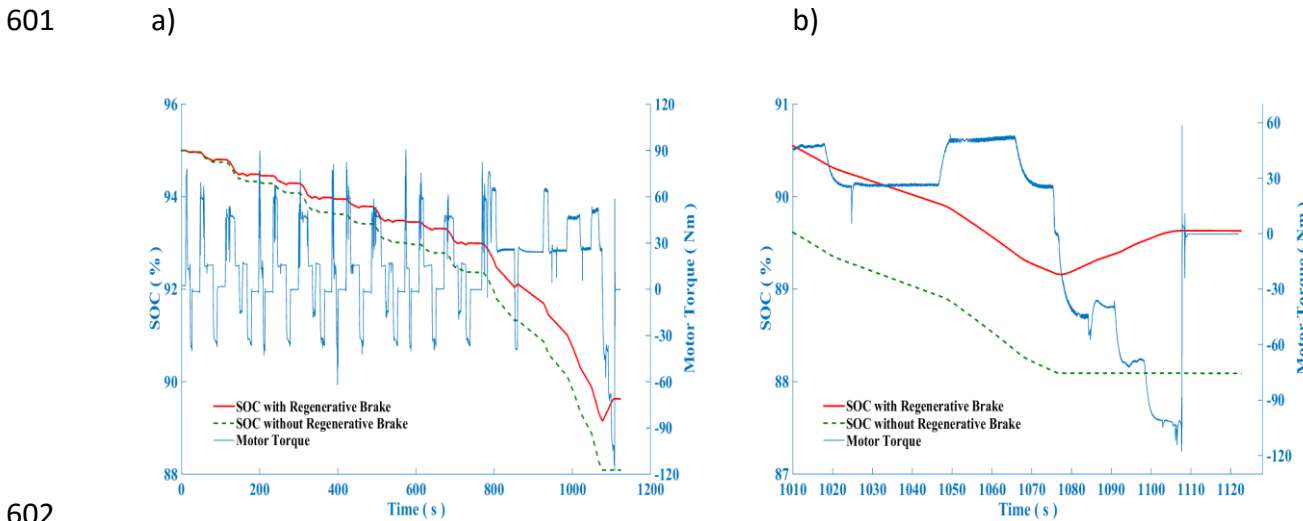
591 [43], which has maximum charging current more than 180 Amps, this charging current can be
 592 easily absorbed.

593 a) b)

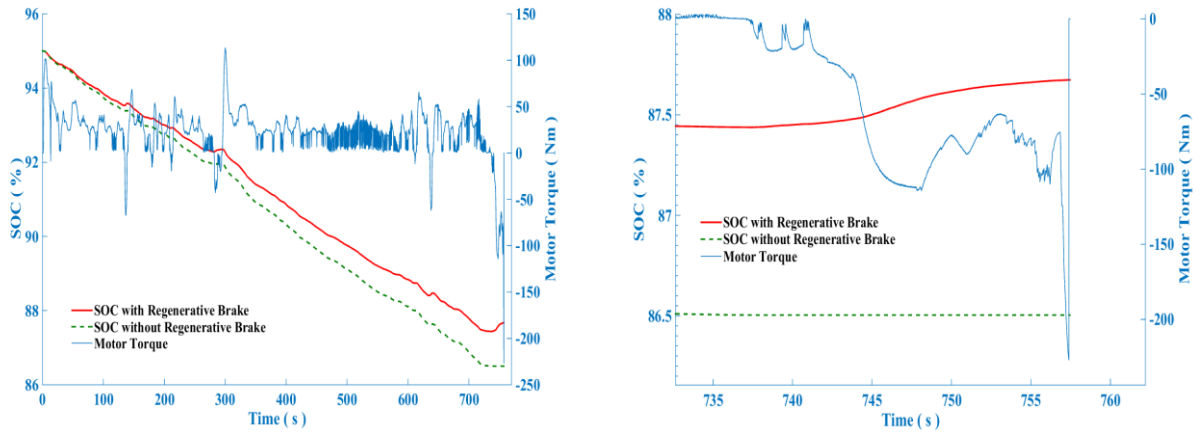


594
 595 Figure 19: Motor current and vehicle speed for 'Eco' mode in: a) NEDC and b) HWFET cycles

596 Fig.20 & Fig.21 compare the SOC for the powertrain with and without the regenerative braking
 597 in one NEDC or HWFET cycle. We can see that the motor has sufficient ability to meet the
 598 requirement of normal braking in daily use. Significant benefits, 23.3% and 14.1% energy
 599 recovery rates for NEDC and HWFET respectively, are achieved by inclusion of regenerative
 600 braking in the 'Eco' strategy experimental testing.



602
 603 Figure 20: SOC and motor torque in NEDC cycle for 'Eco' mode over: a) the full cycle; and b) the
 604 final 100 s



605
 606 Figure 21: SOC and motor torque in HWFET cycle for 'Eco' mode over: a) the full cycle; and b)
 607 the final 25 s

608 **8. Energy Recovery and Cost Saving Analysis**

609 **8.1 The cost saving in braking energy recovery**

610 According to the test results in Sec.7 and the battery specification in Table.1A (Appendix), the
 611 recaptured braking energy in one NEDC and HWFET cycle by 'Eco & Safety' strategy are
 612 calculated and shown in Table.3. The measured battery energy recovery rates were
 613 approximately 10% below the simulated rates given in Fig.1, which can be considered good
 614 agreement.

615 Table 3: Recovered braking energy and mileage per NEDC and HWFET cycle

	NEDC	HWFET
Mileage per cycle (MPC)	11.0 km	16.5 km
Consumed energy (with no regenerative braking)	1.888 kWh	2.326 kWh
Consumed energy per km (CPK)	0.1716 kWh/km	0.141 kWh/km
Recaptured energy in braking by 'Eco & Safety'	0.44 kWh	0.328 kWh
Recovered braking energy per km (RPK)	0.04 kWh/km	0.0199 kWh/km
Battery energy recovery rate Q_{re}	23.3%	14.1%

617 Daily driving conditions are mixed for commuters. A particular testing cycle may have a good
618 braking energy recovery rate but may not reflect the real performance correctly [44]. Therefore,
619 a combined driving cycle is special designed, according to the requirement of Environment
620 Protection Agency (EPA) of United States, to make the testing more authentic and reliable in this
621 study. The combined cycle combines the city and highway cycles, i.e. NEDC and HWFET, with
622 43% and 57% weightings for the distance spent in each cycle respectively [45] [ref]. The
623 reasonable consumed and recaptured braking energy per km of a combined driving, i.e.
624 $CPK_{Combined}$ and $RPK_{Combined}$, are shown in Eq.19 and Eq.20, comparing to 0.12 kWh/km in
625 an average cycle and ranging from 0.1 – 0.16 kWh/km for individual cycles [46].

$$CPK_{Combined} = \frac{1}{\frac{0.57}{CPK_{HWFET}} + \frac{0.43}{CPK_{NEDC}}} = \frac{1}{\frac{0.57}{141.0} + \frac{0.43}{171.6}} = 0.1527 \text{ kWh/km} \quad (19)$$

$$RPK_{Combined} = \frac{1}{\frac{0.57}{RPK_{HWFET}} + \frac{0.43}{RPK_{NEDC}}} = \frac{1}{\frac{0.57}{19.9} + \frac{0.43}{40}} = 0.0254 \text{ kWh/km} \quad (20)$$

626 The total mileage per charge for EV without regenerative braking is:

$$Range_{without_Regen} = \frac{C_B \times V_B}{CPK_{Combined}} = \frac{72 * 380}{152.7} = 179.2 \text{ km} \quad (21)$$

627 The total mileage per charge with regenerative braking is:

$$Range_{with_Regen} = \frac{C_B \times V_B}{CPK_{Combined} - RPK_{Combined}} = \frac{72 * 380}{152.7 - 25.4} = 215 \text{ km} \quad (22)$$

628 Therefore, the rate of extended mileage per charge with same battery for vehicle equipped with
629 regenerative braking is:

$$Extended_{MileageRate} = \frac{Range_{with_Regen} - Range_{without_Regen}}{Range_{without_Regen}} = 20.0\% \quad (23)$$

630 In term of battery capacity, the reduced requirement for the same travel distance, 188 km, is:

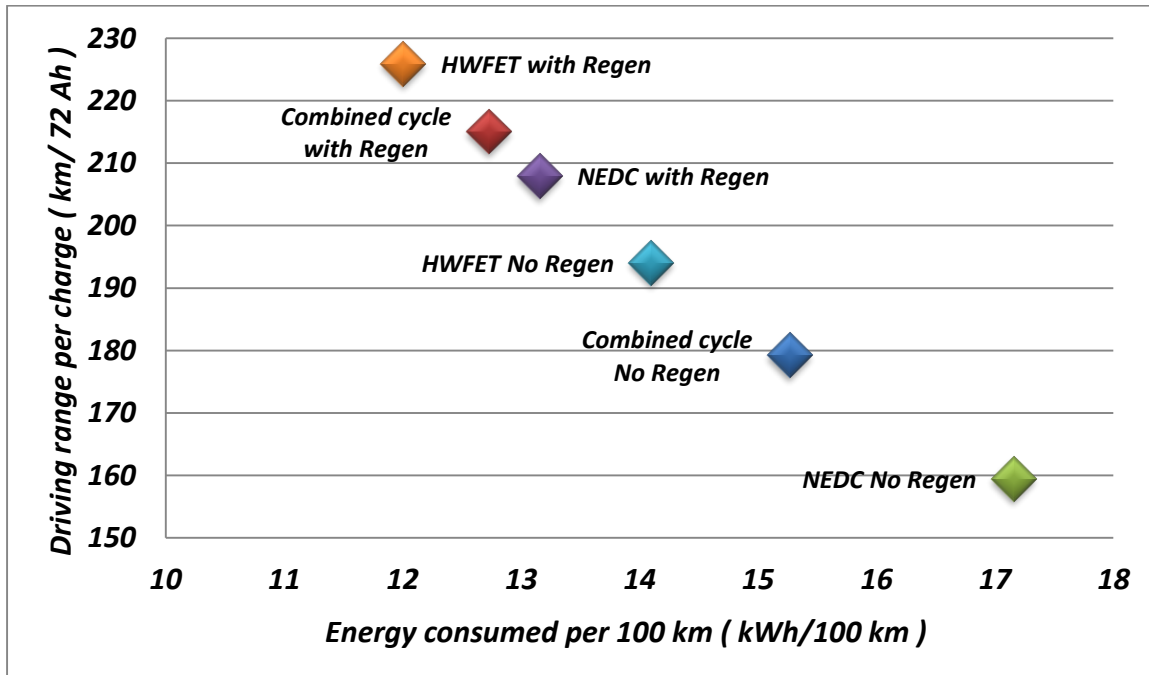
$$C_{reduced} = Range_{without_Regen} \times RPK_{Combined} = 188 \times 25.4 = 4.8 \text{ kWh} \quad (24)$$

631 The energy consumed per 100 km with and without regenerative braking respectively in
632 specification Table 1A are:

$$No \text{ Regen: } 152.7 \times 100 = 15.27 \text{ kWh} \quad (25)$$

$$\text{Regen: } (152.7 - 25.4) \times 100 = 12.73 \text{ kWh} \quad (26)$$

633 Fig.22 clearly demonstrates the braking energy recovery benefit, regarding to the driving range
 634 improvement and energy consuming minimizing. Top left three points, representing BEV with
 635 regenerative braking, have a longer driving range per charge and lower energy consuming rates
 636 (kWh/100 km), comparing to bottom right three points without energy recovering. Specific to
 637 cycles, highway cycle has the best performance, and city cycle consumes more energy. This
 638 graph also validates the effectiveness of representing two different kinds cycles for combined
 639 cycle.



640
 641 Figure 22: Driving range and energy utilization benefit of braking energy recovering

642 A typical passenger vehicle will travel a lifetime mileage of 250000 km according to [47] or
 643 208000 km according to the product of the typical annual average travel of 18240 km per year
 644 [48] times the typical 11.4 years average vehicle life [49]. Considering that the powertrain of an
 645 EV is more reliable and simpler than that of the traditional vehicle, having a more robust motor
 646 and no gearbox or a simple 2-3 speed gearbox, 250000 km lifetime mileage is taken in this
 647 paper. Additionally, the charging efficiency with Level 2 standard voltage is 81% [50], as a result
 648 of same 90% efficiency for both plug-in charger and lithium-ion battery charge/discharge [51].
 649 The total expected electricity energy saved by regenerative braking with 'Eco' strategy in the
 650 whole life cycle is:

$$E_{save} = \frac{RPK_{Combined} \times Range_{lifetime}}{Charging\ Eff} = \frac{0.0254 \times 250000}{0.81} = 7840 \text{ kWh} \quad (27)$$

651 Since the limited electricity energy in the battery can be replenished by regenerative braking,
 652 significant cost saving can be achieved by reducing the required capacity of this expensive
 653 power source. The prices given in Table 4 are based on data and results from laboratory and
 654 industry [52–55]:

655 Table 4: Manufacturing cost and retail price of EV basic parts

Vehicle component	Cost (US \$)
Battery manufacture	\$ 400/kWh
BMS, power electronics, etc.*	\$ 238/kWh
Battery pack final cost (incl. margin and warranty)	\$ 800/kWh
Average electricity cost (in Australia)	\$ 0.3/kWh

656 *This part includes battery management system (BMS), power electronics, connections, cell
 657 support, housing and temperature control. The estimated battery charge/discharge cycles in
 658 vehicle lifetime span with deep (80%) / shallow (45%) depth of discharge (DOD) are calculated
 659 in Eq.28 and Eq.29:

$$\text{Without Regen} \begin{cases} LifeCycle_{50\%DOD} = \frac{250000/100 \times 15.27}{72 \times 380/1000} \times \frac{1}{50\%} = 2791 \\ LifeCycle_{80\%DOD} = \frac{250000/100 \times 15.27}{40 \times 380/1000} \times \frac{1}{80\%} = 1744 \end{cases} \quad (28)$$

$$\text{With Regen} \begin{cases} LifeCycle_{50\%DOD} = \frac{250000/100 \times 12.73}{40 \times 380/1000} \times \frac{1}{50\%} = 2326 \\ LifeCycle_{80\%DOD} = \frac{250000/100 \times 12.73}{40 \times 380/1000} \times \frac{1}{80\%} = 1454 \end{cases} \quad (29)$$

660 The reduced charging/discharging cycles in different DOD by regenerative braking are:

$$\begin{cases} LifeCycleSave_{50\%DOD} = 2791 - 2326 = 465 \\ LifeCycleSave_{80\%DOD} = 1744 - 1454 = 290 \end{cases} \quad (30)$$

661 The lifetime cycles of a typical li-ion battery are 3200 and 18000 for deep and shallow DOD
 662 respectively at room temperature (25°C) [56]. However, the lifetime cycles are not only related

663 to DOD, also subjected to operating temperature and chemical materials. With the increasing
 664 working temperature, higher DOD and discharging rate, the life cycles declines to lower than
 665 1000 [57–59]. Additionally, considering the 5-8 years battery calendar year life span[57,60,61],
 666 it is inevitable for battery EV to replace the battery pack at least one time during the whole
 667 vehicle life. There is no doubt that regenerative braking can improve the battery life in terms of
 668 cycles/calendar year aging, however, the reduced charging/discharging cycles are not enough to
 669 save a whole battery pack.

670 In summary, the costs saving in electricity fee and battery pack by ‘Eco’ strategy are:

$$Electricity_{save} = 7840 \times 0.3 = 2352 \text{ (USD)} \quad (31)$$

$$BatteryPack_{save} = 800 \times 4.8 = 3840 \text{ (USD)} \quad (32)$$

671 **8.2 The cost saving in braking equipment maintenance**

672 Comparing to the mechanical parts in traditional vehicles, electrical components such as
 673 traction motors require little maintenance. The estimated overall maintenance costs for a BEV is
 674 approximately 70% of an equivalent ICE vehicle [62]. Specific to the RBS, the unique advantage
 675 is the durability and high-temperature resistance compared to friction braking system.
 676 Whatever the materials selected for brake disk and pad, wear and deformation are inevitable,
 677 and failure is a fatality risk. Motor electric braking eliminates all these potential risks by directly
 678 applying negative torque on rotating shafts.

679 Depending on the vehicle type, brake pad materials, driving routes and operating environment,
 680 the average pad life varies from 28400 km to 33800 km [63]. Considering the emergency
 681 braking produces more wear than usual, ten brake pad replacements for whole 250000 km
 682 vehicle life is regarded as a reasonable assumption in this paper.

683 The cost of brake pads and rotors, which are presented in the following table, can be obtained
 684 from quotes on the web [64,65]. The rotors can last 2-3 sets of pads before needing
 685 replacement. The share of friction braking and motor braking for ‘Sport’ and ‘Safety (Motor
 686 Priority)’ strategies are roughly 15/85 and 50/50, based on the Fig.16 and Eq.17, which are used
 687 to calculate the required brake pads/rotors and cost respectively. Additionally, one extra pair of
 688 brake pads are added to each blended braking strategy for emergency braking.

689 Table 5: Friction brake applications and pedal replacement cost (US \$)*

	Friction brake only	‘Eco’	‘Safety (Motor Priority)’	‘Sport’
Number of replaced pads	10	1	6	9

Pads cost with labor (8 sets, two axles, \$ USD)	\$ 350	\$ 350	\$ 350	\$ 350
Lifetime pads replacement cost	\$ 3500	\$ 350	\$ 2100	\$ 3150
Number of replaced rotors	4	0	2	3
Rotors cost with labor (4 sets, two axles)	\$ 210	\$ 210	\$ 210	\$ 210
Lifetime rotor replacement cost	\$ 840	0	\$ 420	\$ 630

690 *Average value is used based on the reference data

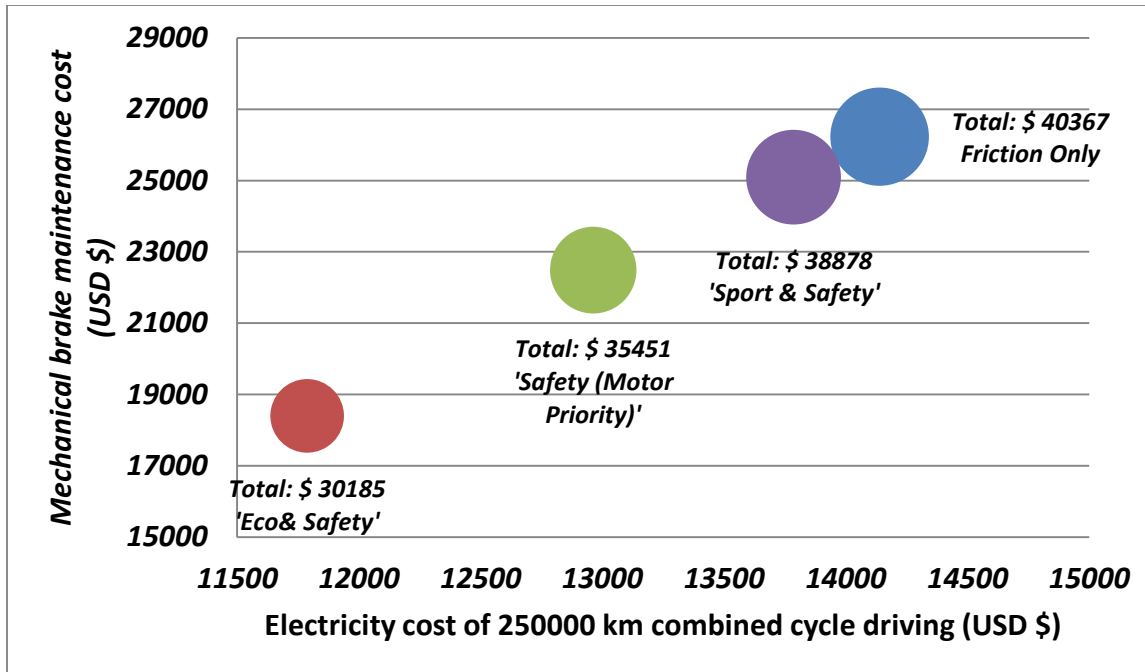
691 Finally, the total cost of BEVs based on different braking architectures and strategies are
692 demonstrated in Table.6:

693 Table 6: Blended braking system related EV lifetime cost saving summary (US \$)

	Friction Brake Only	'Eco'	'Safety (Motor Priority)'	'Sport'
Electricity Fee	\$ 14139	\$ 11787	\$ 12963 (Approx.)	\$ 13786 (Approx.)
Battery Pack	\$ 21888	\$ 18048	\$ 19968 (Approx.)	\$ 21312 (Approx.)
Brake Pads	\$ 3500	\$ 350	\$ 2100	\$ 3150
Brake Rotors	\$ 840	0	\$ 420	\$ 630
Total	\$ 40367	\$ 30185	\$ 35451	\$ 38878

694

695 The effectiveness of 'Eco & Safety' strategy is validated in both city and highway cycles in this
696 experiment, expect rare emergency braking. Therefore, the 'Eco & Safety' strategy' can be used
697 to evaluate the economic benefit of regenerative braking in daily commuting, comparing to
698 conventional friction braking. The economic benefit of different blended braking strategies is
699 shown in Fig.23, regarding to 'fuel' cost and mechanical maintenance cost. As shown in Fig.23,
700 more than one fourth of total cost, including brake system maintenance and electricity, can be
701 saved by braking energy recovering in 'Eco & Safety' strategy. The figures for 'Safety (Motor
702 Priority)' and 'Sport & Safety' are 12% and 4% respectively.



703

704 Figure 23: Maintenance and electricity cost of regenerative brake equipped BEV in 'Eco' strategy

705 **9. Summary**

706 This paper commenced by reporting the significant kinetic energy recovery potential in daily
 707 driving. The structure and advantage of front driven EV, especially for braking energy recovery,
 708 were discussed in detail. The factors which restrict blended braking were analyzed to determine
 709 the available regenerative braking from the motor, the ratio of motor and friction braking and
 710 the ratio of front and rear braking. Then, three blended braking strategies, 'Eco', 'Sport' and
 711 'Safety (Motor Priority)' with their characteristics, were proposed, the latter optimizing braking
 712 energy recovery and improving braking performance simultaneously. A 'motor fault insurance'
 713 strategy was developed to avoid any unexpected and fatal error in motor braking system.

714 Several braking testing maneuvers were used in this paper to test the possible safety issues,
 715 which may be caused by redistributing the braking force between the front/rear axles in a
 716 mechanical/regenerative braking system. The feasible solutions are analyzed and included in the
 717 specially designed algorithms. In a straight line braking test, the details of the braking force
 718 distribution between the front and rear wheels from the motor and hydraulic system are given
 719 in figures. Split Mu testing examined the influence on a blended braking strategy from load
 720 transfer, cornering and the road condition changing during emergency braking. A cooperation
 721 algorithm of RBS, EBD and ABS is proposed to provide safe, efficient blended braking. The
 722 possible braking torque interruption risk introduced by gear shifting is avoided by this specially
 723 designed strategy. The share of front/rear friction braking and motor regenerative braking in
 724 strategies for typical driving cycles were presented in charts. Consequently, the braking energy
 725 recovery rates for different driving cycles were calculated.

726 The performance of the 'Eco' blended braking strategy has been experimentally verified in
727 driving cycles by an integrated powertrain testing bench in the Lab. Thanks to the powerful
728 motor and relatively small required braking force, most of the braking events were covered by
729 motor regenerative braking alone in both city and highway cycles. In other words, the motor,
730 especially for BEV, has sufficient ability to meet the braking requirement in the daily use.
731 Specifically, 23.3% and 14.1% energy recovery rates, for NEDC and HWFET respectively, were
732 achieved by the powertrain with regenerative braking in 'Eco' mode in experimental testing.
733 These figures were approximately 10% below the calculated values, representing good
734 agreement between the simulation and the measurements.

735 Initial manufacture and daily-use cost savings by RBS were analyzed and compared to evaluate
736 the three strategies. The outcomes show that vehicle equipped with RBS can achieve a longer
737 driving range per charge, a lower 'fuel' cost and a lower battery pack price with same target
738 driving range, and lower maintenance cost. In term of vehicle lifetime, savings of approximately
739 US\$10k in 'Eco', US\$4-5k in 'Safety (Motor Priority)' and US\$1-2k in 'Sport' are expected
740 respectively, considering that friction braking is always required in all strategies for emergency
741 braking.

742 In summary, the three blended braking strategies not only improve braking performance,
743 enabling adaptive braking force control, shorter stopping distance when the load is changing,
744 and seamless transfer within RBS, EBD and ABS, but they also save customer's money.

745

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910

911 **Appendix**

912 The summaries of vehicle specifications in powertrain testing rig are presented in Table.1A:

913 Table 1A: Vehicle Specifications

Parameter	Description	Value	Units
m	Vehicle mass (incl. battery)	1500	kg
δm	Equivalent mass (Incl. Rotation part)	1.1m	kg
r	Tire radius	0.3125	m
i_g	Gear ratio	8.45/5.36	-
C_R	Coefficient of rolling resistance	0.016	-
h_g	Height of centre of mass	0.5	m
L	Length of wheelbase	2.675	m
L_a	Length of front axle centre of mass	1.2	m
L_b	Length of rear axle centre of mass	1.476	m
ϕ	Road incline	-	%
C_D	Aerodynamic Drag coefficient	0.28	-
A	Vehicle frontal area	2.2	m ²
u	Vehicle speed	-	m/s
T_{peak}/T_{rated}	Motor peak/rated output torque	300/150	Nm
P_{peak}/P_{rated}	Motor peak/rated output power	125/45	Kw
n_{peak}	Max speed of peak torque	2500	rpm
n_{max}	Max motor speed	8000	rpm
V_{bat}	Battery voltage	380	V

C_{bat}	Battery capacity	40	Ah
E_{bat}	Battery energy content	27.4	kWh

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928 **Definitions/Abbreviations**

BEV	Battery Electric Vehicle
DCT	Dual Clutch Transmission
AT	Automatic Transmission
AMT	Automated Manual Transmission
CVT	Continuously Variable Transmission
VCU	Vehicle Control Unit
ABS	Anti-Lock Brake System
EBD	Electro Control Brake Distribution
RBS	Regenerative Brake System
SOC	State of Charge
MPC	Mileage per cycle
CPK	Consumed energy per km
RPK	Recovered braking energy per km

929