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Design and Analysis of a Claw Pole Permanent Magnet Motor with Molded Soft Magnetic Composite Core

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SMC (Soft magnetic composite) materials and SMC electromagnetic devices have undergone substantial development in the past decade. Much work has been conducted on designing and prototyping various types of electrical machine. However, the iron cores were often made by cutting existing SMC preforms which were formed by compacting SMC powder in simple cylinder or bar shape molds, and the magnetic properties of the cores may deteriorate significantly during the cutting process. To investigate "industry production ready" products, this paper presents the design and analysis of a claw pole permanent magnet (PM) motor with a molded SMC core of low mass density to replace the existing induction motor in a dishwasher pump. The magnetic properties of the molded SMC core are measured and utilized in the motor design and analysis. Finite element analysis of magnetic field is carried out to accurately determine key motor parameters, and an improved phase variable model is applied to predict the motor performance. Both parameter computation and performance prediction are validated by the experimental results on the prototype.

*Index Terms***— Soft magnetic composite (SMC); molded SMC core; claw pole permanent magnet motor; finite element analysis of magnetic field; improved phase variable model.**

I. INTRODUCTION

ECAUSE OF the many unique properties such as magnetic \mathbf{B} ECAUSE OF the many unique properties such as magnetic isotropy, very low eddy current, great design flexibility and great potential for low cost mass production, soft magnetic composite (SMC) materials and their application in electromagnetic devices have undergone significant development in the past decade [1]. A large amount of research has been conducted by various researchers on designing and prototyping various types of electrical machines [2]-[6] using SMC material. Notable examples include claw pole and transverse flux motors featuring complex structures and 3-D flux paths [7], where it is difficult to use laminated steels so that SMC seems to be an ideal substitute.

However, most of the SMC motor prototypes investigated used iron cores cut from existing preforms which were previously compacted with high pressure in a simple shape mold such as cylinder and bar. The wire-cutting technique may be convenient and cost-effective for fabricating laboratory prototypes but would not be appropriate for commercial productions due to the large cost of a single processing. Also, the cutting process may significantly reduce the magnetic and mechanical properties of the SMC core.

In commercial production, the manufacturing cost of the SMC motor can be dramatically reduced if a high-productivity low-pressure press is used in the molding. On the other hand, the magnetic properties of the SMC core and hence the motor performance depends greatly on the mass density of the core. To investigate "industry production ready" products, the authors have recently developed techniques for the design and prototyping of permanent magnet (PM) motors with low density molded SMC cores. As an example, this paper presents the development of a claw pole PM SMC motor for replacing an existing single phase induction motor in a dish washer pump. A mold for pressing SMC claw pole disk was designed and made. SMC cores were compacted with different pressures and the corresponding magnetic properties were measured and applied in the design and analysis of the motor. The SMC motor is designed within the envelop of the original induction motor and produces the same output.

To accurately determine the magnetic field distribution and key parameters of the claw pole motor, 3-D magnetic field finite element analysis (FEA) was carried. To effectively predict the dynamic and steady-state performance, an improved phase variable model was adopted. The motor prototype has been fabricated and tested, validating the parameter computation and performance analysis.

II. SMC CORE AND PROTOTYPE MOTOR

Fig. 1 shows the SMC claw pole disk compacted in a mold with a single step press (no further machining required), and Fig. 2 the assembled 3 phase stator core. Each phase consists of two disks with a concentrated global coil in between, and the stator is formed by stacking three phases axially with a circumferential shift of 120° electrical from each other. The major structural parameters include: stator inner diameter of 43 mm, stator outer diameter of 67 mm, effective axial length of 55 mm, and air-gap of 1 mm. 12 NdFeB magnets with dimensions of 55 x 6.7 x 3 mm³ are mounted on the surface of a mild steel rotor. The motor is designed to operate at 3000 rpm, delivering a power of 60 W.

The stator core disks were compacted in a mold with a pressure of 20 ton force (about 179 MPa) or 100 ton force (895 MPa), which is slightly higher than 800 MPa, the nominal pressure for the SMC material [1]. The average mass densities are 5.8 g/cm³ and 7.2 g/cm³, respectively. As shown in Fig. 3, the measured B-H curve of the 5.8 $g/cm³$ core is much lower than that of the 7.2 $g/cm³$ core. On the other hand, the low density cores can be compacted by small pressure, which yields much higher productivity than large ones. This can be attractive for industry applications. In this paper, the molded SMC core of 5.8 $g/cm³$ is employed.

Fig. 1. Molded SMC claw pole disk

Fig. 2. Molded stator of a 3-phase claw pole motor

III. FINITE ELEMENT ANALYSIS OF MAGNETIC FIELD AND COMPUTATION OF MOTOR PARAMETERS

Due to the complex structure and 3-D magnetic flux path of the claw pole motor, numerical analysis of magnetic field by for example finite element method is necessary to accurately determine the magnetic field distribution and major parameters. By ignoring the magnetic coupling between stacks and considering the structural symmetry, only a pole region of one stack is needed for the field analysis. On the two radial boundary surfaces, the scalar magnetic potentials should obey the following half-periodical boundary conditions:

$$
\varphi_m(r,\theta,z) = -\varphi_m(r,\theta + \Delta\theta,-z) \tag{1}
$$

where $\Delta\theta = 30^\circ$ is the angle of one pole pitch, and the origin is located in the centre of the stack.

Fig. 4 illustrates the magnetic flux density vector plot at no-load at $\theta = 0^\circ$, where the claw poles face rotor magnets. It can be seen that the magnetic flux flows along 3-D path and a substantial flux leakage exists. From the no-load magnetic field distribution, a number of major motor parameters can be determined. For example, Fig. 5 plots the computed flux linking a phase winding, produced by the rotor PMs, against rotor position. The back electromotive force (EMF) can be easily obtained by differentiating the flux waveform with respect to rotor position or time. The cogging torque curve can also be obtained by using the virtual work method or the Maxwell stress tensor method using the field distribution.

Fig. 4. Flux density vector plot at no-load

Fig. 5. Per-turn flux of a phase winding produced by rotor PMs

Unlike conventional machines, claw pole SMC motors usually have largely variable inductance and core loss when the rotor rotates. These variations can be easily obtained by using the time-stepping finite element analysis (FEA). Fig. 6 plots the inductance of a phase winding by using a modified incremental energy method [8].

Fig. 7 shows the transient core loss which was obtained using the following three-term formulation [9]:

$$
P_{j\hat{e}} = \left\{ \sum_{j=x}^{z} |H_j \frac{dB_j}{dt} | \frac{\partial}{\partial t} \right\}^{\frac{\beta}{2}} + \frac{k_c}{2\pi^2} \sum_{j=x}^{z} \left(\frac{dB_j}{dt} \right)^2 + \frac{k_e}{C_e} \left\{ \sum_{j=x}^{z} \left(\frac{dB_j}{dt} \right)^2 \right\}^{\frac{3}{4}} \tag{2}
$$

where the coefficients β , k_c , k_e and C_e are obtained by curve fitting the results from the measurements on the SMC sample. The calculation uses each element (for which the flux density and field strength are obtained) in the time-stepping FEA solutions.

IV. IMPROVED PHASE VARIABLE MODEL AND MOTOR PERFORMANCE PREDICTION

An improved phase variable model [10] is applied to analyze the performance of the motor driven by a sensorless brushless DC (BLDC) controller [11], which can produce a reasonably sinusoidal phase voltage waveform to match that of the motor back-EMF. The phase variable model consists of a few electrical and mechanical equations as the following, where L_{jk} is the apparent inductance which is independent of the stator currents, and L'_{ik} the incremental inductance. All other parameters are used as their conventional meaning.

$$
v_j = r_j \dot{i}_j + \frac{d\lambda_j}{dt} + e_j \ \lambda_j = \sum_{k=a}^{c} L_{jk} \dot{i}_k , \ j = a, b, c \tag{3}
$$

$$
\frac{d\lambda_j}{dt} = \sum_{k=a}^{c} \frac{\partial \lambda_j}{\partial i_k} \frac{di_k}{dt} + \frac{\partial \lambda_j}{\partial \theta_r} \frac{d\theta_r}{dt} = \sum_{k=a}^{c} (L'_{jk} \frac{di_k}{dt} + \frac{dL_{jk}}{d\theta_r} i_k \omega_r) \tag{4}
$$

$$
T_{em} = \left(\sum_{j=a}^{c} e_j i_j\right) / \omega_r + T_{cog} \tag{5}
$$

$$
J\frac{d\omega_r}{dt} = T_{em} - \frac{P_{fe}}{\omega_r} - T_L - \delta\omega_r, \ \frac{d\theta_r}{dt} = \omega_r \tag{6}
$$

$$
r_j = r_k, L_{jk} = L_{kj}, \sum_{j=a}^{c} i_j = 0, (j, k=a, b, c)
$$
 (7)

In BLDC operation, one of the 3 phase windings is not excited and the voltage of the phase is not measurable, so the equations based model cannot be applied directly and an alternative model, consisting of several circuit components, has to be used [12]. To estimate the voltage (potential) of the neutral point and then the voltage of the non-excited phase winding, the following equation is used in this paper.

$$
U_a = U_N + \sum_{j=a}^{c} L'_{ja} \frac{di_a}{dt} + e_a + \sum_{k=b}^{c} \left(L'_{ak} \frac{di_k}{dt} + \frac{dL_{ak}}{d\theta_r} i_k \omega_r \right)
$$
 (8)

The improved phase variable model can simulate the motor performance must faster than the FEA but with the same level of accuracy. The rotor position dependence of key motor parameters, i.e., the waveforms of the winding flux, back-EMF, winding inductance, core loss and cogging torque against rotor angle or time are all obtained in advance using a series of time-stepping magnetic field FEA solutions and stored in lookup table for retrieval for performance simulation.

Using the above equations, a model was developed in Simulink, which can simulate both the steady-state and dynamic performances of the motor. For example, Fig. 8(a) illustrates the simulated speed curve from start-up, showing that the motor can accelerate smoothly to the rated speed of 3000 rpm with the rated torque of 0.2 Nm, while Fig. 8(b) shows the simulated steady-state electromagnetic torque ripple, which is caused by cogging torque, transient core-loss torque and phase-current switching. Fig. 9 plots the simulated applied voltage and current of one phase.

Fig. 8. Predicted motor performance: (a) speed curve during start-up; (b) steady-state electromagnetic torque curve

V. EXPERIMENTAL VALIDATION

The motor parameter computation has been verified by the measurement. For example, the back-EMF waveform (open circuit voltage) was recorded on a CRO when the rotor was rotated. It was approximately sinusoidal in waveform and the peak-to-peak EMF was 46.5 V at 39.7 Hz, therefore it can be deduced that the per-turn flux of stator winding produced by the rotor PMs is 0.364 mWb, which is very close to the calculation. With the voltage-current method, the equivalent phase winding inductance was measured as 50.9 mH, which is close to the average value of 54.0 mH in Fig. 6. The mutual inductance is measured as only about 5% the self inductance.

Fig. 10 illustrates the experimental setup for measuring the motor performance. The SMC motor prototype is on the right and a dynamo load cell is on the left. A torque transducer is mounted between the motor and the load for measuring the shaft torque and speed. Fig. 11 plots the measured mechanical characteristics, i.e. the motor speed against applied DC link voltage of the inverter with certain load. The motor can successfully deliver a torque of 0.2 Nm at 3000 rpm while the inverter is supplied with a DC link voltage of about 290 V.

Fig. 10. Experimental setup

VI. CONCLUSION AND DISCUSSION

This paper presents the design and analysis of a claw pole PM motor with molded SMC core. The core was compacted at a low pressure of 179 MPa and hence has a low mass density of 5.8 $g/cm³$, which has great benefit for molding. If the motor were made with a high density SMC core of 7.2 g/cm^3 , FEA results show that the back-EMF would increase by 18%. In other words, the lower density SMC motor should have a larger volume core for the same output; this is not a difficulty for our design for replacing an existing induction motor.

Furthermore, the inductance of high density SMC is calculated as 20% lower. This means that the low density SMC motor must operate with a higher V-A rating inverter. For this 60 W motor application, we used 320 VDC as in Fig. 11.

ACKNOWLEDGMENT

This work was supported in part by the Australian Research Council under Linkage Project Grant No. LP0454306.

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