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Model Predictive Control for Single-Phase NPC Converters Based on Optimal Switching Sequences

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Abstract—In this paper, a model predictive control (MPC) based on optimal switching sequences (OSSs) for a single-phase grid-connected full-bridge neutral-point-clamped (NPC) power converter is presented. The predictive control algorithm is formulated in terms of OSSs, which was originally proposed to govern three-phase power converters. In this work, the OSS concept is extended to control single-phase power converters. The proposed MPC algorithm belongs to the continuous control set MPC (CCS-MPC) and is able to provide fixed switching frequency while handling system constraints. The proposed algorithm has been experimentally tested in an NPC power converter prototype. Experimental results show the desired fixed switching behavior in the steady state condition and the intrinsic fast dynamic provided by MPC during transients. Furthermore, the test outcomes demonstrate the robustness of the proposed controller under large system parameter deviations.

I. INTRODUCTION

POWER converters play a key role in applications such as integration of renewable energies, energy storage systems, motor drives, etc [1]–[3]. In particular, single-phase power converters have drawn much attention for low-power photovoltaic (PV) integration and railway traction systems [4]–[6]. For this reason, controller design for single-phase grid connected power converters has an increasing practical value.

The conventional solution to control the input current of power converters is based on linear proportional-integral (PI) regulators working in a synchronous reference frame or proportional plus resonant controllers [7]–[9]. In general, these solutions offer good performance. However, it has been shown that nonlinear control strategies can improve transient and steady state behavior compared with these conventional approaches [10], [11]. One promising alternative to govern power converters is model predictive control (MPC) [12], [13]. In essence, to implement an MPC strategy, it is firstly required to select a cost function to define a desired control objective. Then, a model of the system is used to forecast its future behavior. Finally, the optimal control action to be applied to the system is the one that minimizes the cost function. This process is repeated at each sampling instant using a receding horizon policy [14]. MPC for power converters can be divided in two major groups depending on the nature of the chosen control input [15]: Finite control set MPC (FCS-MPC) [16] and continuous control set MPC (CCS-MPC) [17].

FCS-MPC takes advantage of the discrete nature of the power converter. In this way, it only calculates the cost function value for the available output voltage vectors of the power converter. For instance, in the case of a conventional single-phase H-bridge inverter, only four voltage vectors are evaluated. The main advantage of this approach is that the cost function can manage a multi-objective optimization problem and handle system constraints with ease. The main disadvantage of this strategy for controlling grid-connected converters is that it does not provide a constant switching frequency. As a consequence, it is more difficult to design the grid filter. Some alternatives have been presented to solve this problem [18]–[21]. However, this is still an open issue for FCS-MPC.

On the other hand, CCS-MPC considers the control region of the power converter as a continuous space. Therefore, it solves the optimization problem and provides a control action that should be generated by means of a modulator. The main advantage is that it provides a fixed switching frequency. Therefore, this MPC class fits particularly well to control grid-connected power converters. The main problem is that handling system constraints usually requires to solve an optimization quadratic problem. This is highly computational demanding and very difficult to solve online using a conventional digital hardware platform. For this reason, these techniques are usually limited to solve problems without including system constraints [22]–[24].

This paper presents an MPC algorithm, which belongs to the CCS-MPC family, to govern single-phase grid-connected full-bridge neutral-point-clamped (NPC) power converters. The
proposed method is based on using the optimal switching sequence (OSS) concept to calculate the control action [25]. The main advantage of this approach is that it can handle system constraints while keeping a limited computational burden, hence enabling the implementation of the proposed control algorithm in a standard digital hardware platform. To be more specific, the proposed algorithm evaluates the cost function for each of the available switching sequences for the power converter. Then, like in an FCS-MPC strategy, the one that minimizes the cost function becomes the OSS to be applied in the power converter.

In essence, OSS defines a switching sequence (switching states and corresponding duty cycles) to be applied in the power converter during the next sampling period. The switching sequence in three-phase systems is conventionally calculated implementing a space vector based modulation method. However, in single-phase converters, the usual way to obtain the power switch gate signals is to use a conventional sinusoidal PWM. Since PWM does not relay on the vectorial representation of switching states, a straightforward implementation of the OSS technique by taking into account PWM is not possible. Therefore, a suitable vectorial representation of switching states for single-phase power converters has to be considered first in order to design an OSS-based control algorithm.

In this paper, the basic ideas for developing an OSS-based MPC (OSS-MPC) algorithm for single-phase power converters, focused on the current control tracking, are presented. The proposed OSS-MPC is able to track a reference current, which regulates the transference of power between dc-sources connected to the dc-link and the grid. The proposed algorithm can easily be extended to other configurations but, for the sake of clarity, only the basic concepts are presented using the aforementioned circuit.

The remainder of the paper is organized as follows. Section II shows the model of the grid-connected full-bridge NPC power converter. Section III presents the design of the proposed OSS-MPC strategy. Section IV discusses the selection of a suitable set of switching sequences for the single-phase NPC converter. Section V shows experimental results to validate the proposed control algorithm and finally the main conclusions are summarized in Section VI.

II. MODEL OF THE SYSTEM

The circuit diagram of a single-phase grid-connected full-bridge NPC power converter is depicted in Fig. 1. Here, \( S_{xi} \) and \( S_{ab} \) are the MOSFET switches, \( L \) is the output filter inductor, \( r \) is the output filter resistor, and \( V_d \) is the DC-Link voltage. The input grid voltage \( v_s \) is connected to the dc-link and the grid. The proposed algorithm evaluates the cost function for each of the available switching sequences for single-phase power converters has to be considered first in order to design an OSS-based control algorithm.

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![Circuit diagram of a grid-connected single-phase NPC converter.](image)

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### Table I: System Variables and Parameters

<table>
<thead>
<tr>
<th>Variable</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>( v_s )</td>
<td>Grid voltage</td>
</tr>
<tr>
<td>( i_s )</td>
<td>Grid current</td>
</tr>
<tr>
<td>( v_{ab} )</td>
<td>Inverter output voltage</td>
</tr>
<tr>
<td>( r )</td>
<td>Output filter resistor</td>
</tr>
<tr>
<td>( L )</td>
<td>Output filter inductor</td>
</tr>
<tr>
<td>( V_d )</td>
<td>DC-Link voltage</td>
</tr>
</tbody>
</table>

### Table II: Voltage Vectors for the Single-Phase NPC Converter

<table>
<thead>
<tr>
<th>Vector ( j )</th>
<th>((S_a, S_b))</th>
<th>(v_{abj})</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>((-1, -1))</td>
<td>0</td>
</tr>
<tr>
<td>1</td>
<td>((0, -1))</td>
<td>(V_d/2)</td>
</tr>
<tr>
<td>2</td>
<td>((1, -1))</td>
<td>(V_d)</td>
</tr>
<tr>
<td>3</td>
<td>((-1, 0))</td>
<td>(-V_d/2)</td>
</tr>
<tr>
<td>4</td>
<td>((0, 0))</td>
<td>0</td>
</tr>
<tr>
<td>5</td>
<td>((1, 0))</td>
<td>(V_d/2)</td>
</tr>
<tr>
<td>6</td>
<td>((-1, 1))</td>
<td>(-V_d)</td>
</tr>
<tr>
<td>7</td>
<td>((0, 1))</td>
<td>(-V_d/2)</td>
</tr>
<tr>
<td>8</td>
<td>((1, 1))</td>
<td>0</td>
</tr>
</tbody>
</table>

for all \( i \in \{1, \ldots, 4\} \) and \( x \in a, b \) denotes the, so-called, switching signal to trigger each power switch. Therefore, each of them can take only two values, i.e., \( S_{xi} \in \{0, 1\} \). Moreover, the pairs of switching signals \( S_{x1}, S_{x3} \) and \( S_{x2}, S_{x4} \) work in a complementary way. The variables of the system are shown in Table I. To introduce the concept of OSS, it is assumed that the dc-link voltages are supplied by using external dc sources.

Under this condition, the continuous-time dynamic of the grid current can be described by:

\[
v_s = L \frac{di_s}{dt} + r i_s + v_{ab}, \tag{1}
\]

where the voltage between the output terminals of the power converter is:

\[
v_{ab} = \frac{V_d}{2} (S_{a1} - S_{b1} + S_{a2} - S_{b2}). \tag{2}
\]

Due to the discrete nature of the NPC converter, the output voltage \( v_{ab} \) belongs to the following finite control set:

\[
v_{ab} \in \mathbb{V}_{ab} = \left\{-V_d, -\frac{V_d}{2}, 0, \frac{V_d}{2}, V_d\right\}. \tag{3}
\]
These voltage levels can be generated by redefining (2) as:
\[ v_{ab} = \frac{V_{dc}}{2} (S_a - S_b), \]
with \( S_a \) and \( S_b \) representing the switching functions for the legs \( a \) and \( b \), respectively. Thus, each element of the pair \((S_a, S_b)\), which can individually take only three values, defines the available finite control sets for the single-phase full-bridge NPC converter as:
\[ S_a \in \{-1, 0, 1\}, \]
\[ S_b \in \{-1, 0, 1\}. \]

Table II summarizes the nine output voltages that can be generated using the corresponding voltage vectors \( v_{abj} \) with \( j \in \{0 \cdots 8\} \).

### III. Optimal Switching Sequence Strategy

To design the proposed OSS-MPC strategy for the single-phase full-bridge NPC converter, (1) can be rewritten as:
\[ \frac{di_s}{dt} = \frac{1}{L} (v_s - ri_s - v_{ab}), \]
which represents the variation of the grid current in a switching interval for a given converter output voltage \( v_{ab} \). Therefore, for each \( v_{ab} \in \mathbb{V}_{ab} \), it is possible to define a function that describes the variation of the grid current, \( i_s \), as:
\[ f_i (v_{ab}) = \frac{di_s}{dt} \bigg|_{v_{ab} = v_{abj}} \quad \forall j \in \{0 \cdots 8\}. \]  
(8)

Consider a switching sequence
\[ Seq_m = \{v_{abj,1}, v_{abk,2}, v_{abl,3}\} \]
with \( j, k, l \in \{0 \cdots 8\} \) and \( m \in \mathbb{N} \). The output voltages \( v_{abj,1}, v_{abk,2}, \) and \( v_{abl,3} \) are applied sequentially during the time intervals \( t_1, t_2 \) and \( t_3 \), respectively, where
\[ t_1 + t_2 + t_3 = T_s, \]  
(10)
in which \( T_s \) stands for the sampling period. The time set, \( T_{Seq_m} \), corresponding with \( Seq_m \) can be defined as \( T_{Seq_m} = \{t_1, t_2, t_3\} \). Then, the sequence \( Seq_m \) has associated the set
\[ F_{i_s} \bigg|_{Seq_m} = \{f_{i_1,1}, f_{i_2,2}, f_{i_3,3}\}, \]  
(11)
calculated from applying \( Seq_m \) to (8). With these values, and assuming that the sampling frequency is high enough, then the measured values of \( i_{s,k} \) and \( v_{s,k} \) at each sampling instant \( k \) are assumed to remain constant during the interval \( T_s \). Therefore, from (7) and (8), a prediction for the grid current at the end of the sampling period can be computed as:
\[ \hat{i}_{s,k+1} \bigg|_{Seq_m} = i_{s,k} + \sum_{n=1}^{n=3} f_{i_n} t_n, \]  
(12)
where \( \hat{i}_{s,k+1} \) and \( i_{s,k} \) stand for the predicted and actual current at instants \( k+1 \) and \( k \), respectively. An illustrative example of the proposed concept showing the evolution of the predicted current trajectories from the beginning to the end of a sampling period is shown in Fig. 2.

![Fig. 2. Predicted current trajectories (\( i_{s,1}, i_{s,2} \) and \( i_{s,3} \)) for a switching sequence of three vectors.](image)

### A. Cost Function Formulation

The proposed OSS-MPC can be designed using (12). For this purpose, the current error at the instant \( k + 1 \) is defined as
\[ e_{i,k+1} = i_{s,k+1}^* - \hat{i}_{s,k+1}, \]  
(13)
i_{s,k+1}^* being the current reference. Substituting (12) in (13) yields
\[ e_{i,k+1} = e_i0 - \sum_{n=1}^{n=3} f_{i_n} t_n, \]  
(14)
where \( e_i0 = i_{s,k+1}^* - i_{s,k} \). Taking into account (10), the expression for the current error of each sequence \( Seq_m \) becomes
\[ e_{i,k+1} = e_i0 - ((f_{i_1} - f_{i_2}) t_1 + (f_{i_2} - f_{i_3}) t_2 + f_{i_3} T_s). \]  
(15)

A simple cost function considering the quadratic current error is adopted as
\[ J = e_i^2 \big|_{k+1}. \]  
(16)
Other cost functions can be considered. For instance, if only one dc voltage source is employed and the converter handles the dc-link capacitor balancing problem, then the cost function
\[ J = e_i^2 \big|_{k+1} + \lambda e_{\Delta v_{dc}} \big|_{k+1} \]  
(17)
could be used, where \( e_{\Delta v_{dc}} \big|_{k+1} \) stands for the dc-link capacitor voltages difference error at instant \( k + 1 \) and \( \lambda \) is a weighting factor. However, to introduce the concept of the proposed control strategy, in this work \( J \) is chosen as defined in (16) to be as simple as possible for the sake of clarity. This cost function allows one to track a desired current reference while the dc-link capacitor voltage balance problem can be solved by using a voltage vector redundancy approach [11], [26].

The time values \( T_{Seq_m} = \{t_1, t_2, t_3\} \) that minimize the cost function \( J \) using the voltage sequence \( Seq_m = \{v_{abj,1}, v_{abk,2}, v_{abl,3}\} \) can be calculated solving the system
\[ \frac{\partial J}{\partial t_1} \bigg|_{Seq_m} = 0, \]  
(18)
\[ \frac{\partial J}{\partial t_2} \bigg|_{Seq_m} = 0. \]  
(19)

Once \( T_{Seq_m} \) is calculated, it is possible to determine the cost value, \( J_m \), when a particular sequence \( Seq_m \) is evaluated,
\[ J_m = J \bigg|_{Seq_m}. \]  
(20)
As each sequence $Seq_m$ provides a different cost value, $J_m$, then an FCS-MPC fashion approach can be used to obtain the optimal global solution. In this way, the OSS, $Seq_{\text{opt}}$, is thus defined as

$Seq_{\text{opt}} = \left\{ v_{abl,1}, v_{abl,2}, v_{abl,3} \right\}_{\text{opt}}, \quad (21)$

which is the one that minimizes $J$, i.e.,

$Seq_{\text{opt}} = \arg \min_{Seq_m} J, \quad (22)$

with the associated optimal time set, $T_{\text{opt}}$, which has the form

$T_{\text{opt}} = \{ t_1, t_2, t_3 \}_{\text{opt}}. \quad (23)$

**B. Handling System Constraints**

Assuming that the maximum current the power switches in the converter can stand is $I_{\text{max}}$, then, the cost function (16) is modified to account for this system constraint as follows:

$J' = J + J_{\text{max}}, \quad (24)$

where $J_{\text{max}}$ is defined as

$J_{\text{max}} = \begin{cases} 0 & \text{if } \hat{i}_{s,k+1} \leq I_{\text{max}} \\ \infty & \text{if } \hat{i}_{s,k+1} > I_{\text{max}}. \end{cases}$

It should be noticed that

$\frac{\partial J'}{\partial t_1}_{Seq_m} = \frac{\partial J}{\partial t_1}_{Seq_m}, \quad (25)$

$\frac{\partial J'}{\partial t_2}_{Seq_m} = \frac{\partial J}{\partial t_2}_{Seq_m}. \quad (26)$

Therefore, the time set $T_{Seq_m}$ calculated from (18) and (19) is the same that minimizes $J'$. Once $T_{Seq_m}$ is calculated, the value of $J'$ can be evaluated. Thus, for a given sequence $Seq_m$ the cost function value $J'_m$ is

$J'_m = J'_{Seq_m}, \quad (27)$

and the optimization problem to be solved is transformed to

$Seq_{\text{opt}} = \arg \min_{Seq_m} J', \quad (28)$

with the associated optimal time set, $T_{\text{opt}}$.

**IV. Switching Sequence Definition**

The problem solved in (28) requires a suitable set of switching sequences to be evaluated in order to find the optimal one. Defining this set can be addressed considering the discrete nature of the output voltage vectors generated by the NPC single-phase converter. An approach similar to the two-dimensional modulation technique can be used to describe the control region [27]-[29].

The control region associated to the single-phase NPC converter is represented in Fig. 3. In this plot, the nine available output voltage vectors are defined by the pair $(S_a, S_b)$. Several voltage sequences can be defined in the control region depicted in Fig. 3. However, a simple approach will be described in this work for the sake of clarity. Further analysis of this issue will be addressed in future work.

---

Fig. 3. Control region showing the discrete output voltage vectors generated by the single-phase full-bridge NPC converter.

Fig. 4. Proposed switching sequences generated by combining three output voltage vectors.

**A. A Simple Switching Sequence Definition**

In order to define the switching sequences, it is important to analyze the problem to be solved. The first step is to find the application times, $T_{Seq_m}$, for a given switching sequence, $Seq_m$ as per (9). Recalling (25) and (26), and considering (15), for a given sequence the system is reduced to

$\varepsilon_0 - (f_{i_1} - f_{i_3})T_1 - (f_{i_2} - f_{i_3})T_2 - f_{i_3}T_3 = 0. \quad (29)$

From (29), it can be observed that the solution for the system is not unique. Therefore, an additional constraint can be included to find a straightforward solution to determine the switching sequences.

If $Seq_{\text{opt}}$ and $T_{\text{opt}}$ were defined, then an equivalent control signal $v_m$ could be calculated as

$v_m = \frac{1}{T_s} \left( v_{abl,1}t_1 + v_{abl,2}t_2 + v_{abl,3}t_3 \right), \quad (30)$

where $\{ v_{abl,1}, v_{abl,2}, v_{abl,3} \}$ and $\{ t_1, t_2, t_3 \}$ are taken from the sets $Seq_{\text{opt}}$ and $T_{\text{opt}}$, respectively.

Taking into account that a degree of freedom exists, the control region is divided, as seen in Fig. 4, in order to achieve a similar behavior of the single-phase full-bridge NPC converter as if modulated by unipolar PWM scheme. In that case, the equivalent control signal, $v_m$, should move...
 proper path and direction to go through the selected switching approach are shown in Table III. These switching sequences, along the discontinuous grey line in Fig. 4. Therefore, only four switching sequences, Seqj, with \( j \in \{1, \ldots, 4\} \) are needed to synthesize \( v_m \). The switching sequences for this approach are shown in Table III. These switching sequences and their associated sector are depicted in Fig. 4. In addition, a proper path and direction to go through the selected switching sequences has been chosen, as described by the arrows in Fig. 4.

Under the assumption that \( v_m \) moves on the dashed grey line in Fig. 4, then the voltage vectors \( v_{abj,1} \) and \( v_{abj,3} \) should be applied during the same time duration, i.e., \( t_3 = t_1 \). In this way, it is ensured that \( v_m \) is located over the desired line in the control region. Using this constraint, the system (29) can be solved and the application times for each voltage vector in the switching sequence are

\[
\begin{align*}
t_1 |_{Seqm} & = \frac{e_{i0} - f_{i1,2} T_s}{(f_{i1,1} - 2f_{i1,2} + f_{i1,3})}, \\
t_2 |_{Seqm} & = T_s - 2t_1, \\
t_3 |_{Seqm} & = t_1.
\end{align*}
\]

Then, the OSS is determined by solving (28) as described in Section III. The implementation of the new switching sequences can be performed as described in Table IV, where \( \delta_{1a} \) and \( \delta_{2a} \) stand for the duty cycles of the power switches \( S_{a1} \) and \( S_{a2} \) in leg \( a \) in Fig. 1, respectively, while \( \delta_{1b} \) and \( \delta_{2b} \) represent the duty cycles of the power switches \( S_{b1} \) and \( S_{b2} \) in leg \( b \) in Fig. 1, respectively. A block diagram of the proposed OSS-MPC strategy is presented in Fig. 5.

### TABLE III

<table>
<thead>
<tr>
<th>Switching sequence</th>
<th>Voltage vector sequence</th>
</tr>
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<tbody>
<tr>
<td>Seq0</td>
<td>{7, 6, 3}</td>
</tr>
<tr>
<td>Seq1</td>
<td>{7, 4, 3}</td>
</tr>
<tr>
<td>Seq2</td>
<td>{5, 4, 1}</td>
</tr>
<tr>
<td>Seq3</td>
<td>{5, 2, 1}</td>
</tr>
</tbody>
</table>

### TABLE IV

<table>
<thead>
<tr>
<th>Sector</th>
<th>( v_{abj} )</th>
<th>( S_a )</th>
<th>( S_{a1} )</th>
<th>( S_{a2} )</th>
<th>( S_{b} )</th>
<th>( S_{b1} )</th>
<th>( S_{b2} )</th>
<th>Duty Cycles</th>
</tr>
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<tr>
<td>0</td>
<td>7</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>( \delta_{1a} = 0 )</td>
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<tr>
<td></td>
<td>6</td>
<td>-1</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>( \delta_{2a} = \frac{1}{T_s} )</td>
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<tr>
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<td>0</td>
<td>( \delta_{1b} = 0 )</td>
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</table>

Thus, the OSS is determined by solving (28) as described in Section III. The implementation of the new switching sequences can be performed as described in Table IV, where \( \delta_{1a} \) and \( \delta_{2a} \) stand for the duty cycles of the power switches \( S_{a1} \) and \( S_{a2} \) in leg \( a \) in Fig. 1, respectively, while \( \delta_{1b} \) and \( \delta_{2b} \) represent the duty cycles of the power switches \( S_{b1} \) and \( S_{b2} \) in leg \( b \) in Fig. 1, respectively. A block diagram of the proposed OSS-MPC strategy is presented in Fig. 5.

### V. EXPERIMENTAL RESULTS

Experimental results of a single-phase three-level NPC converter governed by the proposed OSS-MPC strategy are presented in this section to validate the effectiveness and performance of the proposed controller. The following results have been obtained with the parameters showed in Table V by using the experimental setup presented in Fig. 6.

In general, MPC algorithms have a significant computational burden. However, due to the development in processing power of control hardware, predictive control algorithms can be implemented in standard hardware platforms [30]. The proposed OSS-MPC particularly performs the number of operations reflected in Table VI. Although this amount of computations is not small, they can be executed in real time in any standard control hardware platform. For the experiments, the control algorithm was implemented in a DS1106 DSPACE platform, while the switching sequence were generated in a DS5203 FPGA board. The FPGA board provides the interruption signal to the processor at a predetermined sampling frequency \( f_s = 1/T_s \). In response to the interruption signal, the control algorithm generates the switching duty cycles that returns into the FPGA to finally firing the NPC switches according to Table IV. Since \( t_1 \) and \( t_3 \) have been considered to be equal, a symmetrical switching pattern [31] between two consecutive switching sequences is used. The symmetrical switching pattern allows one to implement a faster sampling
<table>
<thead>
<tr>
<th>Variable</th>
<th>Description</th>
<th>Value (p.u.)</th>
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<tr>
<td>$S_r$</td>
<td>Total rated apparent power</td>
<td>2.5kVA</td>
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<tr>
<td>$v_s$</td>
<td>grid-voltage</td>
<td>230 V</td>
</tr>
<tr>
<td>$V_{dc}$</td>
<td>dc capacitor voltage</td>
<td>400 V</td>
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<td>$L$</td>
<td>Filter inductor</td>
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<tr>
<td>$r$</td>
<td>Filter resistance</td>
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</tr>
<tr>
<td>$f_s$</td>
<td>Sampling frequency</td>
<td>10 kHz</td>
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<tr>
<td>$f_{sw}$</td>
<td>Switching frequency per leg</td>
<td>5 kHz</td>
</tr>
</tbody>
</table>

Table V: System Parameters

![2.5 kVA experimental prototype.](image)

A. Dynamic Performance

As an initial test, a step change in the amplitude of the current reference $i_s^*$ from 10 A to 15 A is introduced as depicted in Fig. 7. This figure includes the grid voltage, $v_s$, which is affected by the current ripple due to the fact that $v_s$ comes from a non-stiff low voltage ac source. Since implementing the proposed control algorithm requires the measured value of $v_{s,k}$, this voltage is obtained through a second order generalized integrator (SOGI) single-phase phase-locked-loop [32]. The output of this block provides a reconstructed version of $v_{s,k}$ which is free of harmonic distortion, and therefore useful to run predictions. The converter output voltage shown in Fig. 7(c) presents a three-level waveform as expected, where no undesired spikes in the voltage are observed.

In Fig. 8, a zoom view of the results of the OSS-MPC test is depicted. Fig. 8(a) shows that the grid current effectively tracks its reference when a step change is applied. In this case, the controller behaves correctly by forcing to apply the switching sequence that produces the lowest available output (-400 V), as shown in Fig. 8(b). Moreover, a response of 1 ms in the tracking of the current is achieved when a step change of 1.5 p.u. is applied.

For comparison purpose, the same test is performed when the NPC converter is governed by a standard FCS-MPC and a traditional Resonant-Proportional Controller (RPC) adopted from [11] and [9] respectively. The closed-loop performance obtained when using FCS-MPC is depicted in Fig. 9. Here, one can observe that the current also achieves its reference in 1 ms (see Fig. 9(a)). Therefore, the proposed control strategy is able to provide a fast closed-loop dynamic that matches the one obtained with FCS-MPC. In addition, Fig. 10 and Fig. 11 show the results for the same test when the the converter is governed by RPC. A damping factor $\xi$ equal to 0.707, and two different close-loop band width (BW) equal to 550 Hz and 1100 Hz were selected. It can be noticed that the RPC with larger BW produces a large overshoot (see Fig. 11(a)), which is not observed with the proposed OSS-MPC. To mitigate this, an RPC with lower BW can be implemented. However, as
expected, this leads to a low dynamic response as shown in Fig. 10(a). The details about the RPC implementation have been omitted for the sake of brevity, but can be found in [9].

B. Steady State Performance

In Fig. 12, experimental results of the proposed control strategy in the steady state operation are presented. A nearly sinusoidal grid-current is achieved, while the associated spectrum presents harmonics around 10 kHz which is twice the switching frequency per leg. The harmonic content in the grid current at frequencies below 10 kHz are characterized by a magnitude less than 0.25 % of the fundamental component. Ideally, the third and fifth harmonics should be cancelled. However, the harmonic content of the current depends not only on the current tracking but also on the harmonics presented in the reference signals. Clearly, an optimization of the single-phase PLL may be carried out to reduce the lower harmonics.

Nevertheless, the harmonic content is still in concordance with the recommendations of the IEEE Std. 519, [33].

C. Parameters’ Sensitivity

It follows from (8) and (15) that the proposed OSS-MPC requires information about the output filter to carry out prediction calculations needed to find the OSS. Therefore, it is important to test the controller behavior under parameter uncertainties. As a final test, inductance value variations were performed in order to experimentally obtain the distortion indices related with uncertainty in the output filter value. Fig. 13(a) summarizes the distortion indices obtained when the output filter changes, but the controller is still set to work with the rated value of $L$. Two types of distortion indices are used. The total harmonic distortion (THD) and THD until the 50$^{th}$ harmonic ($\text{THD}_{50}$). The results show that the indices
raise close to 5% when the actual inductance is 50% of the rated value. The controller responds to the lack of accurate information by increasing the tracking error as shown in Fig. 13(b). For this reason, the small variation of weighted THD (WTHD) around 1 is useful to show that uncertainties in L affect the tracking error but still the controller behaves as intended by pushing the lowest harmonics near to the switching frequency.

VI. CONCLUSION

In this work, the optimal switching sequence MPC (OSS-MPC) algorithm focused on the current control loop for single-phase full-bridge NPC power converters has been presented. The proposed OSS-MPC belongs to the continuous control loop dynamic performance that matches the one obtained with standard FCS-MPC but with the advantage of obtaining a well-defined and concentrated current spectrum. Robustness of the proposed strategy under system parameter uncertainties has been also tested. Practical results have shown that the proposed controller performs well even under large parameter deviations.

REFERENCES


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